

Electronic Structure and Bonding in YTi_2Ga_4 – A Gallide with Linear Titanium Chains and Four-bonded Gallium Atoms

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The gallium-rich ternary intermetallic compound YTi_2Ga_4 is isotypic with YbMo_2Al_4 , $I4/mmm$, $Z = 2$. Yttrium is located in a large cage built up by 12 gallium atoms. Chains of condensed Y@Ga_{12} polyhedra and linear titanium chains build up a tetragonal rod packing. The gallium atoms are bonded within Ga_4 squares (265 pm Ga–Ga) which are condensed *via* longer Ga–Ga bonds (292 pm) to a three-dimensional gallium substructure with formally four-connected gallium, in agreement with a Bader charge partitioning scheme $[\text{YTi}_2]^{4+}[\text{Ga}_4]^{4-}$. These features are addressed with electronic structure and chemical bonding considerations. The metallic behavior of YTi_2Ga_4 is found to be of the itinerant electron type within the valence band and Ti *d*-like states at E_F . Ga–Ga and Ti–Ga bonding characteristics provide mechanical properties derived from the full set of elastic constants leading to a brittle material.

Key words: Gallide, Intermetallic Compound, Electronic Structure, Yttrium, Titanium

Introduction

The aluminide YbMo_2Al_4 [1] crystallizes with its own structure type, space group $I4/mmm$, with peculiar substructures. The molybdenum atoms form linear chains which extend along the *c* axis, which are separated by Al_4 squares. GdMo_2Al_4 and ErMo_2Al_4 are isotypic with the ytterbium compound. This structure type has also been observed for a variety of gallides RTi_2Ga_4 ($R = \text{Zr, Sc, Y, Tb, Dy, Ho, Er, Tm, Lu}$) [2–6] and RV_2Ga_4 ($R = \text{Sc, Zr, Er, Hf}$) [2], the indide $\text{SrAu}_{4.76}\text{In}_{1.24}$ [7], the cadmium compounds CaAu_4Cd_2 , SrAu_4Cd_2 , and EuAu_4Cd_2 [8] as well as the solid solutions $\text{YbCu}_{5.1}\text{Al}_{0.9}$ [9], $\text{YbCu}_{5.12}\text{Al}_{0.88}$ [10] and $\text{CeCu}_{4.7}\text{Mn}_{1.3}$ [11]. From the point of view of chemical bonding, the coloring (*i. e.* exchanging the transition metal and *p*-element positions) of the polyanionic network is an interesting question, regarding *e. g.* YbMo_2Al_4 *vs.* SrAu_4Cd_2 ; aluminides *vs.* aurides *etc.*

In continuation of our studies on the structural data and chemical bonding behavior of YbMo_2Al_4

type intermetallics [7, 8] we have now investigated the electronic structure of YTi_2Ga_4 [4]. The purpose of this work is to present further analyses of the electronic band structure and the chemical bonding using computational methods built within the well-established quantum-theoretical density functional theory (DFT) framework [12, 13]. Two complementary computational methods were used. The Vienna *ab initio* simulation package (VASP) code with the PAW method [14, 15] allows geometry optimization, establishing the energy-volume equation of states EOS as well as the set of elastic stiffness constants and an analysis of the charge density. The full analysis of the electronic structure and the chemical bonding is then carried out using the full potential scalar-relativistic augmented spherical wave (ASW) method [16, 17]. The PBE generalized gradient approximation (GGA) functional [18], accounting for the effects of exchange and correlations within DFT, was considered in all calculations. For details of the methods the reader is referred to the theoretical development presented in ref. [19].

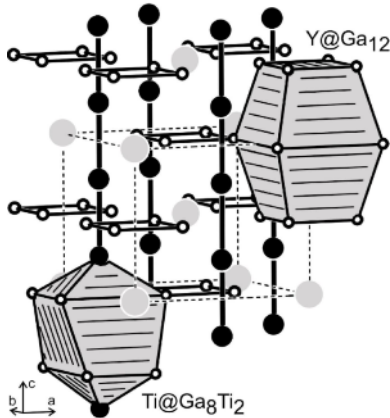


Fig. 1. The crystal structure of YTi₂Ga₄. Yttrium, titanium and gallium atoms are drawn as medium grey, black filled and open circles, respectively. The coordination polyhedra around the yttrium and titanium atoms as well as the titanium chains and the Ga₄ squares are emphasized.

Results

Crystal chemistry

The crystal structure of YTi₂Ga₄ (*I4/mmm*, *Z* = 2) [4] is shown in Fig. 1. The striking sub-structures are linear titanium chains which extend in *c* direction. The Ti–Ti distances of 274 pm are remarkably short when compared with *hcp* titanium (6×290 and 6×295 pm) [20] or the chains in Ti₂In₅ (300 pm) [21]. This is indicative of substantial Ti–Ti bonding. The titanium chains are separated by Ga₄ squares with Ga–Ga distances of 265 pm, similar to those in the crystals of the element (1×244 and 6×270 pm) [20]. Each titanium atom has two titanium neighbors within its chain and eight gallium neighbors at 279 pm Ti–Ga, somewhat longer than the sum of the covalent radii of 257 pm [22]. These Ti@Ga₈Ti₂ polyhedra interpenetrate each other along the *c* axis. Each titanium atom within a chain is a center of such a polyhedron. The yttrium atoms have twelve gallium neighbors at Y–Ga distances ranging from 288 to 332 pm. These Y@Ga₁₂ polyhedra are condensed *via* common square faces along the *c* axis. Since the Y@Ga₁₂ polyhedra comprise all gallium atoms in their coordination shell, we can alternatively describe the YTi₂Ga₄ structure as a tetragonal packing of rods of consensed Y@Ga₁₂ polyhedra and linear titanium chains. The peculiar features of chemical bonding are addressed in detail below.

Geometry optimization, equation of state and elastic modules

Table 1 provides the experimental and calculated (in parentheses) structural parameters for YTi₂Ga₄. There is a good agreement for the gallium *x* coordinate (Wyckoff site 8*h*) but the geometry-optimized *a* and *c* parameters are calculated larger, respectively smaller, than the experimental ones, leading to a larger calculated cell volume of 0.1251 nm³ per formula unit (fu) *versus* $V_{\text{exp}} = 0.1235$ nm³ per fu. This follows from the trend usually observed for the GGA DFT functional which is known to be underbinding, *i. e.* overestimating lattice spacing. Nevertheless the agreement is good enough to examine the physical properties such as the mechanical characteristics. One derives the equilibrium zero pressure parameters from the energy-volume, $E(V)$, equation-of-state (EOS) with calculations around minima found from geometry optimization. The resulting values are plotted in Fig. 2. The fit of the curves with a Birch EOS [23]:

$$E(V) = E_0(V_0) + [9/8]V_0B_0 \left[\left((V_0/V)^{2/3} - 1 \right)^2 + [9/16]B_0(B' - 4)V_0 \left[\left((V_0/V)^{2/3} - 1 \right)^3 \right] \right]$$

provides E_0 , V_0 , B_0 , and B' , respectively. The equilibrium energy, the volume, the bulk modulus and its pressure derivative are given in the inset. The fitted curves reproduce the trends of the geometry optimization for the volume. The corresponding zero pressure bulk modulus of $B_0 = 97$ GPa places the title compound in the range of intermetallics [24] which are softer than typical oxides and ceramics.

We also determined the elastic properties by performing finite distortions of the lattice and deriving the elastic constants from the strain-stress relationship. In tetragonal symmetry there are six independent elastic stiffness constants C_{11} , C_{33} , C_{44} , C_{66} , C_{12} , and C_{13} . Most samples are polycrystalline, where monocrystalline grains are randomly oriented so that on a large

Table 1. Experimental [4] and calculated (in parentheses) lattice and atomic parameters for YTi₂Ga₄, space group *I4/mmm*: $a = 671.2$ pm (677 pm), $c = 548.4$ pm (546 pm); Total energy per formula unit (fu): -37.38 eV.

Atom	Wyckoff site	<i>x</i>	<i>y</i>	<i>z</i>
Y	2 <i>a</i>	0	0	0
Ti	4 <i>d</i>	0	1/2	1/4
Ga	8 <i>h</i>	0.303 (0.302)	<i>x</i>	0

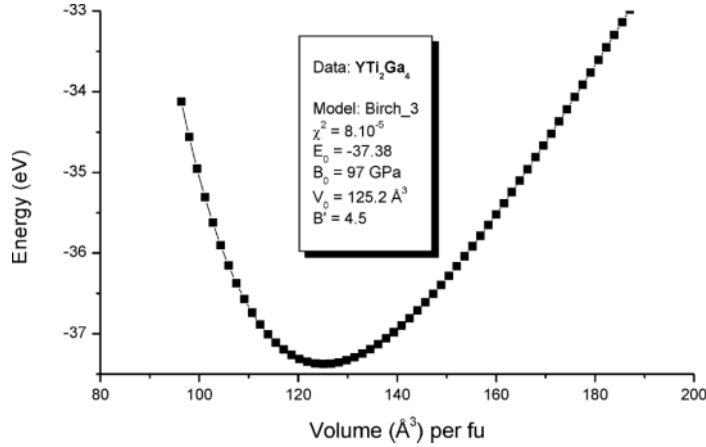


Fig. 2. YTi₂Ga₄: Energy volume curve and fit values (in the inset) from a Birch 3rd order equation of state.

scale such materials can be considered as statistically isotropic. They are then completely described by the bulk modulus B and the shear modulus G , which may be obtained by averaging the single-crystal elastic constants. The most widely used averaging procedure for the elastic stiffness constants is Voigt's method [25] based on a uniform strain. The calculated set of elastic constants in YTi₂Ga₄ in units of GPa are:

$$C_{11} = C_{22} = 175; C_{12} = 77; C_{13} = 55;$$

$$C_{33} = 160; C_{44} = 99 \text{ and } C_{66} = 53.$$

All C_{ij} values are positive and their combinations: $C_{11} > C_{12}$, $C_{11}C_{33} > C_{13}^2$ and $(C_{11} + C_{12})C_{33} > 2C_{13}^2$ obey the rules pertaining to the mechanical stability of the intermetallic compound. The bulk (B_V) and shear (G_V) modules according to Voigt's method are formulated as:

$$B_V = 1/9 \{2(C_{11} + C_{12}) + 4C_{13} + C_{33}\} \text{ and}$$

$$G_V = 1/30 \{12C_{44} + 12C_{66} + C_{11} + C_{12} + 2C_{33} - 4C_{13}\}$$

The numerical values are then: $B_V = 98$ GPa and $G_V = 72$ GPa. The value of B_V is in close agreement with the one obtained from the EOS fit (Fig. 2, inset) thus validating the two different approaches. The shear modulus which defines the rigidity of the material is significantly lower. The Pugh's G/B ratio [26] is an indicator of brittleness or ductility for $G/B > 0.5$ and $G/B < 0.5$, respectively. For YTi₂Ga₄ $G/B = 0.73$, indicating brittleness, contrary to the properties of coinage metals Ag, Pt, or Au with G/B ratios in the

range of 0.4–0.2 [27]. This behavior should arise from directional bonding characteristics (*vide infra*).

Analysis of charge transfer

The analysis of the charge density issued from the self consistent calculations can be done using the AIM (atoms in molecules theory) approach [28] developed by Bader who devised an intuitive way of splitting molecules into atoms as based purely on the electronic charge density. Typically in chemical compounds, the charge density reaches a minimum between atoms, and this is the natural region to separate them from each other. Such an analysis can be useful when trends between similar compounds are examined; it does not constitute a tool for evaluating absolute ionizations. Bader's analysis is done using a fast algorithm operating on a charge density grid arising from high precision VASP calculations and generates the total charge associated with each atom. The results of computed charge changes (ΔQ) are such that they lead to neutrality when the respective multiplicities are accounted for:

$$\Delta Q(Y) = 1.376; \Delta Q(Ti) = 1.315; \Delta Q(Ga) = -1.$$

From these results one can formally write $[YTi_2]^{4+}[Ga_4]^{4-}$, thus classifying YTi₂Ga₄ as a gallide. According to this charge partitioning scheme the gallium components are formally isoelectronic with germanium, but we only observe two-connected gallium within the Ga₄ rings (265 pm Ga–Ga) instead of four-connected gallium. If we consider also the longer Ga–Ga distances of 292 pm between the

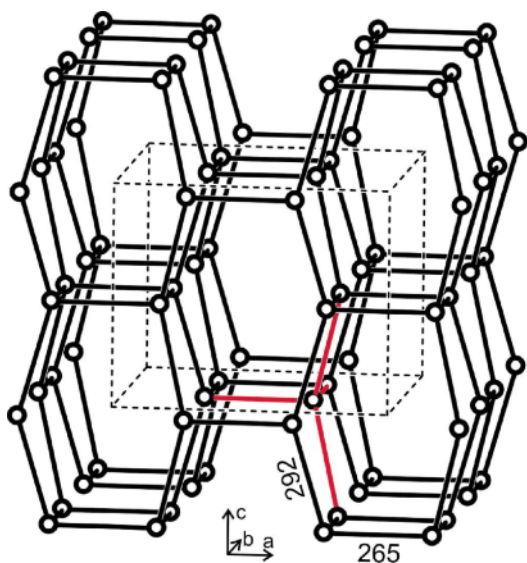


Fig. 3 (color online). The gallium substructure of YTi_2Ga_4 . One distorted Ga_4 tetrahedron is emphasized in red color. Relevant interatomic distances are indicated.

Ga_4 rings, we obtain the three-dimensional gallium substructure (Fig. 3) which shows strongly distorted tetrahedral gallium coordination with Ga–Ga–Ga angles of 90, 104.1 ($2\times$) and 139.7°. Thus, the Ga^- entities formally fulfill Zintl’s rule. Ideal $\text{GaGa}_{4/4}$ tetrahedra with 268 pm Ga–Ga distance occur in the NaTi-type Zintl phase LiGa [29]. CaGa_2 [30] contains elongated $\text{GaGa}_{4/4}$ tetrahedra with 265 and 306 pm Ga–Ga and Ga–Ga–Ga angles of 103.5 and 114.7°, comparable to the gallium substructure of YTi_2Ga_4 . Nevertheless, YTi_2Ga_4 is not a Zintl phase in the classical sense. We observe strong covalent bonding of the gallium substructure with the titanium chains and pronounced metallic character.

The bonding peculiarities are further illustrated by the electron localization function (ELF). ELF is a normalized function ($0 \leq \text{ELF} \leq 1$) [31, 32]. In the plots three main localization zones are identified: no localization for $\text{ELF} = 0$ (blue areas), strong localization for 1 (red areas) and free electron like behavior for $\text{ELF} = 1/2$ (green areas). The selected planes are shown in Fig. 4 for slices perpendicular to the tetragonal c axis. The basal plane comprising two Ga and one Y (Fig. 4a) shows significant localization around the Ga atoms and an extension towards the intermediate plane (Fig. 4b). The red zones in the immediate surroundings of Y are due to the core electrons included in

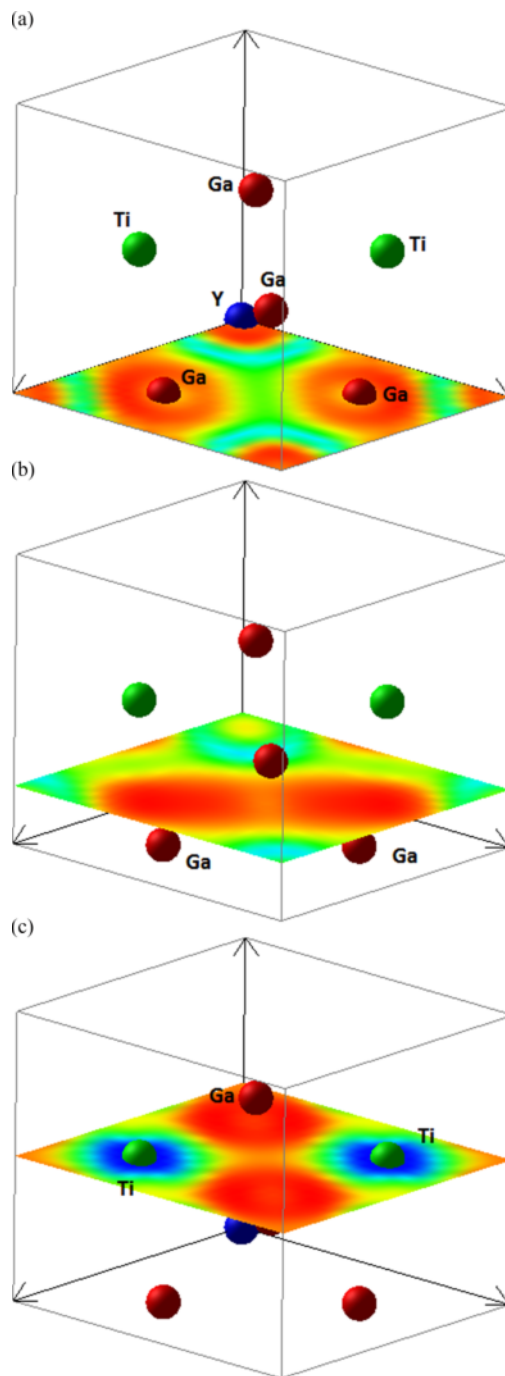


Fig. 4 (color online). YTi_2Ga_4 : ELF slice planes perpendicular to the tetragonal c axis. a) Basal plane comprising two Ga and one Y (at the origin); b) intermediate plane showing strong localization arising from the two gallium atoms at the basal plane and c) slice plane at $z = 1/2$ with titanium showing no localization ELF contours (*cf.* text).

the PAW method. The slice plane at $z = 1/2$ (Fig. 4c) contains Ti exhibiting no localization with blue ELF contours. The strong localization ($\text{ELF} \sim 1$) around Ga is more explicit than in the first panel and points to Ga–Ga bonding as shown in the next section.

Electronic structure and chemical bonding

Using the experimental structural data for YTi_2Ga_4 (Table 1) we analyze the electronic structure using all electron calculations with the full potential ASW method [16, 17]. The chemical bonding for pair interactions is analyzed qualitatively using the crystal orbital overlap populations COOP based on the overlap matrix elements S_{ij} [33]. In the plots positive, negative and zero magnitude COOP indicate bonding, antibonding and non bonding interactions, respectively.

At self-consistent energy and charge convergence the transfer of electrons follows the trend discussed above. The site projected densities of states (PDOS) are shown in Fig. 5. The zero energy along the x axis is with respect to the Fermi level E_F . The compound is metallic with mainly d -like PDOS arising from the lower part of Ti d states. This is due to the low filling of the Ti $3d$ subshell with 2 electrons in the atomic state so that the d band is centered above E_F within the conduction band. The valence band from -10 eV up to E_F is dominated by Ga p states, and the valence band is mostly of itinerant s, p like character. Similar PDOS shapes between Ga and Ti are noted for the lower part

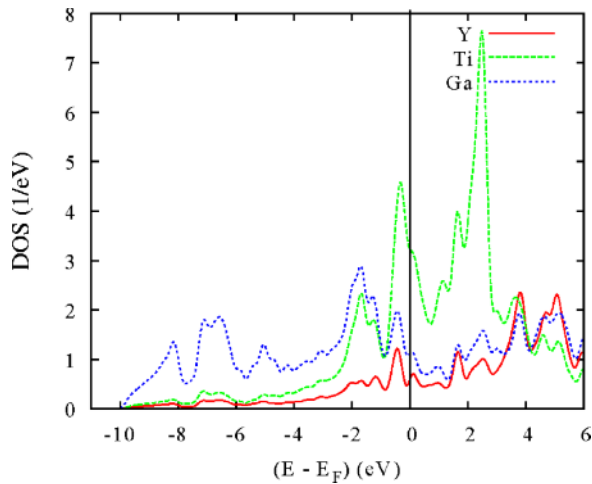


Fig. 5 (color online). YTi_2Ga_4 : Site projected density of states (PDOS).

of Ti d at ~ -2 eV, and quantum mixing can be expected leading to significant Ti – Ga bonding. Nevertheless, the similar PDOS shapes of Y and Ti just below E_F indicate quantum mixing involving d states.

Fig. 6 shows the COOP for the different interactions. The first panel (a) shows the COOP accounting for two atoms of each kind in order to allow comparisons of bond strengths. Clearly the Ga – Ga interaction is dominant and is found to be of bonding nature (positive COOP); it also reflects the Bader charge trends as well as the ELF plots presented in the preceding section. Ti – Ti bonding is largely present in the DOS region where d states are found, thus indicating that Ti – Ti interaction along the chains is ensured by d orbitals. This also follows the course of the dis-

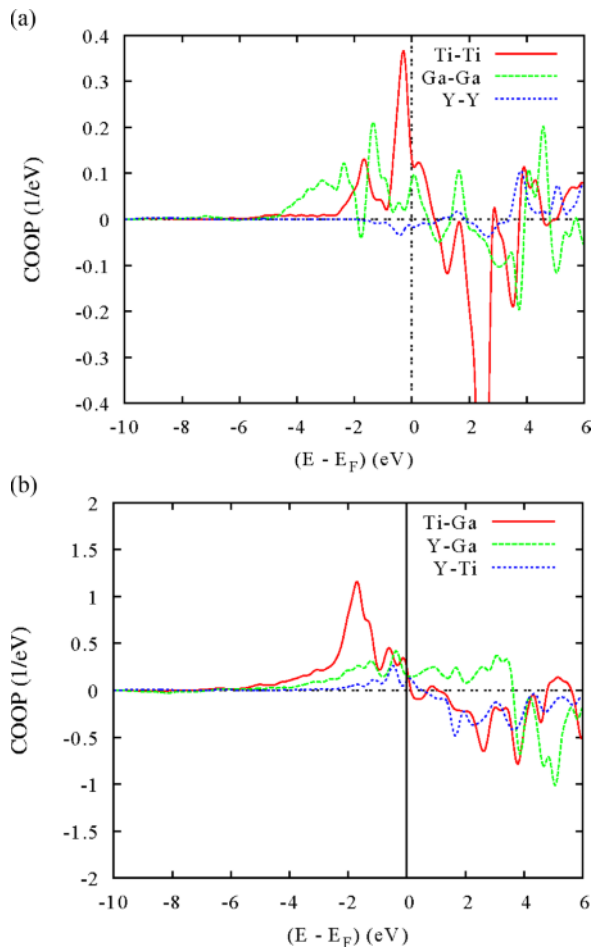


Fig. 6 (color online). YTi_2Ga_4 : Chemical bonding according to the COOP criterion: a) for atoms of the same type, b) for atoms of different types.

tances whereby short Ti – Ti ($d_{\text{Ti-Ti}} = 274$ pm) connections are identified. Similar bonding characteristics were computed for Hf_2In_5 with Hf – Hf chains [34]. The titanium chains in the RETi_2Ga_4 gallides are non-magnetic. Temperature-dependent susceptibility measurements on samples with $\text{RE} = \text{Tb} - \text{Er}$ [5] reveal only the paramagnetic contribution of the RE^{3+} ions.

Fig. 6b shows the bonding between the different chemical species accounting for their respective site multiplicities (Table 1). Strong bonding is observed for Ti – Ga, followed by the (much smaller) Y – Ga and Y – Ti COOPs which are vanishingly small ex-

cept in the vicinity of E_F involving the d bands from both Y and Ti. The relative bonding strengths follow the course of the distances (in pm): $d_{\text{Ga-Ga}} = 265$; $d_{\text{Ti-Ga}} = 279$ and $d_{\text{Y-Ga}} = 288$.

The directional Ga – Ga and Ti – Ga interactions provide brittle mechanical properties as confirmed by the analysis of the elastic constants.

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