

Structural Evolution of the Binary System Ba-Si under High-pressure and High-temperature Conditions

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A new silicon-rich binary compound BaSi_6 has been prepared by the treatment of the $\text{Ba}_8\text{Si}_{46}$ clathrate compound under a pressure of 15 GPa at 1000 °C, or from a stoichiometric mixture of BaSi_2 and Si by treatment under similar high-pressure and high-temperature conditions. The Rietveld refinements revealed that BaSi_6 is isomorphous with EuGa_2Ge_4 , and crystallizes with space group $Cmcm$ and the lattice parameters $a = 4.485(1)$, $b = 10.375(2)$, and $c = 11.969(3)$ Å. Each Ba atom is surrounded by 18 Si atoms in an irregularly shaped polyhedron $@\text{Si}_{18}$. The polyhedra are connected by sharing faces to form Ba containing tunnels along the a axis. All of the Si-rich compounds so far with atomic ratios $\text{Si}/\text{Ba} > 2$ in the binary system have been prepared only under high-pressure and high-temperature conditions. There is a general tendency that the Si/Ba ratio of the compounds increases with an increase of the pressure in the preparation.

Key words: Ba-Si System, BaSi_6 , High-pressure Phase, Clathrate

Introduction

The binary compound BaSi_2 containing $[\text{Si}_4]^{4-}$ Zintl anions crystallizes in an orthorhombic structure [1], which is stable on compression up to 7.1 GPa at r. t. At elevated temperatures, however, it undergoes an orthorhombic-trigonal transition at 5.2 GPa and 400 °C, and a trigonal-cubic transition at 600 °C [2, 3]. The structures found in the Ba-Si binary system are shown in Fig. 1. The high-pressure phases with the trigonal and cubic structures have the EuGe_2 (or CaSi_2 -like) and the SrSi_2 structures, respectively, which correspond to the structures of other disilicides of alkaline earth metals with smaller atomic radii [3, 4]. Binary compounds with atomic ratios $\text{Si}/\text{Ba} > 2$ can be obtained only under high pressures at elevated temperatures. $\text{Ba}_{24}\text{Si}_{100}$ ($\text{Si}/\text{Ba} = 4.17$) was prepared under a pressure of 1.5 GPa at 800 °C [5] and $\text{Ba}_8\text{Si}_{46}$ ($\text{Si}/\text{Ba} = 5.75$) under a pressure of 3.0 GPa at 800 °C [6]. When $\text{Ba}_{24}\text{Si}_{100}$ is compressed under a pressure of 3 GPa at 800 °C, it decomposes into a mixture of $\text{Ba}_8\text{Si}_{46}$ and Ba. These silicon-rich binary compounds belong to a silicon clathrate family: $\text{Ba}_8\text{Si}_{46}$ is isotypic with Type I gas (G) hydrate $\text{G}_x(\text{H}_2\text{O})_{46}$ [7]. The $\text{H}-\text{O}\cdots\text{H}$ hydrogen bonds of the gas hydrates are replaced by the Si-Si covalent bonds

in the Si clathrate compound, and Ba atoms are trapped in silicon polyhedral cages, two dodecahedra ($@\text{Si}_{20}$: 5^{12}) and six tetrakaidecahedra ($@\text{Si}_{24}$: $5^{12}6^2$) in the unit cell. The two types of polyhedra are linked by face sharing to form the A15 or β -tungsten structure. $\text{Ba}_8\text{Si}_{46}$ is a superconductor with a critical temperature (T_c) of 8.0 K. Note that this is the first superconductor composed of a $\text{Si}-sp^3$ three-dimensional network. $\text{Ba}_{24}\text{Si}_{100}$ also consists of Ba containing silicon dodecahedral cages ($\text{Ba}@\text{Si}_{20}$), which are linked by sharing pentagonal faces to form a chiral zeolite-like network; the rest of the Ba atoms are located in the interstices of the network. Recently, it has been found that $\text{Ba}_{24}\text{Si}_{100}$ can also become a superconductor at $T_c = 1.4$ K [8].

San-Miguel *et al.* [9] studied the structural change of $\text{Ba}_8\text{Si}_{46}$ under high pressure using a diamond anvil cell (DAC) at r. t. They revealed that $\text{Ba}_8\text{Si}_{46}$ was homothetically compressed up to 30 GPa with a reduction of the volume by 25%, and reversibly recovered on releasing the pressure. At higher pressures, above 40 GPa, irreducible amorphization occurred. An excellent review on the high-pressure properties of group IV clathrates was given by San-Miguel and Toulemonde [10]. In this study, the structural change of $\text{Ba}_8\text{Si}_{46}$ under high-pressure conditions at elevated

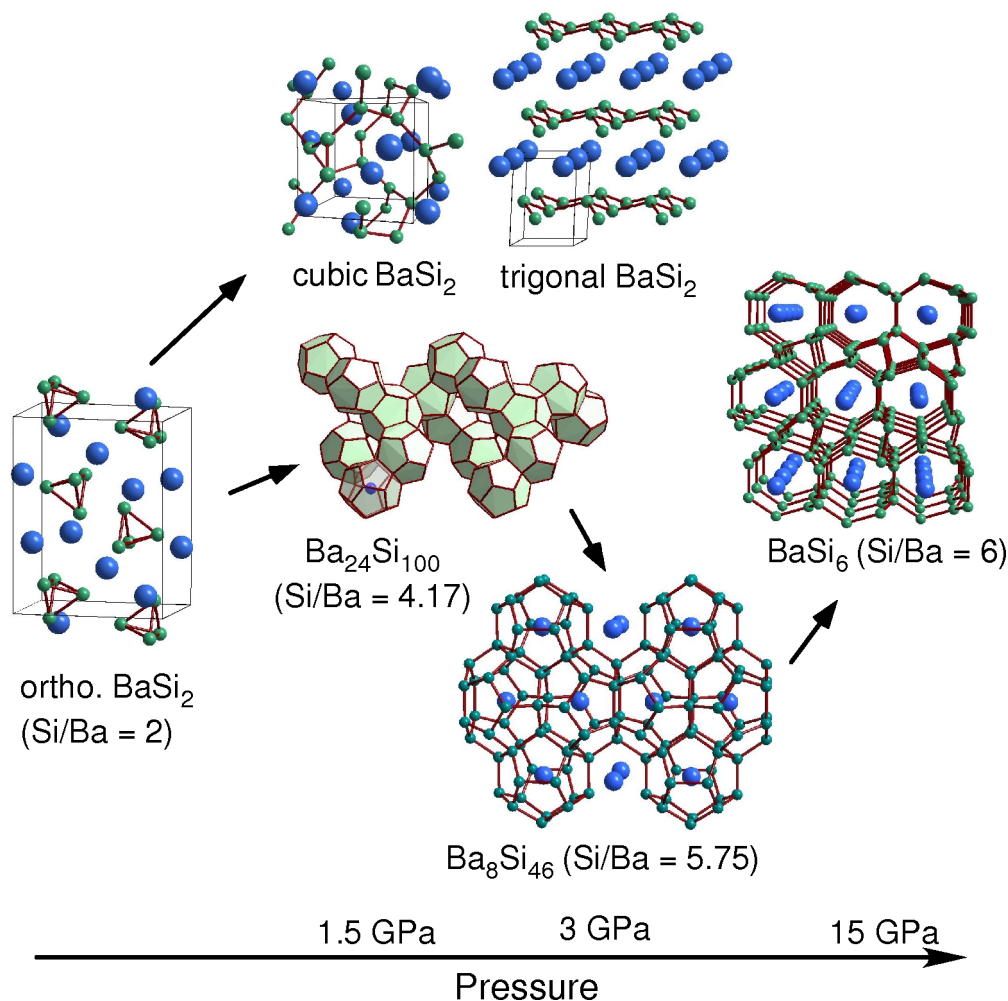


Fig. 1. Schematic illustration of various crystal structures in the binary system Ba-Si found by high-pressure and high-temperature treatments; orthorhombic BaSi_2 is transformed to trigonal BaSi_2 and cubic BaSi_2 .

temperatures has been investigated, and a new Si-rich clathrate-like phase with a composition of BaSi_6 has been found.

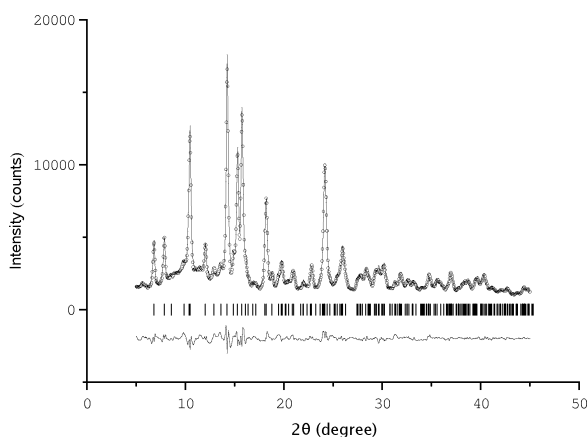
Results and Discussion

A new binary compound was obtained by the treatment of $\text{Ba}_8\text{Si}_{46}$ under a pressure of 15 GPa at 1000 °C. The XRD powder pattern could be indexed on the basis of an orthorhombic unit cell with $a = 4.485(1)$, $b = 10.375(2)$, and $c = 11.969(3)$ Å. The composition was determined to be $\text{BaSi}_{5.99}$ (Ba: 45.6, Si: 55.7, total 101.3 wt%) by EPMA. A compound showing the same XRD pattern was also obtained from a mixture of BaSi_2 and Si in a molar ratio of 1:4

by treatment under the same high-pressure and high-temperature condition. The XRD pattern was very similar to that of EuGa_2Ge_4 with space group $Cmcm$ [11], and the structure was successfully determined in the same space group by Rietveld refinement (Fig. 2.). The refined structural parameters are summarized in Table 1. It was assumed that Ga and Ge atoms in EuGa_2Ge_4 are randomly distributed in the network. In BaSi_6 these sites are substituted by Si atoms. Geometry optimization of the structural parameters determined by the Rietveld refinements were performed using the *ab initio* program CASTEP [12], including the lattice constants and the coordinates. The results are compared in Table 1, together with the experimental data. Note the very good agreement between ex-

Table 1. Crystallographic data of BaSi₆ in comparison with the structural data optimized by CASTEP.

Lattice parameters, Å	Atomic Coordinates and Isotropic Temperature Factors				
	Atom	Site	x	y	z
Rietveld refinement					
S. G.: <i>Cmcm</i> (No. 63)	Ba	4c	0	0.273(4)	1/4
<i>a</i> = 4.485(1)	Si1	8f	0	0.250(1)	0.537(1)
<i>b</i> = 10.375(2)	Si2	8f	0	0.559(1)	0.351(1)
<i>c</i> = 11.969(3)	Si3	8f	0	0.024(1)	0.599(1)
Reliability factors (%): <i>Rwp</i> = 5.33, <i>Re</i> = 1.95, <i>Rp</i> = 4.09; goodness-of-fit <i>S</i> (<i>Rwp/Re</i>) = 2.73					
^a <i>Rwp</i> , <i>R</i> -weighted pattern; <i>Re</i> , <i>R</i> -expected; <i>Rp</i> , <i>R</i> -pattern.					
CASTEP geometry optimization					
S. G.: <i>Cmcm</i> (No. 63)	Ba	4c	0	0.2787	1/4
<i>a</i> = 4.3999	Si1	8f	0	0.2447	0.5384
<i>b</i> = 10.3113	Si2	8f	0	0.5626	0.3518
<i>c</i> = 11.8842	Si3	8f	0	0.0201	0.5977

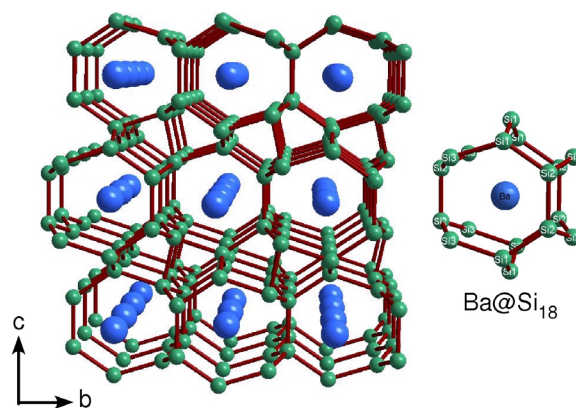
Fig. 2. Observed (open circle) and final calculated (line) profile plots, thick marks for Bragg peak positions, and difference profile plot from the Rietveld refinements of BaSi₆.

perimental data and the computationally determined parameters.

A schematic structural model of BaSi₆ is shown in Fig. 3, and selected bond lengths and angles are listed in Table 2. Each Ba atom is surrounded by 18 Si atoms forming an irregularly shaped polyhedral cage @Si₁₈ as shown in Fig. 4a. The bond distances between the central Ba atom and the surrounding Si atoms are in a range of 3.2–3.58 Å, the average distance being 3.435 Å. In the type I clathrate Ba₈Si₄₆, the average bond distance Ba-Si in the Ba@Si₂₀ cage is 3.365 Å, and that of the Ba@Si₂₄ cage is 3.712 Å (Fig. 4b) [13]. The Ba@Si₁₈ cage of BaSi₆ is as small as the Ba@Si₂₀ cage of the Ba₈Si₄₆ clathrate. The Ba@Si₁₈ polyhedra are linked by sharing the faces so as to form tunnels along the *a* axis. All the Si atoms

Table 2. Selected bond lengths (Å) and angles (deg) in BaSi₆.

Ba-Si1	×2	3.444(12)	Si1-Si2	2.411(6)
Ba-Si1	×4	3.404(9)	Si1-Si2	2.393(15)
Ba-Si2	×2	3.202(11)	Si1-Si3	2.454(11)
Ba-Si2	×4	3.381(8)	Si2-Si2	2.418(16)
Ba-Si3	×2	3.579(7)	Si2-Si3	2.477(5)
Ba-Si3	×4	3.564(6)	Si3-Si3	2.424(16)
Ba-Si _{ave}		3.435		
Si1-Si1-Si1		136.9(5)	Si1-Si3-Si2	×2 113.9(4)
Si1-Si1-Si2	×2	101.9(4)	Si1-Si3-Si3	84.5(3)
Si1-Si1-Si3	×2	96.4(4)	Si2-Si3-Si2	129.7(4)
Si2-Si1-Si3		128.3(4)	Si2-Si3-Si3	×2 99.3(3)
Si1-Si2-Si2		124.1(5)		
Si1-Si2-Si3	×2	98.9(4)		
Si2-Si2-Si3	×2	103.9(4)		
Si3-Si2-Si3		129.7(4)		

Fig. 3. Schematic illustration of the structure of BaSi₆. The Ba@Si₁₈ polyhedra are linked by sharing faces to form tunnels running along the *a* axis.

are bonded to four different Si atoms in three different types of distorted tetrahedra (Table 2), forming a clathrate-like network containing Ba@Si₁₈ polyhedral cages. BaSi₆ is isopointal with the clathrate structure of EuGa₂Ge₄.

The band structure was calculated with the program CASTEP, and the density of states (DOS) obtained is shown in Fig. 5. The non-zero DOS near the Fermi level shows that BaSi₆ is metallic. The electrical resistivity of BaSi₆ was measured by a conventional 4-probe method, and the result is shown in Fig. 6. The temperature dependence of the resistivity is almost flat over the temperature range from 300 to 2 K, although the resistivity of the order of ~0.1 Ωcm is not as small as that of metallic compounds. The relatively high electrical resistivity can be attributed to the many micro-cracks in the samples, which were observed under the scanning electron microscope for the EPMA measurement (Fig. 7).

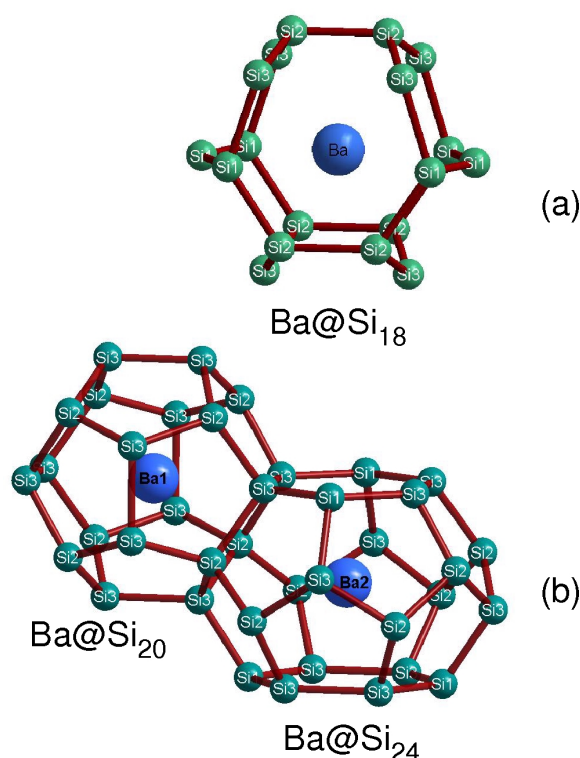


Fig. 4. Comparison of the polyhedra found in the clathrate structures, (a) Ba@Si_{18} in BaSi_6 and (b) Ba(1)@Si_{20} and Ba(2)@Si_{24} in $\text{Ba}_8\text{Si}_{46}$. The average Ba-Si distances (d) are $d_{\text{Ba-Si}} = 3.435$, $d_{\text{Ba1-Si}} = 3.365$, and $d_{\text{Ba2-Si}} = 3.712$ Å.

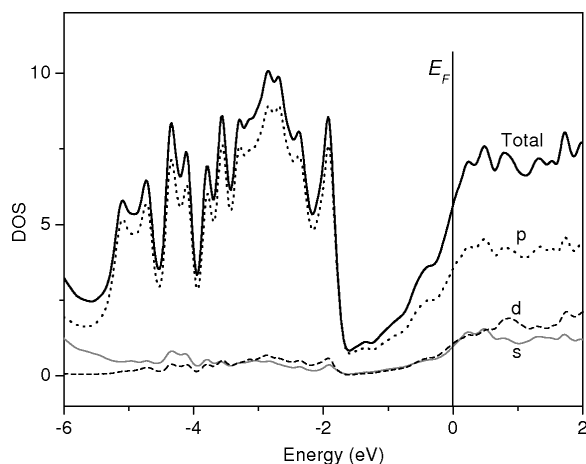


Fig. 5. Density of states (DOS) of BaSi_6 ; total DOS (solid line), and partial DOS for s (gray line), p (dotted line), and d (dashed line) orbitals.

It is obvious that the structures of the Ba-Si binary compounds are susceptible to compression at elevated

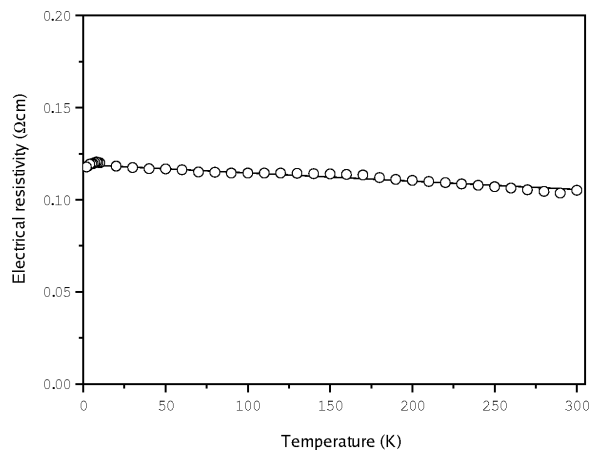


Fig. 6. Electrical conductivity of BaSi_6 as a function of temperature.

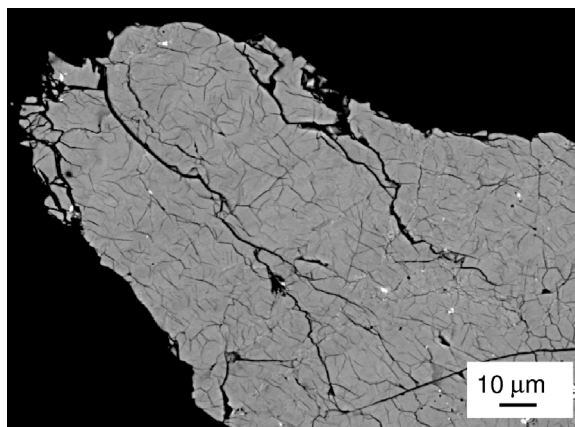


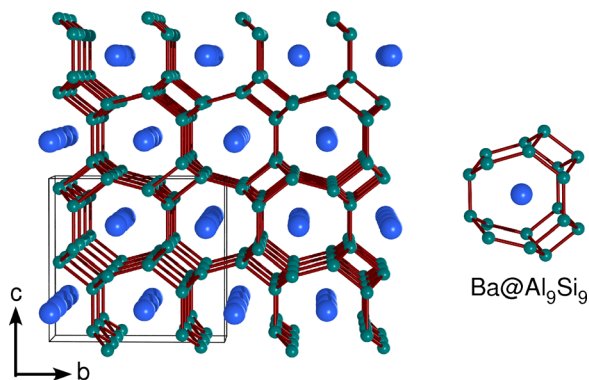
Fig. 7. Scanning electron micrograph of BaSi_6 showing a number of micro-cracks.

temperatures as shown in Fig. 1. Table 3 compares the volume changes between the reactant mixtures of BaSi_2 and Si and the products of different Si/Ba ratios. Note that there are large volume decreases in the formation of the Si-rich compounds; high-pressure and high-temperature synthesis is favorable for these compounds. It is also interesting to note that our recent study showed that the $\text{Ba}_8\text{Si}_{46}$ clathrate compound has a slight deficiency at the Ba sites, and the composition was determined to be $\text{Ba}_{7.76}\text{Si}_{46}$ with a Si/Ba ratio of 5.93 [14], very close to the ratio in BaSi_6 . The $\text{Ba}_8\text{Si}_{46}$ clathrate with the Ba deficiency can be transformed into BaSi_6 without a compositional change.

A similar trend was also observed for Ge-rich compounds in the La-Ge and Sr-Ge systems under high-pressure and high-temperature conditions; new Ge-rich

Reactant mixture	Reaction conditions	Total volume (cm ³ /mol)	Clathrate product	Clathrate volume (cm ³ /mol)	Volume difference (%)
24 BaSi ₂ + 52 Si	1.5 GPa, 800 °C	1884.7	Ba ₂₄ Si ₁₀₀	1676.8	−9
8 BaSi ₂ + 30 Si	3.0 GPa, 800 °C	778.2	Ba ₈ Si ₄₆	663.6	−15
BaSi ₂ + 4 Si	15 GPa, 1000 °C	100.2	BaSi ₆	83.9	−16

Table 3. Comparison of molecular volumes between reactants and products.

Fig. 8. Schematic illustration of the structure of the α -BaAl₂Si₂ and a Ba@(Al₉Si₉) polyhedral unit.

phases LaGe₅ [15] and SrGe_{6- δ} ($\delta \cong 0.5$) [16] were respectively obtained under high-pressure and high-temperature conditions of 5 GPa and 1200 °C. In the La-Ge system, La₃Ge, La₅Ge₃, La₄Ge₃, La₅Ge₄, LaGe, and LaGe₂ were prepared at ambient pressure. In the Sr-Ge system, Sr₂Ge, Sr₅Ge₃, SrGe, Sr_{0.76}Ge, SrGe₂ (trigonal), and SrGe₂ (orthorhombic) have been reported as yet. The new Ge-rich SrGe_{6- δ} phase is isotypic with BaSi₆. The DOS profile was calculated for SrGe_{6- δ} using the non-deficient germanide SrGe₆ [16], which is very similar to that shown for BaSi₆ in Fig. 5.

EuGa₂Ge₄, isotypic with BaSi₆, is a charge-balanced Zintl phase with a formal charge of Eu²⁺Ga⁻¹₂Ge⁰₄, and Ga⁻¹ and Ge⁰ can complete the clathrate covalent network with the octet configuration. It has been reported that EuGa₂Ge₄ is often associated with another charge-balanced Zintl phase, Type I clathrate Eu₈Ga₁₆Ge₃₀ [11]. If the Ga and Ge sites are denoted by *E*, the two charge-balanced Zintl phases have very close compositions, EuE₆ (*E*/Eu = 6) and Eu₈E₄₆ (*E*/Eu = 5.75), respectively, and the formation conditions should be very similar. These two compounds were prepared from a mixture of the elements by direct heating at ambient pressure [11].

Fig. 8 shows the crystal structure of α -BaAl₂Si₂ which is isostructural with BaAl₂Ge₂ [17]. Note that the structure is composed of Ba@(Al,Si)₁₈ polyhedral cages very similar to Ba@Si₁₈ of BaSi₆. Similar tun-

nels with Ba atoms are running along the *a*-axis formed by the sharing of faces of the polyhedra. α -BaAl₂Si₂ is a low-pressure polymorph, which is transformed into the high-pressure polymorph β -BaAl₂Si₂ having the ThCr₂Si₂ structure [17]. α -BaAl₂Si₂ is also a charge-balanced Zintl phase, and was prepared by simple direct heating of a mixture of the elements at ambient pressure.

More than 100 types of group IV clathrate compounds have been synthesized [18]. Most of them are charge-balanced Zintl compounds such as Eu₈Ga₁₆Ge₃₀ and SrGa₁₆Ge₃₀, and can be prepared from the mixtures of the elements by direct heating. A few exceptions are Ba₈Si₄₆, Na₈Si₄₆, and (Na,Ba)₈Si₄₆, where the clathrate covalent networks can be completed without using electrons from the guest metal atoms in the cages. The excess electrons from the guest metal atoms in the cages are accommodated in the antibonding orbital bands of the network. This type of compounds can be classified as “intercalation-type clathrate compounds” [19]. The intercalation-type clathrate compounds should be metallic, while the nature of the Zintl-type clathrate compounds is semiconducting. Most of the intercalation-type clathrate compounds cannot be prepared by direct heating under ambient pressure. Na₈Si₄₆ [20] and (Na,Ba)₈Si₄₆ [21] were prepared by removing Na atoms *via* thermal decomposition of the Zintl compounds NaSi and BaNa₂Si₄, respectively. The binary intercalation-type clathrate compounds Ba₂₄Si₁₀₀, Ba₈Si₄₆, and BaSi₆ can be prepared only by using high-pressure and high-temperature conditions.

After the submission of this manuscript, another isotypic compound EuSi₆ and its ternary derivatives EuSi_{6-*x*}Ga_{*x*} ($0 \leq x \leq 0.6$) have just been reported by Wosylus *et al.* [25]. These compounds were also prepared by applying a pressure of 8 GPa and a temperature of 1250 °C. There are a number of interesting similarities between the Eu and Ba analogues with regard to the structures and electrical properties. It has also been pointed out that the compounds with an excess of electrons can only be prepared by application of high pressure.

Conclusions

High-pressure and high-temperature synthesis favors the formation of Si-rich Ba-Si binary phases. The higher the pressure, the more Si-rich are the compounds formed. The new Si-rich compound BaSi_6 was prepared under a pressure of 15 GPa at 1000 °C. The structure was determined by Rietveld refinement, and the structural parameters were successfully reproduced by the geometry optimization using the *ab initio* program CASTEP. Similar trends were also found in Sr-Ge and La-Ge binary systems. BaSi_6 is a new type of clathrate compound, which can be classified into the intercalation type. Superconductivity could be anticipated as found in the other Si clathrates $\text{Ba}_8\text{Si}_{46}$ and $\text{Ba}_{24}\text{Si}_{100}$, which become superconductors at $T_c = 8.0$ and 1.4 K, respectively.

Experimental

High-pressure and high-temperature experiments

BaSi_2 was prepared by an arc-melting method described elsewhere [6]. $\text{Ba}_8\text{Si}_{46}$ was prepared from a stoichiometric mixture of BaSi_2 and Si powders by high-pressure treatment at 3 GPa and 800 °C using a cubic multianvil-type press [6]. High-pressure and high-temperature experiments were carried out using Kawai-type multianvils [22]. The samples were filled in a cylindrical *h*-BN cell with an inner diameter of 1.5 mm, which was surrounded by a thin Ta-tube heater. The heater was placed in a ZrO_2 tube, and the whole sample assembly was centred in a pierced CoO doped MgO octahedron with an edge length of 10 mm. The octahedron was placed in the center of eight truncated tungsten carbide cubes as anvils (truncation edge length: 4 mm) separated by pyrophyllite gaskets, and compressed in a multianvil apparatus up to 15 GPa, followed by heating to temperatures up to 1000 °C in 5 min. After keeping the sample at the temperature for one hour, it was cooled down to r. t.

rapidly. Then the pressure was gradually released over the matrix.

Characterization

Powder X-ray diffraction patterns were measured on a diffractometer having a curved imaging plate (IP) detector (Rigaku-RAXIS) using graphite-monochromated $\text{MoK}\alpha$ radiation ($\lambda = 0.71073$ Å). The radius of the IP was 127.4 mm, and the resolution was 0.044 deg/pixel. The powder sample was filled in a glass capillary with a diameter of 0.3 mm and rotated over 180 degrees on the ω axis. The intensity of the diffraction pattern measured by IP was traced along the horizontal line, and converted into the intensity vs diffraction angles (2θ) profile using the program package RAPID. The structure of BaSi_6 was analyzed on the profile data over the range from 5 to 45 deg using the software package TOPAS-Academic for the Rietveld analysis [23]. The composition was determined by an electron probe microanalyzer (JEOL JCMS-733II).

The geometry optimizations, the density of states, and band structure calculations were performed within the density functional theory (DFT) framework, using the program CASTEP [12, 24]. The calculations were performed using the GGA-PBE (generalized gradient approximation-Perdew-Burke-Ernzerhof) functional. Ultrasoft *pseudo* potentials were used within a plane wave basis with cutoff energy of 230 eV. A $6 \times 4 \times 4$ Monkhorst-Pack mesh was used for k-point sampling within the Brillouin zone. The structural parameters optimized included cell parameters and internal coordinates of atoms.

Acknowledgements

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