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# A Crossover from High Stiffness to High Hardness: The Case of Osmium and Its Borides

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**Abstract:** Transition-metal light-element compounds are currently raising great expectations for hard and superhard materials. Using the widely attracting osmium (Os) and its borides ( $\text{OsB}$ ,  $\text{Os}_2\text{B}_3$  and  $\text{OsB}_2$ ) as prototypes, we demonstrate by first-principles calculations that heavy transition metals, which possess high stiffness but low hardness, can be converted into highly hard materials by incorporating of light elements to form compounds. Such a crossover is a manifestation that the underlying sources of high stiffness and high hardness are fundamentally different. The stiffness is related to elastic deformation that is closely associated with valence electron density, whereas the hardness depends strongly on plastic deformation that is determined by bonding nature. Therefore, the incorporation of light atoms into transition metal should be a valid pathway of designing hard and superhard materials. This strategy is in principle also applicable to other transition-metal borides, carbides, and nitrides.

**Keywords:** First-Principles Calculations; Mechanical Properties; Transition Metal Borides.

## 1 Introduction

Hard and superhard materials are technologically important in many applications from reducing the wear of everyday objects to creating machining tools [1, 2]. Experimentally, the hardness of a material is defined by pressing a diamond indenter into the surface of the material and measuring the size of the impression. It is obvious that the hardness definition is a macroscopic concept, which

leads to the difficulty in calculating the hardness value microscopically; thus, theoretical scientists need to look for an additional replacement of hardness. A frequently used candidate for this is the bulk modulus, which reflects the volume stiffness of the material [3]. It is often true that a highly hard material must possess a high bulk modulus. For example, diamond is the hardest existing material with the highest known bulk modulus. However, it is a bit confusing whether a material with a high bulk modulus has a high hardness. In fact, bulk modulus has little direct connection with hardness. For example, the bulk modulus of WC is as high as 439 GPa but its hardness is below 30 GPa [4]. Nevertheless,  $\text{B}_6\text{O}$  possesses a higher hardness between 32 and 60 GPa even though its relatively lower bulk modulus of 230 GPa [5]. Therefore, it is highly desirable to hunt for a type of prototype materials to exemplify the exact difference of high stiffness and high hardness and, in particular, to provide the essential guidance in the design of hard and superhard materials.

In the last years, transition-metal Os has attracted much attention. Its bulk modulus was first measured to be 462 GPa by Cynn et al. [6] and later reported to be 411 GPa by Occelli et al. [7] and 395 GPa by Kenichi [8] using different experimental methods. These values are considered to be extremely high, exceeding that of cubic boron nitride (392 GPa) and even rivaling with that of diamond (446 GPa) [9]. Based on high bulk modulus, it has been proposed that incorporating light atoms (e.g. boron, carbon, and nitrogen) into heavy transition metals (e.g. Os, Re, and W) might be a possible strategy to design hard and superhard materials [10–12]. Theoretically, a series of transition-metal borides have been predicted for promising hard and superhard [13–17]. Implicit in such efforts is an assumption that the metal atoms (creating high valence-electron density) prevent the structures from being squeezed together, while the light atoms (forming strong covalent bond) withstands both elastic and plastic deformations, both of which enhance the hardness of materials. By applying this principle, the first prototype material  $\text{OsB}_2$  was synthesised and was characterised to be an ultra-incompressible, hard material [11]. Subsequently,  $\text{OsB}$  and  $\text{Os}_2\text{B}_3$  have also been synthesised experimentally [18]. So far, there are a few theoretical works reporting their mechanical properties and electronic structures [19–23],

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but these calculated results are quite scattered due to the inconsistency in different techniques. In particular, the changing trends of stiffness and hardness have not fully addressed.

In this article, we systematically investigate the equation of state (EOS), elastic properties, and hardness of Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> using the first-principles calculations. The transition-metal Os has high stiffness but low hardness. While the incorporation of boron into the lattice structure of Os forms OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>, their bulk moduli decrease steadily but their hardness values enhance rapidly. We reveal that the crossover from high stiffness to high hardness is a result of their completely different underlying origins, which may provide a new strategy of designing hard and superhard materials.

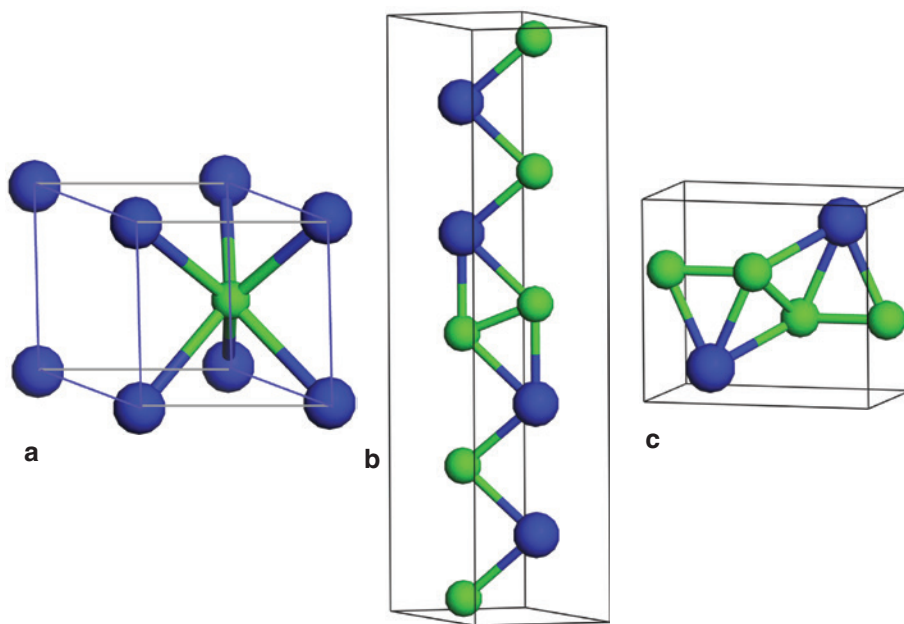
## 2 Structures and Methods

Experimentally, Os adopts the hexagonal close-packed (hcp) lattice (space group  $P6_3/mmc$ ) [6–8]. OsB (space group  $P-6m2$ ) and Os<sub>2</sub>B<sub>3</sub> (space group  $P6_3/mmc$ ) form in the hexagonal lattice with few freedoms of atomic positions as shown in Figure 1a and b, respectively. OsB has only one formula unit per unit cell with one Os atoms on the  $1a$  (0, 0, 0) Wyckoff site and one B atom on the  $1d$  ( $1/3$ ,  $2/3$ ,  $1/2$ ) position [18]. For Os<sub>2</sub>B<sub>3</sub>, there are two formula units per unit cell, in which four Os atoms occupy the  $4f$

( $2/3$ ,  $1/3$ , 0.6398) sites and six B atoms hold the  $2d$  ( $2/3$ ,  $1/3$ ,  $3/4$ ) and  $4f$  ( $2/3$ ,  $1/3$ , 0.4727) positions [18]. As shown in Figure 1c, OsB<sub>2</sub> crystallises the related body-centered orthorhombic structure with the space group of  $Pmmn$ . In each unit cell, two Os atoms are situated in the  $2a$  ( $2/3$ ,  $1/3$ ,  $3/4$ ) sites, whereas four B atoms occupy the  $4f$  ( $2/3$ ,  $1/3$ , 0.455) positions [11, 18].

First-principles calculations based on density functional theory (DFT) have been performed for Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> using the all-electron projector augmented wave (PAW) method within the generalised gradient approximation (GGA) of Perdew, Burke, and Ernzerhof (PBE) [24], as implemented in VASP code [25]. A very careful check for the convergence of calculated results with respect to the kinetic cutoff energy and the number of  $k$ -points has been conducted. We finally adopt a plane-wave basis set with a large cutoff energy of 500 eV and the  $k$ -mesh with a dense grid of  $0.025 \text{ \AA}^{-1}$  for all the considered systems to ensure the numerical accuracy.

We carry out total-energy calculations over a wide range of volumes for the considered materials. The structure optimisations are performed for each constant volume and each material. The equilibrium volume, bulk modulus, and its first pressure derivative are estimated through a least-square fit of calculated volume-energy sets to the third-order Birch–Murnaghan EOS [26]. The elastic constants are obtained by the efficient strain energy method with the maximum strain of 0.04, and the details

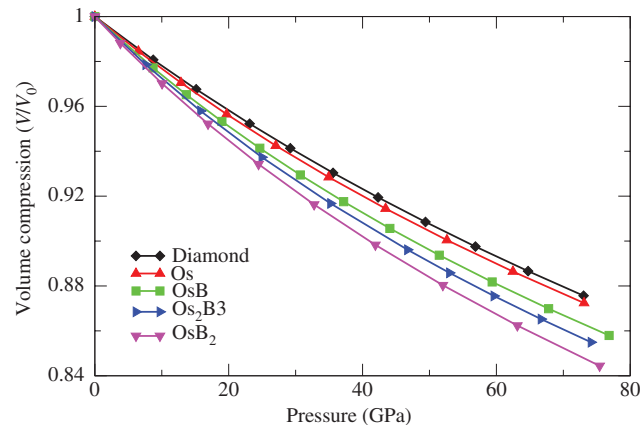


**Figure 1:** Crystal structures of the (a) hexagonal OsB, (b) hexagonal Os<sub>2</sub>B<sub>3</sub>, and (c) orthorhombic OsB<sub>2</sub>. The blue (large) and green (small) spheres represent Os and B atoms, respectively.

are described in our previous work [22]. This method has been demonstrated to be very good in providing accurate and reliable predictions of mechanical properties of various systems [27–29]. According to the Voight–Reuss–Hill bounds [30], their shear moduli, Young’s moduli, and Poisson’s ratio are also determined. For diamond, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>, the Vickers’ hardness values are estimated by Chen’s model [31].

### 3 Results and Discussion

Table 1 lists the space group, calculated equilibrium lattice constants, equilibrium volume, bulk modulus, its pressure derivative at zero pressure with available data for Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>. For comparison, diamond has also been studied in this work. From this table, we can see that these calculated results are in relatively good agreement with the experimental data within the GGA errors, and this confirms the validity of our calculations. As expected, diamond has the highest known bulk modulus (433 GPa) among the five materials. For the transition-metal Os, its bulk modulus is predicted to be 404 GPa, which agrees well with the experimental measurements [6–8]. This value is slightly smaller than that of diamond, and thus, Os is an ultrastiff material. While boron atoms insert into Os to form its borides, the bulk modulus steadily decreases from 357 GPa for OsB to 334 GPa for Os<sub>2</sub>B<sub>3</sub> and then to 311 GPa for OsB<sub>2</sub>. To further compare the volume stiffness of diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> under pressure, the volume compressions as a function of pressure are plotted in Figure 2. We can explicitly see that the order of volume stiffness from high to low is diamond > Os > OsB > Os<sub>2</sub>B<sub>3</sub> > OsB<sub>2</sub>, although they all have very high volume stiffness.



**Figure 2:** Calculated volume compression ( $V/V_0$ ) under pressure for diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>.

The accurate calculation of elasticity is essential for understanding the macroscopic mechanical properties of solids, for establishing the constitutive equations and for the design of hard materials. Our obtained elastic constants, shear moduli, Young’s moduli, and Poisson’s ratios for diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> are presented in Table 2. For the cubic, hexagonal, and orthorhombic lattices, there are three ( $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ ), five ( $C_{11}$ ,  $C_{12}$ ,  $C_{13}$ ,  $C_{33}$ , and  $C_{44}$ ), and nine independent elastic constants ( $C_{11}$ ,  $C_{12}$ ,  $C_{13}$ ,  $C_{22}$ ,  $C_{23}$ ,  $C_{33}$ ,  $C_{44}$ ,  $C_{55}$ , and  $C_{66}$ ), respectively. First, the mechanical stability of any crystal complies with the mandatory requirement of the strain energy to be positive. We have carefully checked these calculated elastic constants  $C_{ij}$  and the results show that the five materials are mechanically stable at zero pressure. Then, the elastic constants  $C_{11}$ ,  $C_{22}$ , or  $C_{33}$  measure the  $a$ -,  $b$ -, or  $c$ -direction resistance to linear compression, respectively. All three directions of diamond are isotropic and possess the highest linear

**Table 1:** Space group, equilibrium lattice constants  $a_0$ ,  $b_0$ ,  $c_0$  (Å), equilibrium volume  $V_0$  (Å<sup>3</sup>), bulk modulus  $B_0$  (GPa), and its pressure derivative  $B'_0$  at zero pressure compared with available data for diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>.

Materials	Space group	$a_0$	$b_0$	$c_0$	$V_0$	$B_0$	$B'_0$	
Diamond	<i>Fd-3m</i>	3.575	3.575	3.575	45.68	433	3.62	This study
		3.567	3.567	3.567	45.38	446	3.0	Expt. [9]
Os	<i>P6<sub>3</sub>/mmc</i>	2.755	2.755	4.344	28.54	404	4.92	This study
		2.733	2.733	4.318	27.941	395–462	2.4–4.5	Expt. [6–8]
OsB	<i>P-6m2</i>	2.899	2.899	2.882	20.98	357	4.42	This study
		2.876	2.876	2.873	20.58	431	5.8	Expt. [18]
Os <sub>2</sub> B <sub>3</sub>	<i>P6<sub>3</sub>/mmc</i>	2.943	2.943	12.943	97.08	334	4.41	This study
		2.909	2.909	12.945	94.88	396	7.1	Expt. [18]
OsB <sub>2</sub>	<i>Pmmn</i>	4.705	2.890	4.093	55.66	311	4.24	This study
		4.684	2.871	4.075	54.80	343	4.4	Expt. [18, 19]

**Table 2:** Calculated elastic constants  $C_{ij}$  (GPa), shear modulus  $G$  (GPa), Young's modulus  $E$  (GPa), Poisson's ratio  $\nu$ , and hardness  $H$  (GPa) for diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>.

Material	$C_{11}$	$C_{22}$	$C_{33}$	$C_{12}$	$C_{13}$	$C_{23}$	$C_{44}$	$C_{55}$	$C_{66}$	$G$	$E$	$\nu$	$H$	$H$ (Exp.)
Diamond	1049	1049	1049	127	127	127	573	573	573	525	1123	0.069	94.8	93.5 <sup>a</sup>
Os	747	747	832	227	231	231	254	254	260	262	649	0.237	—	4 <sup>b</sup>
OsB	635	635	809	201	200	200	193	193	217	217	543	0.250	20.0	14.4 <sup>b</sup>
Os <sub>2</sub> B <sub>3</sub>	556	556	910	202	193	193	215	215	177	212	530	0.247	24.0	21.8 <sup>b</sup>
OsB <sub>2</sub>	588	578	846	184	222	121	163	286	215	225	552	0.226	29.6	23.5 <sup>b</sup>

The theoretical hardness of Os is not estimated due to the failure of the hardness model to pure metallic compounds.

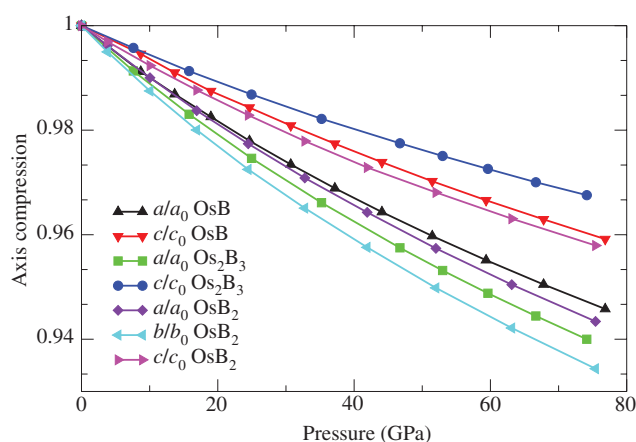
<sup>a</sup>Reference [21].

<sup>b</sup>Reference [18].

stiffness (1049 GPa). The linear stiffness of Os is inferior to that of diamond but is superior to that of OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>. Moreover, we interestingly find that there is substantial anisotropy in the mechanical behavior of OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>. It is observed that  $C_{11}$  for OsB (635 GPa), Os<sub>2</sub>B<sub>3</sub> (556 GPa), and OsB<sub>2</sub> (588 GPa) are smaller by 39 %, 47 %, and 44 %, respectively, compared with that of diamond (1049 GPa). However,  $C_{33}$  for OsB (809 GPa), Os<sub>2</sub>B<sub>3</sub> (910 GPa), and OsB<sub>2</sub> (846 GPa) are comparable to that of diamond. In addition, Young's moduli for OsB (543 GPa), Os<sub>2</sub>B<sub>3</sub> (530 GPa), and OsB<sub>2</sub> (552 GPa) are only half of that of diamond (1123 GPa). It is obvious that the off-diagonal elastic constants and Poisson's ratios for OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> are much larger than the corresponding values of diamond. We have further calculated the axial ratios  $c/a$  or  $c/b$  as function of pressure. As seen from Figure 3, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> exhibit substantial anisotropy under high pressure. Therefore, the present results show that the linear stiffness of Os is superior to that of OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>, although OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> also have high linear stiffness and anisotropy.

Shear stiffness measures the resistance to shape change under the applied loads. The shear moduli of Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> are calculated to be 262, 217, 212, and 225 GPa, respectively. Clearly, the shear stiffness of Os is superior to that of its borides (OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>) but only approaches 50 % of that of diamond (525 GPa). The elastic constants  $C_{44}$ ,  $C_{55}$ , and  $C_{66}$  are also an important parameter to describe the shear property of a material. For OsB, its  $C_{44}$  (193 GPa) is smaller than  $C_{66}$  (217 GPa); for Os<sub>2</sub>B<sub>3</sub>,  $C_{44}$  (215 GPa) is larger than  $C_{55}$  (177 GPa). For orthorhombic OsB<sub>2</sub>, the elastic constants  $C_{44}$ ,  $C_{55}$ , and  $C_{66}$  are calculated to be 163, 286, and 215 GPa, respectively. Therefore, these results indicate that the shear stiffness of OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub> not only is inferior to that of Os but also exhibit substantial anisotropy.

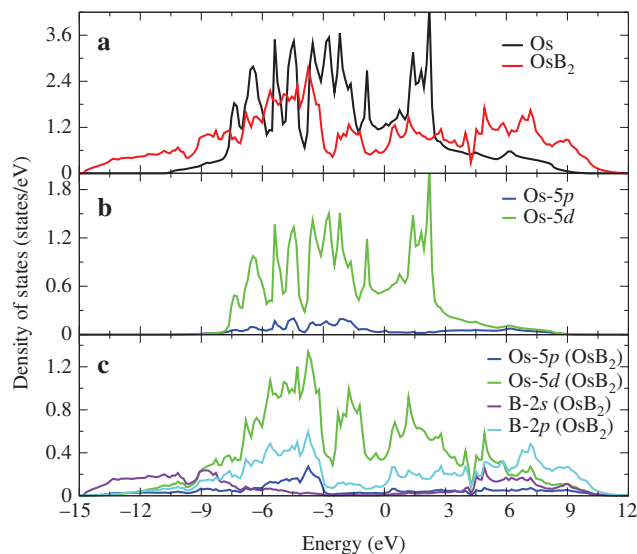
The hardness values are presented in Table 2 for diamond, Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>. Except for Os, the estimated hardness values agree with the measured results. Below the experimental data are adopted to discuss their trend. We notice that the changing trend of hardness is completely different from that of stiffness. Although the bulk modulus of Os rivals with that of diamond, the hardness of Os (4 GPa) is by far smaller than that of diamond (93.5 GPa), implying that ultrastiff Os is not a hard material at all. Hence, high stiffness does not guarantee high hardness. Nevertheless, can a highly stiff material transform into a highly hard one? In diamond, the four  $sp^3$  hybrids of carbon form a three-dimensional network composed of strong covalent bonds, which is responsible for its hardness. At the same time, its high valence electron density results in its exceptionally high bulk modulus. The high stiffness of Os can be explained from its high valence electron density, and its low hardness is attributed to the weak metallic bonds that allow plastic deformation. In order to enhance the hardness of a material, the nondirectional metallic bonds must be changed to directional covalent bonds by inserting light atoms into transition metals. With the addition of boron atoms, the values of hardness

**Figure 3:** Calculated axis compression ( $a/a_0$ ,  $b/b_0$ , and  $c/c_0$ ) under pressure for OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>.



enhance from 14.4 GPa for OsB to 21.8 GPa for  $\text{Os}_2\text{B}_3$  and then to 23.5 GPa for  $\text{OsB}_2$ . These results demonstrate that the transition-metal Os, which has high stiffness but low hardness, is converted into hard materials by incorporating of boron atoms to form borides. Such a crossover is a manifestation that the underlying sources of high stiffness and high hardness are fundamentally different. Moreover, the opposite trends of stiffness and hardness for Os and its borides provide an illustrative case explicitly to differentiate their natures.

Upon incorporating boron atoms into the interstitial sites of the Os lattice to form OsB, the crystal volume largely expands. This volume expansion results in the drop in valence electron density and thus gives rise to a negative contribution to the bulk modulus. As shown in Figure 1a, the structure of OsB can be described as stacking of Os- and B-layers along the  $c$ -direction and the covalent bonds of Os-B are formed, which achieves the sharp hardness enhancement from Os to OsB. With the increasing in boron content, the valence electron density continues to fall slowly, and thus, the bulk modulus slightly decreases from OsB to  $\text{Os}_2\text{B}_3$ , then to  $\text{OsB}_2$ . However, for  $\text{Os}_2\text{B}_3$ , the boron atoms of puckered layers are tetrahedrally surrounded by four Os atoms and three additional boron neighbors. The boron atoms of planar layers have a trigonal prismatic environment of six Os atoms and no adjacent boron atoms (see Fig. 1b). The higher degree of covalent bonding makes the hardness of  $\text{Os}_2\text{B}_3$  increase. In  $\text{OsB}_2$ , there exist well-defined zigzag covalent chains along the  $c$ -direction, interconnected by shared B and Os atoms. This feature of covalent bond network plays a key role in enhancing its hardness, but the presence of soft metallic Os–Os layers limits its enhanced hardness at a large load [21]; thus,  $\text{OsB}_2$  is a hard but not superhard material. In order to understand the underlying origin of hardness enhancement, we use Os and  $\text{OsB}_2$  as an illustrative case to compare their electronic structures. Our calculated density of states (DOS) for Os and  $\text{OsB}_2$  are plotted in Figure 4. As can be seen, the electronic structure of Os is predominated by  $5d$  states while that of  $\text{OsB}_2$  is governed by a strong hybridisation between the Os- $5d$  and B- $2p$  states. It is the crossover from partially metallic bonds to covalent bonds that has an important contribution to the hardness enhancement from Os to its borides. Ideally, a boron-rich compound would be a preferred harder material, as a higher concentration of boron may easily lead to a three-dimensional B–B bonding and thus a higher hardness. Therefore, pursuing boron-rich borides has recently stimulated much interest and some transition-metal borides with high boron content, such as  $\text{WB}_3$ ,  $\text{FeB}_4$ , and  $\text{MnB}_4$  [32–34], have become the prime



**Figure 4:** Density of states (DOS). (a) total DOS of Os and  $\text{OsB}_2$ , (b) projected DOS of Os, and (c) projected DOS of  $\text{OsB}_2$ .

candidates to be superhard materials. Pursuing the thermodynamically stable transition-metal borides with ultimate boron content may be a reasonable strategy used for designing hard and superhard materials [35].

Finally, we briefly discuss the relation between mechanical properties and deformations. In order to split a crystal, electron-pair covalent bonds must first be broken and remade. Accordingly, hardness depends strongly on plastic deformation that is mainly determined by bonding nature. However, bulk modulus measures resistance to elastic compression of volume, which has little direct connection with hardness from dislocation theory. In elastic deformation, the basic relations between atoms do not change. Therefore, valence electron density mostly determines the bulk modulus of a material, but the bonding nature, optimal filling of bonding states, and crystal structure also partially contribute to the stiffness. In general, covalent materials show high bond-bending force constants, contain highly directional bonds, and thus possess high shear modulus. Although a good correlation has been observed between hardness and shear modulus, the dependence is not unequivocal and monotonic [36]. Thus, it is sometimes difficult to design hard and superhard materials only on the basis of high stiffness.

## 4 Conclusion

In summary, we have used the first-principles calculations to systematically investigate the trends of stiffness and

hardness of Os, OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>. The results indicate that Os possesses high stiffness but low hardness. Upon incorporating of boron atoms into Os to form OsB, Os<sub>2</sub>B<sub>3</sub>, and OsB<sub>2</sub>, the hardness values of these borides enhance largely, although their stiffness decreases slightly. Such a crossover is a manifestation that the underlying sources of high stiffness and high hardness are fundamentally different. The stiffness is related to elastic deformation that is closely associated with valence electron density, whereas the hardness depends strongly on plastic deformation that is determined by bonding nature. Therefore, the incorporation of light atoms into transition metal should be a valid pathway of designing hard and superhard materials. This article not only clarifies the nature of some mechanical behaviors but also provides a useful strategy in the quest for intrinsically superhard transition-metal borides, carbides, and nitrides.

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