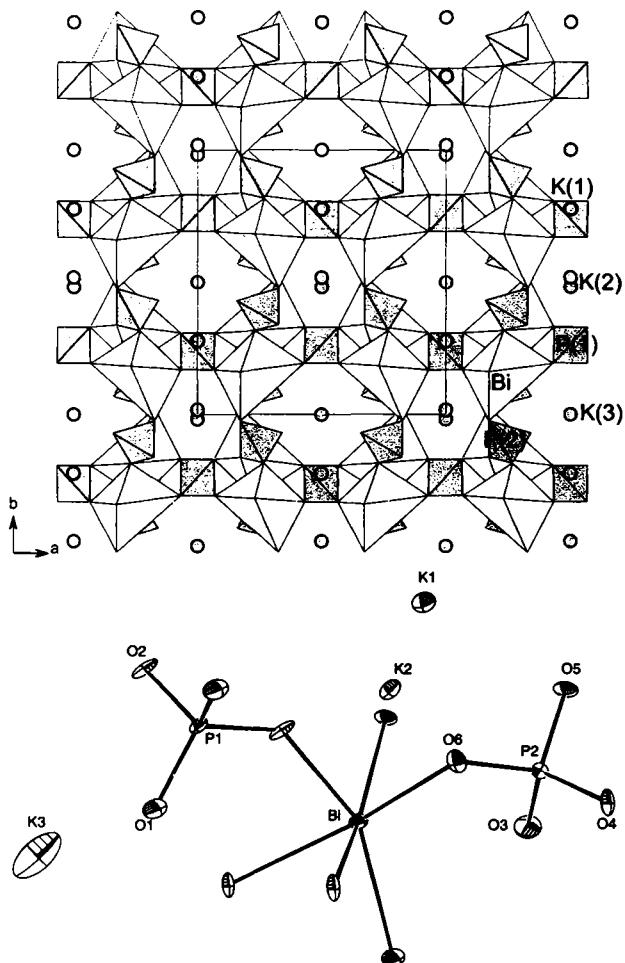


# Crystal structure of tripotassium dibismuth phosphate, $K_3Bi_2(PO_4)_3$

C. Falah, H. Boughzala and T. Jouini\*

Faculté des Sciences, Département de Chimie, 1060 Campus Universitaire, Tunis, Tunisia

Received June 28, 2001. CSD-No. 409582



## Abstract

$Bi_2K_3O_{12}P_3$ , monoclinic,  $C12/c1$  (No. 15),  $a = 13.828(7)$  Å,  $b = 13.482(5)$  Å,  $c = 6.808(3)$  Å,  $\beta = 114.94(4)^\circ$ ,  $V = 1150.9$  Å $^3$ ,  $Z = 4$ ,  $R_{gt}(F) = 0.028$ ,  $wR_{ref}(F^2) = 0.090$ ,  $T = 293$  K.

## Source of material

The title compound was prepared by the reaction of  $K_2CO_3$ ,  $Bi_2O_3$  and  $NH_4H_2PO_4$  in the molar ratio  $K$ :  $Bi$ :  $P = 3$ : 2: 3. The mixture was first heated at 573 K until decomposition, and then kept for 20 days at 823 K. A slow cooling to room temperature led to colourless plate crystals of  $BiPO_4$  (high temperature form [1]) together with colourless parallelepiped crystals of  $K_3Bi_2(PO_4)_3$ .

## Discussion

Double orthophosphates of bivalent, trivalent or quadrivalent cations with alkali metals are promising materials in the field of inorganic material technology. Several phosphates such as  $M^{I}_3M^{III}_2(PO_4)_3$  ( $M^I = Li, Na$ ;  $M^{III} = Cr, Fe, Sc$ ) have been extensively investigated: they are known to be fairly good ionic conductors structurally related to Nasicon ( $Na_3Zr_2Si_2PO_12$ ). Furthermore, it is well established that ions such as  $Bi^{3+}$  often generate distorted structures due to the electrostatic effect of the lone pair of electrons. In the system  $K$ - $Bi$ - $P$ - $O$ , several well-characterized phases have been reported:  $Bi(PO_3)_3$  [2],  $Bi_2P_4O_{13}$  [3],  $BiPO_4$  [1],  $K_3BiO_3$  [4],  $K_4Bi_2O_5$  [5],  $KBiO_2$  [6],  $K_2Bi_3O(PO_4)_3$  [7],  $KBi(PO_3)_4$  [8],  $KBi_4O_5(PO_4)$  [9] and  $K_3Bi_2(PO_4)_3$  [9]. To our knowledge, three structural works of double phosphates of bismuth and alkali metals have been published  $K_2Bi_3O(PO_4)_3$  [7],  $Na_3Bi(P_2O_7)_2$  [10] and  $Na_3Bi_5(PO_4)_6$  [11]. We have identified two compounds: the title compound  $K_3Bi_2(PO_4)_3$  and an interesting non-centrosymmetric structure of  $K_6Bi_2(P_2O_7)_3$  [12].

The structure of the title compound is built up from  $BiO_6$  octahedra and  $PO_4$  tetrahedra sharing corners to form a three-dimensional framework enclosing two types of tunnels where  $K^+$  cations reside. The crystal structure consists of infinite chains of dimers of edge-sharing  $BiO_6$  octahedra to form a  $Bi_2O_{10}$  unit. These infinite chains are linked together by  $P(1)O_4$  and  $P(2)O_4$  tetrahedra to form layers parallel to the (010) plane. The ten vertices of the dimer are shared with eight  $PO_4$  tetrahedra. Two of the eight phosphates form bridges between two  $Bi$  atoms in a dimer. The  $BiO_6$  octahedra appear to be highly distorted, the angle subtended by two of the axial oxygens is  $151.3(3)^\circ$ . This distortion probably occurs as a result of the need to accommodate to the connectivity of the  $PO_4$  tetrahedra, which are rather rigid entities. This framework defines large tunnels running along the  $c$  direction (see figure). The structure is closely related to the alluaudite structure type [13,14], but there are two important differences: one site is empty and the coordination number of the  $K$  atoms. The X(1) site (1/2,0,0) is occupied by  $K(3)$ , whereas the X(2) site (0,0,0) is empty. The maximum bond distance for  $K$ - $O$  determined by using the procedure in [15] with the revised radii in [16] is 3.35 Å. Accordingly,  $K(1)$ ,  $K(2)$  and  $K(3)$  ions are co-ordinated to eight, ten and six oxygen atoms, respectively, ranging from 2.684(7) Å to 3.313(7) Å, forming irregular coordination polyhedra. In contrast to  $Na_3In_2(PO_4)_3$  [17], where the coordination numbers of  $Na(1)$ ,  $Na(2)$  and  $Na(3)$  are six, eight and six oxygen atoms, respectively. The bond valence sum of  $K$ - $O$  bonds using the formula in [18] is 1.18, 1.32 and 1.01 for  $K(1)$ ,  $K(2)$  and  $K(3)$ , respectively.

In contrast to the analogous formula compound  $Na_3Sc_2(PO_4)_3$  that has the well-known Nasicon structure [19], the title compound is isotopic to  $Na_3In_2(PO_4)_3$ .

\* Correspondence author (e-mail: t.jouini@gnet.tn)

**Table 1.** Data collection and handling.

|   |  |
|---|--|
| Crystal:  | colourless parallelepipedic,<br>size $0.07 \times 0.07 \times 0.09$ mm |
| Wavelength:   | Mo $K_\alpha$ radiation ( $0.71073 \text{ \AA}$ )                      |
| $\mu$ :   | $321.05 \text{ cm}^{-1}$   |
| Diffractometer, scan mode:                              | CAD4, $\omega/2\theta$   |
| $2\theta_{\max}$ :                                      | $53.92^\circ$  |
| $N(hkl)_{\text{measured}}$ , $N(hkl)_{\text{unique}}$ : | 1363, 1257   |
| Criterion for $I_{\text{obs}}$ , $N(hkl)_{\text{gt}}$ : | $I_{\text{obs}} > 2 \sigma(I_{\text{obs}})$ , 1062                     |
| $N(\text{param})_{\text{refined}}$ :                    | 95   |
| Programs:   | SHELXS-90 [20], SHELXL-97 [21]   |

**Table 2.** Atomic coordinates and displacement parameters (in  $\text{\AA}^2$ ).

| Atom  | Site | x          | y          | z          | $U_{11}$  | $U_{22}$  | $U_{33}$  | $U_{12}$   | $U_{13}$  | $U_{23}$  |
|-------|------|------------|------------|------------|-----------|-----------|-----------|------------|-----------|-----------|
| Bi(1) | 8f   | 0.26291(2) | 0.35556(2) | 0.33079(5) | 0.0067(2) | 0.0106(2) | 0.0106(2) | -0.0006(1) | 0.0029(2) | 0.0007(1) |
| P(1)  | 4e   | 1/2        | 0.2582(2)  | 3/4        | 0.005(1)  | 0.011(2)  | 0.008(1)  | 0          | 0.000(1)  | 0         |
| P(2)  | 8f   | 0.2589(2)  | 0.3916(2)  | -0.1393(3) | 0.009(1)  | 0.009(1)  | 0.009(1)  | -0.0010(9) | 0.0040(8) | 0.0004(9) |
| K(1)  | 4e   | 1/2        | 0.4817(2)  | 1/4        | 0.011(1)  | 0.019(2)  | 0.016(1)  | 0          | 0.005(1)  | 0         |
| K(2)  | 4e   | 1/2        | 0.2226(2)  | 1/4        | 0.008(1)  | 0.009(1)  | 0.010(1)  | 0          | 0.000(1)  | 0         |
| K(3)  | 4b   | 1/2        | 0          | 0          | 0.026(2)  | 0.039(2)  | 0.041(2)  | 0.010(2)   | -0.003(2) | -0.018(2) |
| O(1)  | 8f   | 0.4307(5)  | 0.1927(5)  | 0.822(1)   | 0.010(3)  | 0.021(4)  | 0.017(3)  | -0.003(3)  | 0.002(3)  | 0.004(3)  |
| O(2)  | 8f   | 0.5669(5)  | 0.3309(5)  | 0.944(1)   | 0.007(3)  | 0.015(3)  | 0.014(3)  | -0.002(3)  | -0.002(3) | -0.006(3) |
| O(3)  | 8f   | 0.1571(5)  | 0.4312(6)  | -0.129(1)  | 0.011(3)  | 0.032(4)  | 0.023(4)  | 0.001(3)   | 0.010(3)  | -0.003(3) |
| O(4)  | 8f   | 0.2310(5)  | 0.3169(6)  | -0.3302(9) | 0.018(4)  | 0.015(4)  | 0.006(3)  | 0.003(3)   | 0.004(3)  | 0.004(3)  |
| O(5)  | 8f   | 0.3273(5)  | 0.4759(5)  | -0.171(1)  | 0.012(3)  | 0.009(3)  | 0.019(3)  | -0.003(3)  | 0.006(3)  | 0.004(3)  |
| O(6)  | 8f   | 0.3265(6)  | 0.3386(5)  | 0.080(1)   | 0.020(3)  | 0.006(3)  | 0.012(3)  | -0.002(3)  | 0.008(3)  | 0.000(2)  |

## References

- Masse, R.; Durif, A.: Etude structurale de la forme haute température du monophosphate du bismuth  $BiPO_4$ . C. R. Acad. Sci. Paris, Ser. II, **300** (1985) 849-851.
- Palkina, K.; Jost, K. H.: Crystal structure of bismuth polyphosphate  $Bi(PO_3)_3$ . Acta Crystallogr. **B31** (1975) 2281-2285.
- Bagieu Beucher, M.; Averbuch-Pouchot, M.-T.: Crystal data and crystal structure of bismuth tetraphosphate  $Bi_2P_4O_{13}$ . Z. Kristallogr. **180** (1987) 165-170.
- Zoche, N. J. M.; Jansen, M.: Synthesis and crystal structure determination of  $K_3BiO_3$  and  $Rb_3BiO_3$ . Z. Naturforsch. **52** (1997) 1031-1036.
- Zoche, N.; Sievers, R.; Jansen, M.:  $K_4Bi_2O_5$ , a novel ternary oxobismuthate III. Journal of Solid State Chemistry **139** (1998) 342-346.
- Schwedes, B.; Hoppe, R.: Die Kristallstruktur von  $KBiO_2$  sowie zur Kenntnis von  $RbBiO_2$  und  $CsBiO_2$ . Z. Anorg. Allg. Chem. **392** (1972) 97-106.
- Debreuille-Gresse, M. F.; Drache, M.; Abraham, F.: The crystal structure, phase transition and dielectric properties of  $K_2Bi_3(PO_4)_3O$ , a new oxyphosphate. J. Solid State Chem. **62** (1986) 351-359.
- Berul, S. I.; Solotczi, S. V.: Reaction of bismuth oxide with group I metal metaphosphates. Zh. Neorg. Khim. **14** (1969) 3134-3139.
- Bukhalova, G. A.; Faustova, R. S.; Savenkova M. A.: Phase-equilibria in system consisting of potassium and bismuth metaphosphates. J. Appl. Chem.-USSR **50** (1977) 162-164.
- Boughzala, H.; Jouini, T.: Préparation et structure cristalline d'un nouveau bis-diphosphate de bismuth et de sodium  $Na_5Bi(P_2O_7)_2$ . J. Solid State Chem. **143** (1999) 104-110.
- Arbib, E.; Chaminade, J. P.; Darriet, J.; Elouadi, B.: The crystal structure of eulytite  $Na_3Bi_5(PO_4)_6$ . Solid State Sciences **2** (2000) 243-247.
- Falah, C.; Boughzala, H.; Jouini T.: Un compose non centrosymetrique à larges tunnels  $K_6Bi_2(P_2O_7)_3$ . 11emes journées nationales de la société chimique de Tunisie, 5, 6 et 7 Novembre 2000.
- Yakubovich, O. V.; Simonov, M. A.; Egorov-Tismenko, Y. K.; Belov, N. V.: The crystal structure of a synthetic variety of alluaudite  $Na_2((Fe^{3+})_{0.5}(Fe^{2+})_{0.5})_2(Fe^{2+})(PO_4)_3$ . Doklady Akademii Nauk SSSR **236** (1977) 1123-1126.
- Moore, P. B.: Crystal chemistry of the alluaudite structure type: contribution to the paragenesis of pegmatite phosphate giant crystals. Amer. Mineralog. **56** (1971) 1955-1975.
- Donnay, G.; Allmann, R.: How to recognize  $O^{2-}$ ,  $OH^-$ , and  $H_2O$  in crystal structures determined by X-rays. Amer. Mineralog. **55** (1970) 1003-1015.
- Shannon, R. D.: Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides. Acta Crystallogr. **A32** (1976) 751-767.
- Lii, K. H.; Ye, J.: Hydrothermal synthesis and structures of  $Na_3In_2(PO_4)_3$  and  $Na_3In_2(AsO_4)_3$ : Synthetic modifications of the mineral alluaudite. Journal of Solid State Chemistry **131** (1997) 131-137.
- Brown, I. D.; Altermatt, D.: Bond-Valence Parameters Obtained from a Systematic Analysis of the Inorganic Crystal Structure Database. Acta Crystallogr. **B41** (1985) 244-247.
- Susman, S.; Delbecq, C. J.; Brun T. O.; Prince, E.: Fast ion transport in the Nasicon analog sodium scandium phosphate  $(Na_3Sc_2(PO_4)_3)$ : structure and conductivity. Solid State Ionics **9** (1983) 839-844.
- Sheldrick, G. M.: SHELXS-90, program for the solution of crystal structures. University of Göttingen, Germany 1990.
- Sheldrick, G. M.: SHELXL-97, program for crystal structure determination. University of Göttingen, Germany 1997.