

## Conference paper

Vit Prokop\*, Lukas Strizik\*, Jiri Oswald, Milan Vlcek, Ludvik Benes,  
Spyros N. Yannopoulos, Bozena Frumarova and Tomas Wagner

# 1.5 $\mu\text{m}$ photoluminescence and upconversion photoluminescence in GeGaAsS:Er chalcogenide glass

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**Abstract:** The paper reports on  $\approx 1.5 \mu\text{m}$  Stokes photoluminescence (PL) emission and upconversion photoluminescence (UCPL) emission in the visible and near-infrared spectral region in  $\text{Er}^{3+}$ -doped  $\text{Ge}_{25}\text{Ga}_8\text{As}_2\text{S}_{65}$  chalcogenide glasses at pumping wavelengths of 980 and 1550 nm. The  $\approx 1.5 \mu\text{m}$  PL emission spectra are broadened with increasing concentration of Er ions which is discussed in terms of radiation trapping and UCPL dynamics affecting the  $\text{Er}^{3+}$ :  $^4I_{13/2}$  level lifetime. The UCPL emission was observed at  $\approx 530$ ,  $\approx 550$ ,  $\approx 660$ ,  $\approx 810$  and  $\approx 990$  nm and its overall intensity as well as red-to-green UCPL emission intensity ratio increases with increasing Er concentration. To explore the UCPL dynamics we measured double logarithmic dependency of green ( $\approx 550$  nm) and red ( $\approx 660$  nm) UCPL emission versus pump power at pumping wavelength of 975 nm. Moreover, we measured quadrature frequency resolved spectroscopy (QFRS) on green UCPL emission ( $\approx 550$  nm) using 975 nm pumping wavelength and various excitation powers. The QFRS spectra on green UCPL were analyzed in term of QFRS transfer function for three-level model from which we deduced energy transfer upconversion rate  $w_{11}$  ( $\text{s}^{-1}$ ) originating from  $\text{Er}^{3+}$ :  $^4I_{11/2}$ ,  $^4I_{11/2} \rightarrow ^4F_{7/2}$ ,  $^4I_{15/2}$  transitions.

**Keywords:** chalcogenide glasses; energy transfer upconversion; Er-doped glasses; excited state absorption; photoluminescence; quadrature frequency resolved spectroscopy; SSC-2018; upconversion dynamics; upconversion photoluminescence.

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**\*Corresponding authors: Vit Prokop and Lukas Strizik**, Department of General and Inorganic Chemistry, Faculty of Chemical Technology, University of Pardubice, Studentska 573, Pardubice 532 10, Czech Republic, Tel.: +420 466 037 000, E-mail: vit.prokop@student.upce.cz (V. Prokop); lukas.strizik@upce.cz (L. Strizik)

**Jiri Oswald:** Institute of Physics of the Czech Academy of Sciences v.v.i., Cukrovarnicka 10, 162 00, Prague 6, Czech Republic

**Milan Vlcek:** Institute of Macromolecular Chemistry of the AS CR, v.v.i., Heyrovskeho nam. 2, 162 00, Prague 6, Czech Republic

**Ludvik Benes:** Joint Laboratory of Solid State Chemistry, Faculty of Chemical Technology, University of Pardubice, Pardubice 532 10, Czech Republic

**Spyros N. Yannopoulos:** Foundation for Research and Technology-Hellas, Institute of Chemical Engineering Sciences (FORTH/ICE-HT), P.O. Box 1414, GR-26504 Patras, Greece

**Bozena Frumarova:** Center of Materials and Nanotechnology, Faculty of Chemical Technology, University of Pardubice, nam. Cs. legii 565, Pardubice 530 02, Czech Republic

**Tomas Wagner:** Department of General and Inorganic Chemistry, Faculty of Chemical Technology, University of Pardubice, Studentska 573, Pardubice 532 10, Czech Republic; and Center of Materials and Nanotechnology, Faculty of Chemical Technology, University of Pardubice, nam. Cs. legii 565, Pardubice 530 02, Czech Republic

## Introduction

Amorphous chalcogenides doped with rare-earth (RE) ions are promising materials in many applications due to their unique properties [1–3] such as low phonon energy, high refractive index, broad transparency from the visible to the mid-infrared spectral region with relatively good solubility of  $\text{RE}^{3+}$  ions in chalcogenide glasses (ChG) containing Ga [4], Al [5], In [6]. ChG can be relatively easily prepared as bulks or thin films and in variety of shapes [1].

Among the most studied and promising chalcogenide hosts for  $\text{RE}^{3+}$  doping to achieve the visible UCPL belong sulfides as Ge-Ga-S [7], Ge-Ga-Sb-S [8], Ge-Ga-As-S [9], and Ga-La-S [10]. Compared to Ge-Ga-S glasses, the glasses of the Ge-Ga-As-S system show improved glass-forming ability [9] and thermal stability [8, 11] with still good solubility of  $\text{RE}^{3+}$  ions [9]. The Ge-Ga-Sb-S glasses have higher thermal stability compared to Ge-Ga-As-S however, their transparency is markedly reduced in the visible spectral region [8, 12, 13]. Studied materials show potential for optical fibers [14], optical fiber amplifiers [15], non-linear optical waveguides [16], laser devices [17, 18] or chemical sensors and detectors [19, 20].

In this article we present photoluminescent and structural properties of  $\text{Er}^{3+}$ -doped  $\text{Ge}_{25}\text{Ga}_8\text{As}_2\text{S}_{65}$  (GGAS) chalcogenide glasses as promising candidates for UCPL from the green visible to the near-infrared spectral region. We measured emission spectra and lifetimes of  $\approx 1.5 \mu\text{m}$  PL Stokes emission and UCPL emission spectra at pumping wavelengths of 980 and 1550 nm. Moreover, the green UCPL emission ( $\approx 550 \text{ nm}$ ) at 975 nm pumping wavelength and various pump powers was investigated by QFRS to deduce the energy transfer upconversion rate parameter  $w_{11}$  for 0.01 and 0.5 % Er-doped GGAS glasses.

## Experimental

GGAS:  $x$  at%  $\text{Er}^{3+}$  chalcogenide glasses, where  $x = 0.01\text{--}1$  at%, were synthesized by the melt-quenching technique from high purity elements of Ge (5N), Ga (5N), As (5N), S (4N) and Er (3N). The synthesis was carried out in the rocking furnace at  $1050^\circ\text{C}$  for 24 h. Melt was quenched into water and ampoule with raw glass was subsequently annealed near the glass transition temperature ( $T_g - 20$ )  $^\circ\text{C}$  for 3 h to relax the mechanical strain. After that, the glass samples were slowly cooled down to room temperature, cut into  $\approx 1 \text{ mm}$  thick rectangles and both-side polished into the optical quality.

The amorphous state of  $\text{Er}^{3+}$ -doped GGAS glasses was studied by X-ray diffraction (XRD) analysis using diffractometer Bruker AXS D8 Advance with Cu  $K\alpha$  radiation in the range of  $2\theta$  from  $10^\circ$  to  $70^\circ$ . The chemical composition of prepared samples was determined by the energy dispersive X-ray (EDX) microanalyzer IXRF System with a detector GRESHAM Sirius 10 and at accelerating voltage of the primary electron beam  $\approx 20 \text{ kV}$ . The room temperature Raman spectra were measured by the Raman FRA-106 Bruker as a part of the FT-IR spectrophotometer IFS 55 using the excitation source of the YAG:  $\text{Nd}^{3+}$  laser ( $\lambda_{\text{exc}} \approx 1064 \text{ nm}$ ) in the  $50\text{--}200 \text{ cm}^{-1}$  spectral region. The Raman spectra were reduced by the method of Gammon and Shuker [21] and then decomposed by a sum of eight Gaussians using the Fityk program v. 0.9.8 [22].

The refractive index  $n_g$  of the glasses was analyzed by the variable angle spectroscopic ellipsometry VASE®, J.A. Woollam Co., Inc. in the spectral region of  $500\text{--}2300 \text{ nm}$  measured with a step of  $20 \text{ nm}$  and at angles of light incidence  $65^\circ$ ,  $70^\circ$  and  $75^\circ$ . Ellipsometric data were fitted to the Sellmeier model,  $n_g^2 = A + B\lambda^2/(\lambda^2 - C)$  [23]. The concentration of  $\text{Er}^{3+}$  ions  $\rho$  ( $\text{cm}^{-3}$ ) in glassy samples was calculated from density measurements and chemical composition. Transmittance  $T$  was measured by double-beam UV-Vis-NIR spectrophotometer JASCO V-570 in the spectral region of  $400\text{--}1800 \text{ nm}$  with step of  $1 \text{ nm}$ . The absorption cross-section  $\sigma_a$  spectrum was calculated by the equation  $\sigma_a = \ln 10 [-\log T + \log (1 - R)]/\rho d$ , where  $R$  is reflectance determined from refractive index as  $R = [(n_g + 1)/(n_g - 1)]^2$  and  $d$  is sample thickness in cm units. The absorption cross-section spectrum of 0.5 % Er-doped GGAS glass was used for application of Judd–Ofelt (JO) theory to calculate the intensities of  $\text{Er}^{3+}$  intra- $4f$  electronic transitions.  $\text{Er}^{3+}$   $\approx 1.5 \mu\text{m}$  PL emission spectra were acquired at pumping wavelength of  $980 \text{ nm}$ , the UCPL emission spectra in the spectral region of  $400\text{--}1050 \text{ nm}$  were acquired at  $980 \text{ nm}$  ( $\sim 9 \text{ W cm}^{-2}$ ) and  $1550 \text{ nm}$  ( $\sim 13 \text{ W cm}^{-2}$ ) excitation wavelengths using the diode lasers.

The  $\text{Er}^{3+}: {}^4I_{13/2}$  level lifetimes (at  $\lambda \approx 1535 \text{ nm}$ ) for Er-doped GGAS glasses excited by 980 nm were analyzed by time-resolved spectroscopy from  $1/e$  value or by using the Eq. 1:

$$N_1 = N_1(0)e^{-k_1 t} + N_2(0) \frac{\beta k_2}{k_1 - k_2} (e^{-k_2 t} - e^{-k_1 t}), \quad (1)$$

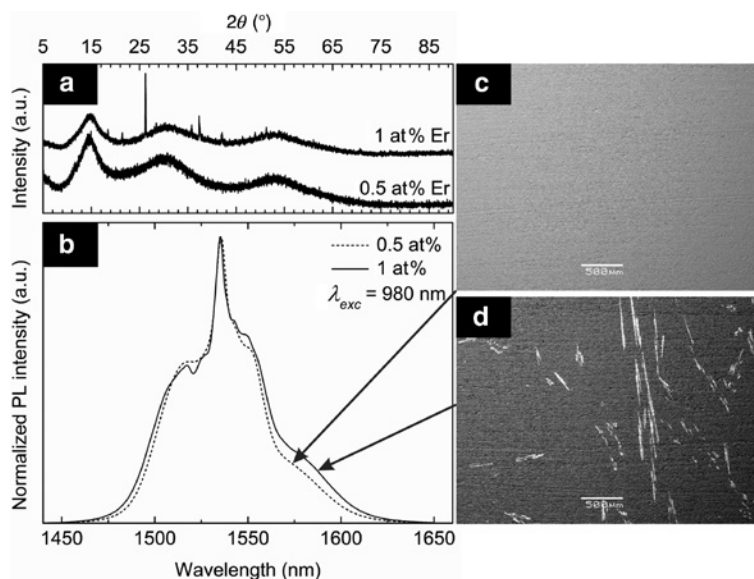
where  $N_i(0)$  is the initial population density,  $k_i$  is relaxation rate at level  ${}^4I_{13/2}$  ( $i=1$ ) and  ${}^4I_{11/2}$  ( $i=2$ ),  $\beta$  is branching ratio of the  ${}^4I_{11/2} \rightarrow {}^4I_{13/2}$  transitions and  $t$  is time. Equation 1 takes into account the delayed population of the  ${}^4I_{13/2}$  energy level from the pumped  ${}^4I_{11/2}$  level.

The QFRS spectra on green UCPL emission ( $\lambda \approx 550 \text{ nm}$ ) were measured at pumping wavelength of 975 nm and at various pump powers using the QFRS system specified in the previous articles [7, 24, 25], except that we replaced the focusing lens to focal length of  $\approx 25 \text{ mm}$  and we used photomultiplier (PMT) tube Hamamatsu H10723-20 as a detector preset to 0.7 V. The QFRS spectra were acquired at various pump powers ranging from 0.79 to 42.5 mW. Pump power  $P=1 \text{ mW}$  corresponds to photon-flux density  $\Phi \sim 2.9 \times 10^{21} \text{ cm}^{-2} \text{ s}^{-1}$ . The excitation power dependence of green ( $\approx 550 \text{ nm}$ ) and red ( $\approx 660 \text{ nm}$ ) UCPL emission was measured by the same instrument using the lock-in detection at chopping frequency of 30 Hz.

## Results and discussion

Figure 1a presents the XRD diffractograms of 0.5 and 1.0 % Er-doped GGAS samples. The samples doped with 0.5 and less at% of  $\text{Er}^{3+}$  ions are amorphous however, the 1 at% Er-doped sample is partially crystalline as indicate the sharp diffraction lines in Fig. 1a. This is also suggested by SEM images of GGAS samples doped with 0.5 or 1 at% of Er ions (Fig. 1c and d) where the presence of at least two phases in heavily Er-doped sample is observed. The presence of crystallites in 1 at% Er-doped GGAS sample is also featured by sharp-shaped  $\text{Er}^{3+}: {}^4I_{13/2} \rightarrow {}^4I_{15/2}$  ( $\approx 1.5 \mu\text{m}$ ) emission spectrum presented in Fig. 1b due to appearance of Stark levels thus indicating that the crystalline phase occurs in close proximity to the  $\text{Er}^{3+}$  ions [26, 27].

The experimentally determined chemical composition of all Er-doped GGAS samples shown in Table 1 agrees well with theoretical composition. However, as presented by SEM image of Fig. 1d, the heavily



**Fig. 1:** Effect of Er content on glass-forming ability.

(a) XRD diffractograms, (b)  $\text{Er}^{3+}: {}^4I_{13/2} \rightarrow {}^4I_{15/2}$  ( $\sim 1.5 \mu\text{m}$ ) PL emission spectra under 980 nm excitation and (c, d) SEM images for the respective 0.5 at% and 1 at% Er-doped GGAS samples.

**Table 1:** The chemical composition of the synthesized GGAS:Er samples determined by the EDX spectroscopy.

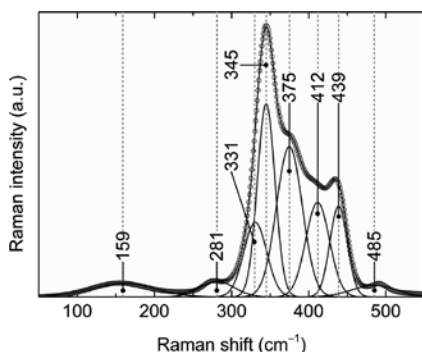
Er in $\text{Ge}_{25}\text{Ga}_8\text{As}_2\text{S}_{65}$	Chemical composition				
	Ga (at%)	Ge (at%)	As (at%)	S (at%)	Er (at%)
0.01 at%	7	26	2	65	–
0.1 at%	7	26	2	65	–
0.5 at%	7	26	2	65	–
1 at% (light phase)	4	12	1	64	19
1 at% (dark phase)	7	26	2	65	–

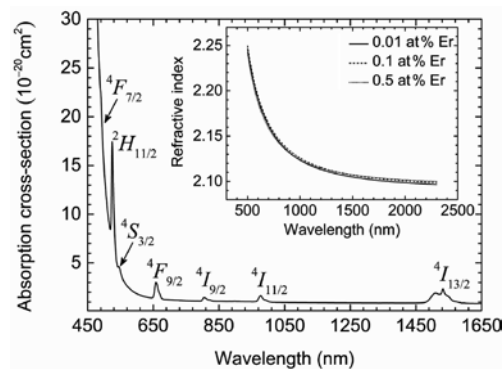
The experimental error is  $\pm 1$  at%.

Er-doped sample contains two phases: dark phase and light phase. The chemical composition of dark phase corresponds to theoretical chemical composition of prepared glasses however, the light phase is Er-enriched phase (see Table 1). Thus, the Er solubility limit in  $\text{Ge}_{25}\text{Ga}_8\text{As}_2\text{S}_{65}$  glasses lies between 0.5 and 1 at% of Er ions which agrees well with the previously published work [27], where for the homogenous distribution of RE ions in chalcogenide glasses the Ga/RE atomic ratio is proposed to be  $\geq 10$ .

The structure of the GGAS glass was investigated by the Raman scattering. A representative reduced Raman spectrum shown in the Fig. 2 was decomposed to 8 Gaussian-type lines centered approximately at 159, 281, 331, 345, 375, 412, 439 and 485  $\text{cm}^{-1}$ . An attempt to interpret the origin of these lines to specific vibrational modes is based on previous works [28–33]. The bands at 159, 345 and 412  $\text{cm}^{-1}$  can be assigned to corner-sharing  $\nu_4$ ,  $\nu_1$  and  $\nu_3$  vibrations of the  $[\text{GeS}_4]$  tetrahedra, while contributions forming the corresponding modes of the  $[\text{GaS}_4]$  tetrahedra cannot be excluded. The band at 375  $\text{cm}^{-1}$  is assigned to  $\nu_1$ - $[\text{GeS}_4]$  and  $[\text{GaS}_4]$  vibrations of edge-shared tetrahedral units. This line is practically the companion  $\nu_1^c$  vibration mode related to edge-shared tetrahedral of  $[\text{GeS}_4]$  at 370  $\text{cm}^{-1}$ . The band at 281  $\text{cm}^{-1}$  can be assigned to the vibrational mode of the  $\text{S}_3\text{Ge}(\text{Ga})\text{-Ge}(\text{Ga})\text{S}_3$  structural units containing homonuclear (semi)metal–(semi)metal bonds. The band centered at 331  $\text{cm}^{-1}$  could be possibly assigned to  $\nu_1$ - $[\text{GaS}_4]$  vibrations of tetrahedral units. The band at 439  $\text{cm}^{-1}$  is still an unsolved issue, but could be probably assigned to companion  $\nu_3^c$  vibration modes related to edge-shared tetrahedral units  $[\text{GeS}_4]$  and  $[\text{GaS}_4]$ . The band around 485  $\text{cm}^{-1}$  has been assigned to the existence of disulfide bonds (or two-membered S chains) in form of  $\text{S}_2\text{As-S-S-As}_2\text{S}$  and  $\text{S}_3\text{Ge}(\text{Ga})\text{-S-S-Ge}(\text{Ga})\text{S}_3$ .

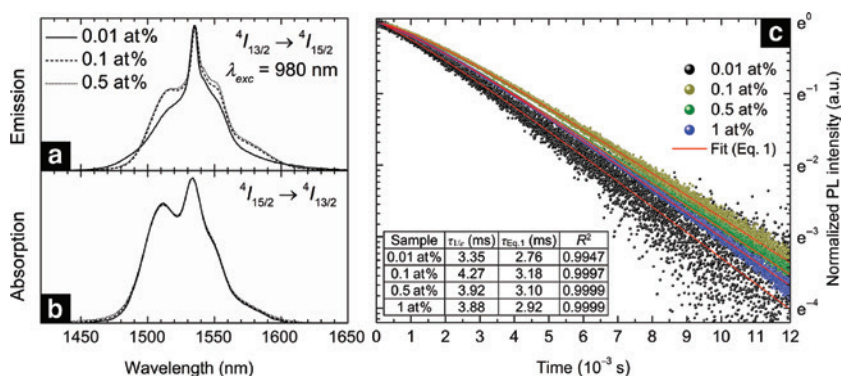
Figure 3 presents absorption-cross section spectrum of  $\text{Er}^{3+}$  in GGAS glass composed of seven  $\text{Er}^{3+}$  absorption bands. These bands are attributed to ground state absorption (GSA) transitions from  $\text{Er}^{3+}$ :  $^4I_{15/2}$  to  $\text{Er}^{3+}$ :  $^4I_{13/2}$  ( $\approx 1552$  nm),  $^4I_{11/2}$  ( $\approx 991$  nm),  $^4I_{9/2}$  ( $\approx 817$  nm),  $^4F_{9/2}$  ( $\approx 666$  nm),  $^4S_{3/2}$  ( $\approx 552$  nm),  $^2H_{11/2}$  ( $\approx 530$  nm) and  $^4F_{7/2}$  ( $\approx 491$  nm) levels. The inset of the Fig. 3 shows the dispersion of refractive index of GGAS:Er $^{3+}$  measured by spectroscopic ellipsometry in transparent spectral region. The refractive index is practically identical for all studied samples ( $n_g \approx 2.10$  at  $\lambda = 1550$  nm), except that of 1 at% Er-doped sample which was partially crystalline and therefore was not analyzed.

**Fig. 2:** Reduced Raman spectrum of the GGAS glass. Open circles are experimental data, bold black line is sum of Gaussians used for spectrum decomposition.



**Fig. 3:** GSA cross-section spectrum of the 0.5 at% Er-doped GGAS glass. Inset: Dispersion of refractive index for GGAS glasses doped with 0.01, 0.1 and 0.5 at% of Er.

Figure 4a and b show normalized absorption and emission spectra of the  $\text{Er}^{3+}$ :  $^4I_{13/2} \leftrightarrow ^4I_{15/2}$  ( $\lambda \approx 1.5 \mu\text{m}$ ) transitions in GGAS glasses at pumping wavelength of 980 nm. The  $\approx 1.5 \mu\text{m}$  emission band is broadened with increasing concentration of Er ions, while the absorption band of all studied glasses samples exhibits no significant changes in shape. For better understanding of this behavior, lifetimes of  $\text{Er}^{3+}$ :  $^4I_{13/2}$  energy level as a function of Er concentration in GGAS glasses were analyzed. The decay curves of the  $^4I_{13/2} \rightarrow ^4I_{15/2}$  transitions under 980 nm pumping wavelength are presented in Fig. 4c. The  $\text{Er}^{3+}$ :  $^4I_{13/2}$  level lifetime  $\tau = 1/k_1$  was analyzed by fitting of decay curves in Fig. 4c using the Eq. 1 with fixed parameters of  $k_2 = 696 \text{ s}^{-1}$  and  $\beta = 0.136$  which were obtained by Judd–Ofelt theory with inclusion of multiphonon relaxation rate [24]. Lifetime values determined by using Eq. 1 or from  $1/e$  values are presented in the inset of Fig. 4c. It can be seen that lifetimes determined from  $1/e$  values are notably higher than those obtained by using the Eq. 1 nevertheless, they holds same trends. The  $\text{Er}^{3+}$ :  $^4I_{13/2}$  lifetime value  $\tau \approx 2.76 \text{ ms}$  determined by Eq. 1 for 0.01 % Er-doped GGAS sample matches better the lifetime  $\tau^{10} \approx 2.16 \text{ ms}$  calculated by Judd–Ofelt theory than that  $\tau \approx 3.35 \text{ ms}$  determined from  $1/e$  value. The  $^4I_{13/2}$  lifetime is firstly prolonged with increasing Er concentration from 0.01 to 0.1 at% and subsequently decreases with further increase of Er content. However, the mechanism behind this is still unclear. The lifetime may be prolonged e.g. due to radiation trapping processes [34–36] or by cross-relaxation CR2 processes  $\text{Er}^{3+}$ :  $^2H_{11/2}$ ,  $^4I_{15/2} \rightarrow ^4F_{9/2}$ ,  $^4I_{13/2}$  [37, 38]. Contrary to that, the lifetime shortening may be explained by the concentration quenching [39] or by the  $\text{Er}^{3+}$ :  $^4I_{11/2}$ ,  $^4I_{13/2} \rightarrow ^4F_{9/2}$ ,  $^4I_{15/2}$  energy transfer upconversion ETU2 processes [40–43]. The considerable presence of cross-relaxation and energy transfer upconversion processes is discussed later in the manuscript.



**Fig. 4:** Er concentration dependence on the  $^4I_{13/2} \leftrightarrow ^4I_{15/2}$  transitions.

(a, b) Are respective normalized emission and absorption spectra of the  $\text{Er}^{3+}$ :  $^4I_{13/2} \leftrightarrow ^4I_{15/2}$  transitions in GGAS:Er glass under 980 nm pumping wavelength. (c) The decay curves of  $\text{Er}^{3+}$ :  $^4I_{13/2} \rightarrow ^4I_{15/2}$  transitions in GGAS glass under 980 nm excitation; inset:  $^4I_{13/2}$  lifetimes determined from  $1/e$  values  $\tau_{1/e}$  or by using the Eq. 1  $\tau_{Eq.1}$  with maximal error of  $\pm 0.05 \text{ ms}$ . (Color online).

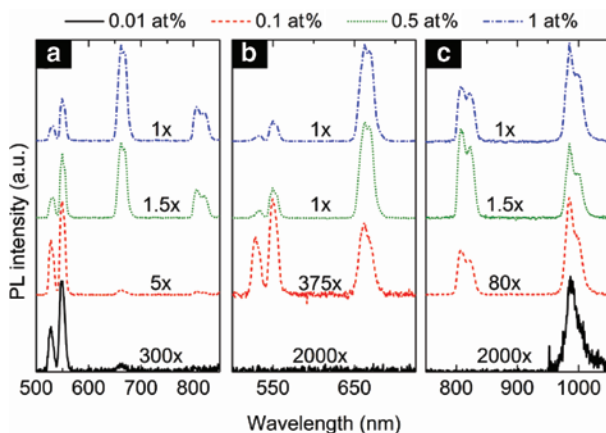


Upconversion photoluminescence (UCPL) emission spectra at pumping wavelengths of 980 or 1550 nm are presented in Fig. 5. There are observed five emission bands originating from electronic transitions from  $\text{Er}^{3+}$  upper levels of  $^2H_{11/2}$  ( $\approx 530$  nm),  $^4S_{3/2}$  ( $\approx 550$  nm),  $^4F_{9/2}$  ( $\approx 660$  nm),  $^4I_{9/2}$  ( $\approx 810$  nm) and  $^4I_{11/2}$  ( $\approx 990$  nm) to  $\text{Er}^{3+}$ :  $^4I_{15/2}$  ground level. The overall UCPL emission intensity as well as red-to-green UCPL emission intensity ratio, i.e. ratio of the red UCPL emission intensity of the  $\text{Er}^{3+}$ :  $^4F_{9/2} \rightarrow ^4I_{15/2}$  ( $\approx 660$  nm) transitions to that of the green UCPL emission intensity of the  $\text{Er}^{3+}$ :  $^2H_{11/2}/^4S_{3/2} \rightarrow ^4I_{15/2}$  ( $\approx 530 + 550$  nm) transitions, increases with increasing  $\text{Er}^{3+}$  concentration. Such behavior may be explained by the exploration of the UCPL dynamics.

There are three basic UCPL mechanisms adopted in literature [44]: (I) ground state absorption (GSA) followed by excited state absorption (ESA), i.e. GSA/ESA; (II) ground state absorption (GSA) followed by energy transfer upconversion (ETU), i.e. GSA/ETU; and (III) ground state absorption (GSA) followed by cross-relaxation (CR) processes, i.e. photon avalanche (PA) upconversion. The GSA/ESA mechanism may originate within single  $\text{Er}^{3+}$  ion thus, it is independent on the Er–Er interionic distance [44]. In contrast, the GSA/ETU or PA UCPL requires energy transfer between two neighboring  $\text{Er}^{3+}$  ions therefore they are dependent on the interionic distance which is usually adjusted by concentration of  $\text{Er}^{3+}$  ions inside of a host matrix [44]. Since the green UCPL emission intensity increases rapidly and nonlinearly with increasing concentration of  $\text{Er}^{3+}$  ions, the additional GSA/ETU mechanism to GSA/ESA may stay behind the UCPL dynamics in highly Er-doped GGAS glasses, i.e. mixed GSA/ESA + ETU [44, 45]. Thus, we investigated the green UCPL dynamics ( $\lambda \approx 550$  nm) using the QFRS for three-level model approximation (see Fig. 7) at pump wavelength of 975 nm and various pump powers  $P$  (mW) or photon-flux densities  $\Phi$  ( $\text{cm}^{-2} \text{s}^{-1}$ ). Further details can be found in the recently published paper [24].

The double logarithmic dependency of UCPL emission intensity versus pump power is presented for green and red UCPL emission in Fig. 6 and comprises of two linear segments, where the slope of each segment provides the number of photons involved in the UCPL process [44]. Theoretically, the slope  $n$  of low-power linear segment is  $n=2$  for both GSA/ESA and GSA/ETU UCPL mechanisms, and it scales as  $n=1-2$  for GSA/ESA or  $n=1$  for GSA/ETU processes at high-power region [44]. The low-power and high-power linear segments are divided by a kink point  $P_k$  (or  $\Phi_k$ ) which was found to be  $\sim 3$  mW for green UCPL and  $\sim 2.8$  mW for red UCPL. The experimentally determined slope values  $n \approx 2$  at  $P < P_k$  indicate a presence of two-photon UCPL processes.

The energy transfer rate parameter  $w_{11}$  ( $\text{s}^{-1}$ ) of the  $\text{Er}^{3+}$ :  $^4I_{11/2}$ ,  $^4I_{11/2} \rightarrow ^4F_{7/2}$ ,  $^4I_{15/2}$  transition for green UCPL may be analyzed by QFRS on green UCPL at pump powers below  $P_k$  in combination with three-level model [24, 44]. Figure 7 shows the  $P$ -evolved QFRS spectra of the green UCPL for the 0.01 (a) and 0.5 % (b) Er-doped GGAS glasses measured from pump powers  $P \sim 0.79$  to 42.5 mW or photon-flux densities from  $\Phi \sim 2.3 \times 10^{21}$  to  $1.2 \times 10^{23} \text{ cm}^{-2} \text{s}^{-1}$ . The QFRS spectra plotted as a function of lifetime  $\tau$  (s) in logarithmic scale are double-peaked, where long-lifetime component  $\tau_1$  corresponds to  $\Phi$ -evolved relaxation rate  $R_1(\Phi) = 1/\tau_1(\Phi)$  at the intermediate level  $^4I_{11/2}$  and short-lifetime component  $\tau_2$  to  $\Phi$ -evolved relaxation rate  $R_2(\Phi) = 1/\tau_2(\Phi)$  at the upper coupled manifolds  $^4F_{7/2}/^2H_{11/2}/^4S_{3/2}$ . The lifetime distributions were obtained by deconvolution of QFRS



**Fig. 5:** UCPL emission spectra of the  $\text{Er}^{3+}$  doped GGAS chalcogenide glasses excited. (a) By the 980 nm or (b and c) 1550 nm laser. (Color online).

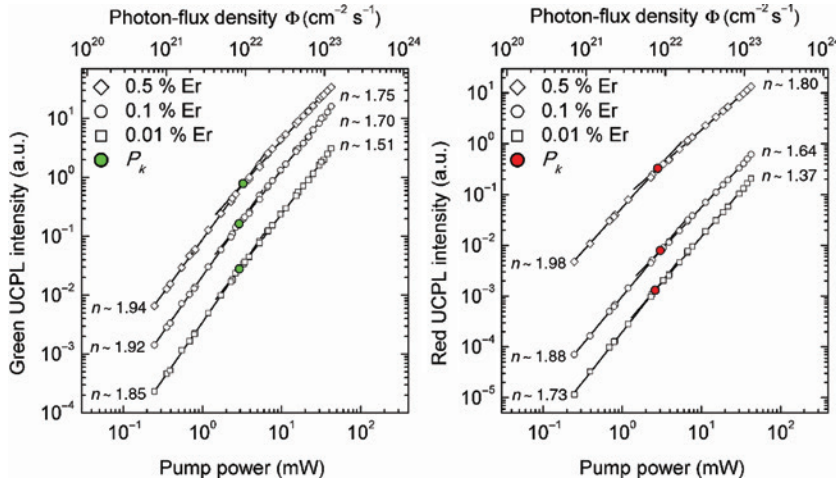


Fig. 6: The double logarithmic plots of green ( $\approx 550$  nm) and red ( $\approx 660$  nm) UCPL emission intensity vs. pump power at pumping wavelength of 975 nm.

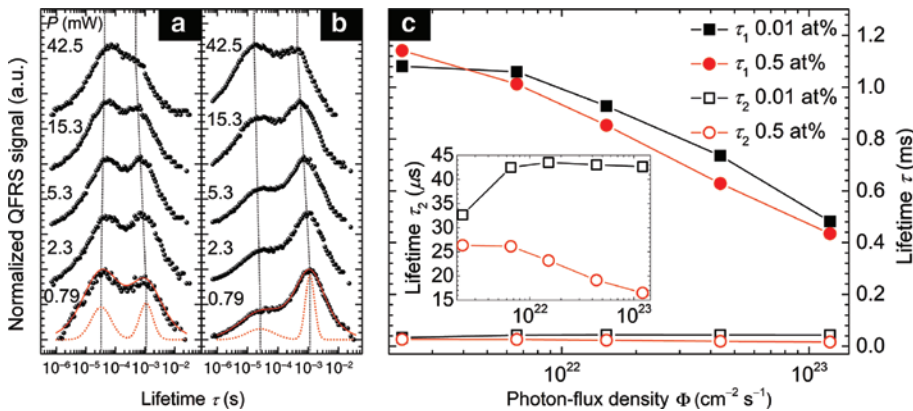


Fig. 7: QFRS spectroscopy.

$P$ -evolved QFRS spectra of the green UCPL for the (a) 0.01 at% and (b) 0.5 at% Er-doped GGAS glasses measured under 975 nm excitation. (c)  $\Phi$ -evolved lifetimes  $\tau_1$  and  $\tau_2$  for 0.01 and 0.5 at% Er-doped GGAS glasses under 975 nm pumping wavelength; inset: Detail of  $\Phi$ -evolved  $\tau_2$ .

spectra by a linear combination of two Gaussians. The  $\tau_1$  component is rapidly shortened with increasing  $\Phi$  from  $\approx 1.14$  to  $\approx 0.43$  ms while  $\tau_2$  component is less sensitive to change of  $\Phi$  with lifetime value of  $\sim 10$   $\mu\text{s}$  (Fig. 7c). Theoretically, the presence of mixed GSA/ESA + ETU process is featured by significant growth of the peak at  $\tau_2$  component compared to peak at  $\tau_1$  component with increasing  $\Phi$  [24] which was observed experimentally in heavily 0.5 at% Er-doped GGAS sample (see Fig. 7).

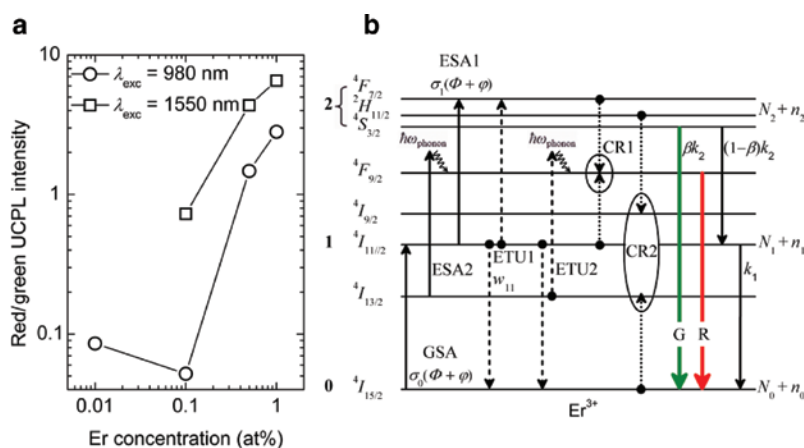
Moreover, from QFRS spectra presented in Fig. 7 may be observed that the short lifetime  $\tau_2$  rapidly decreased in heavily Er-doped GGAS sample. This may be explained by the closer proximity of fundamental absorption edge to thermally coupled  $\text{Er}^{3+}$  energy levels  ${}^4F_{7/2}/{}^2H_{11/2}/{}^4S_{3/2}$  (see Fig. 3) allowing the energy transfer processes from  $\text{Er}^{3+}$  ions to a host matrix [24, 25]. At certain low  $\Phi$ , the energy transfer parameter  $w_{11}$  may be analyzed by the ratio  $\gamma(\Phi \rightarrow 0)$  expressed by Eq. 2, which is ratio between peak  $a_2$  at the short-lifetime component  $\tau_2$  and peak  $a_1$  at the long-lifetime component  $\tau_1$  [24]:

$$\gamma(0) = \left(1 - \frac{k_1}{k_2}\right) \left(1 + \frac{2w\sigma_0}{k_1\sigma_1}\right)^{-1} - \frac{k_1}{k_2}, \quad (2)$$

where  $k_1 = R_1(\Phi \rightarrow 0)$  and  $k_2 = R_2(\Phi \rightarrow 0)$  are relaxation rates at the intermediate and upper coupled energy levels, respectively,  $\sigma_0$  is GSA cross-section and  $\sigma_1$  is ESA cross-section. We approximated the  $\gamma(0)$  ratio utilizing

the parameters  $a_1$ ,  $a_2$ ,  $k_1$ ,  $k_2$  analyzed from the QFRS spectra at  $\Phi < \Phi_k$  ( $P \sim 0.79$  mW). To derive the energy transfer rate  $w_{11}$  ( $\text{s}^{-1}$ ) from ratio  $\gamma(0)$ , the knowledge of  $\sigma_0$  and  $\sigma_1$  is required as well. These parameters were obtained by using Judd–Ofelt (JO) theory [46–50] with resulting JO intensity parameters  $\Omega_2 = (13.02 \pm 0.07) \times 10^{-20} \text{ cm}^2$ ,  $\Omega_4 = (3.41 \pm 0.08) \times 10^{-20} \text{ cm}^2$  and  $\Omega_6 = (1.48 \pm 0.03) \times 10^{-20} \text{ cm}^2$  from which were subsequently calculated  $\sigma_0 = 6.6 \times 10^{-20} \text{ cm}^2$  and  $\sigma_1 = 10.9 \times 10^{-20} \text{ cm}^2$  values. We found that the parameter  $w_{11} = 40 \text{ s}^{-1}$  for the 0.01 % Er-doped GGAS sample and  $w_{11} = 2960 \text{ s}^{-1}$  for the 0.5 % Er-doped GGAS glass. These parameters are slightly higher than those obtained for GeGaS:Er glasses [24] which is however attributed to energy transfer processes from  $\text{Er}^{3+}$ :  ${}^4F_{7/2}/{}^2H_{11/2}/{}^4S_{3/2}$  levels to a host matrix due to their merging [24, 25] as is evident in Fig. 3. This is also supported by the extraordinary low values of short-lifetime component [25]  $\tau_2 \approx 33 \mu\text{s}$  for 0.01 % Er-doped sample and  $\tau_2 \approx 26 \mu\text{s}$  for 0.5 % Er-doped sample at the lowest  $\Phi$  in comparison with lifetime value obtained by JO theory of  $\tau_2(\text{JO}) \approx 168 \mu\text{s}$ .

The increase of red-to-green UCPL emission intensity under 980 nm pumping wavelength with increasing Er concentration Fig. 8a may be explained on the basis of energy level model approximation depicted in Fig. 8b in accordance with Refs. [25, 40–43, 51–55] as following. At low Er concentrations, the ETU or CR processes may be neglected [44]. Thus, the green emitting levels  ${}^4F_{7/2}/{}^2H_{11/2}/{}^4S_{3/2}$  are populated mainly via GSA/ESA processes, while the  $\text{Er}^{3+}$ :  ${}^4F_{9/2}$  energy level may be populated by the radiative and/or nonradiative recombination from excited  $\text{Er}^{3+}$ :  ${}^4F_{7/2}/{}^2H_{11/2}/{}^4S_{3/2}$  levels or by the radiative and/or nonradiative recombination from  $\text{Er}^{3+}$ :  ${}^4I_{11/2}$  to  ${}^4I_{13/2}$  followed by ESA process  $\text{Er}^{3+}$ :  ${}^4I_{13/2} \rightarrow {}^4F_{9/2}$  [25]. As a result, the green UCPL emission dominates over red UCPL emission at low concentrations of Er ions, as was observed in Fig. 8a. However, at higher concentrations of Er ions, the ETU and CR processes become pronounced and may significantly modify above mentioned dynamics. In the case of green UCPL emission, there is proposed  $\text{Er}^{3+}$ :  ${}^4I_{11/2}$ ,  ${}^4I_{11/2} \rightarrow {}^4F_{7/2}$ ,  ${}^4I_{15/2}$  energy transfer [24] which was studied by the QFRS mentioned above. This ETU process significantly promotes the green UCPL emission intensity with increasing Er concentration. However, in the case of red UCPL emission, the red-emitting level  ${}^4F_{9/2}$  may be populated by the  $\text{Er}^{3+}$ :  ${}^4I_{11/2}$ ,  ${}^4I_{13/2} \rightarrow {}^4F_{9/2}$ ,  ${}^4I_{15/2}$  energy transfer and  $\text{Er}^{3+}$ :  ${}^4F_{7/2}$ ,  ${}^4I_{11/2} \rightarrow {}^4F_{9/2}$ ,  ${}^4F_{9/2}$  CR1 processes [43, 53–55] or by the  $\text{Er}^{3+}$ :  ${}^2H_{11/2}/{}^4S_{3/2}$ ,  ${}^4I_{15/2} \rightarrow {}^4I_{9/2}$ ,  ${}^4I_{13/2}$  CR2 followed by ESA2 or ETU2 processes [42, 51, 52]. Since 3–4 photons are required to obtain green ( $\sim 530 + 550 \text{ nm}$ ) and red ( $\sim 660 \text{ nm}$ ) UCPL emission at pumping wavelength of 1550 nm, the UCPL mechanism is more complex. In low  $\text{Er}^{3+}$ -doped samples, the green-emitting levels ( ${}^2H_{11/2}$ ,  ${}^4S_{3/2}$ ) are populated via the sequential GSA/ESA  ${}^4I_{15/2} \rightarrow {}^4I_{13/2} \rightarrow {}^4I_{9/2} \rightarrow {}^2H_{11/2}/{}^4S_{3/2}$  transitions and the red-emitting level  ${}^4F_{9/2}$  by the subsequent radiative or nonradiative recombination  ${}^2H_{11/2}/{}^4S_{3/2} \rightarrow {}^4F_{9/2}$  or by the



**Fig. 8:** Green and Red upconversion photoluminescence.

(a) Red-to-Green UCPL emission intensity ratio versus  $\text{Er}^{3+}$  concentration in GGAS at pumping wavelength of 980 and 1550 nm, (b) Schematic of energy-level diagram for green and red UCPL emission at pumping wavelength of 975 nm; the curved arrows indicate the multiphonon relaxation routes;  $N_i$  represent population densities with perturbed population densities  $n_i$  at energy level  $i$  originating from a sinusoidal modulation  $\varphi$  of continuous-wave photon-flux density  $\Phi$ ;  $\beta$  is branching ratio under three-level model approximation. (Color online).



phonon-assisted  ${}^4I_{15/2} \rightarrow {}^4I_{13/2} \rightarrow {}^4I_{9/2} \rightarrow {}^4I_{11/2} + \text{phonon} \rightarrow {}^4F_{9/2}$  GSA/ESA transitions. In contrast to 980 nm excitation wavelength, the red-to-green UCPL emission intensity ratio is higher for samples excited by 1550 nm which suggests the presence of phonon-assisted GSA/ESA processes mentioned above leading to population of red-emitting level  $\text{Er}^{3+}: {}^4F_{9/2}$ . The presence of the phonon-assisted process “ ${}^4I_{9/2} \rightarrow {}^4I_{11/2} + \text{phonon}$ ” is also supported by the higher UCPL emission intensity of the  $\text{Er}^{3+}: {}^4I_{11/2} \rightarrow {}^4I_{15/2}$  (~990 nm) transitions compared with the  $\text{Er}^{3+}: {}^4I_{9/2} \rightarrow {}^4I_{15/2}$  (~810 nm) UCPL (see Fig. 5c). In heavily Er-doped samples the red UCPL emission dominates over the green UCPL emission which may be attributed to the presence of additional energy transfer  $\text{Er}^{3+}: {}^4I_{13/2}, {}^4I_{11/2} \rightarrow {}^4I_{15/2}, {}^4F_{9/2}$  populating the red-emitting level  ${}^4F_{9/2}$ . Such energy transfer process should depopulate the  $\text{Er}^{3+}: {}^4I_{11/2}$  level thus decrease the  $\text{Er}^{3+}: {}^4I_{11/2} \rightarrow {}^4I_{15/2}$  (~990 nm) UCPL emission intensity which is really lower in comparison with the  $\text{Er}^{3+}: {}^4I_{9/2} \rightarrow {}^4I_{15/2}$  (~810 nm) UCPL intensity in the 0.5 % Er-doped GGAS glass (see Fig. 5c). Moreover, the UCPL emission spectrum for 1 % Er-doped sample in Fig. 5c shows higher UCPL emission intensity at ~990 nm compared with those at ~810 nm which suggests the possible presence of additional cross-relaxation processes  $\text{Er}^{3+}: {}^4I_{13/2}, {}^4S_{3/2} \rightarrow {}^4I_{11/2}, {}^4F_{9/2}$  and  $\text{Er}^{3+}: {}^4I_{9/2}, {}^4S_{3/2} \rightarrow {}^4F_{9/2}, {}^4F_{9/2}$  all populating the red-emitting level  ${}^4F_{9/2}$  [56–59]. So mostly, the red-emitting level is populated at the expense of population of green emitting level under the both 980 and 1550 nm excitation wavelengths [60]. Therefore, red-to-green UCPL emission intensity ratio increases with increasing Er concentration.

## Conclusions

We studied structural properties, ~1.5  $\mu\text{m}$  Stokes and upconversion photoluminescence in Er-doped  $\text{Ge}_{25}\text{Ga}_8\text{As}_2\text{S}_{65}$  glasses at pumping wavelengths of 980 and 1550 nm. Since the 1 at% Er-doped GGAS sample was partially crystalline with Er-enriched phase and those doped 0.5 at% remained amorphous, it may be deduced that the Er solubility limit in studied glasses lies between 0.5 and 1 at%. The broadening of the  $\text{Er}^{3+}: {}^4I_{13/2} \rightarrow {}^4I_{15/2}$  ( $\lambda \approx 1.5 \mu\text{m}$ ) emission spectrum under 980 nm excitation and change of  ${}^4I_{13/2}$  lifetime with increasing concentration of Er ions was discussed in terms of radiation trapping and upconversion processes. Upconversion photoluminescence was observed from visible green to near-infrared spectral region at pumping wavelength of 980 and 1550 nm. The overall UCPL emission intensity as well as red-to-green UCPL emission intensity ratio increases with increasing Er concentration which was discussed by changes of the UCPL dynamics including the energy transfer and the cross-relaxation processes at higher content of Er ions. The green UCPL emission ( $\lambda \approx 550 \text{ nm}$ ) was studied by the QFRS spectroscopy under 975 nm excitation and at various pump powers in term of QFRS transfer function for three-level model from which the energy transfer upconversion parameter  $w_{11}$  was deduced. The double-peaked QFRS spectra are composed of two lifetime components where the long-lifetime component  $\tau_1 \approx 1.14\text{--}0.43 \text{ ms}$  reflects the relaxation at the intermediate level  $\text{Er}^{3+}: {}^4I_{11/2}$  while the short lifetime component  $\tau_2$  of several tens of  $\mu\text{s}$  reflects the relaxation rate at coupled energy levels  ${}^4F_{7/2}, {}^2H_{11/2}, {}^6S_{3/2}$ . The green UCPL dynamics in 0.01 at% Er-doped GGAS glass is mainly driven via the GSA/ESA processes while that in 0.5 at% Er-doped sample contains mixed GSA/ESA + ETU processes which is manifested by the greater energy transfer upconversion rate parameter  $w_{11} = 2960 \text{ s}^{-1}$  for 0.5 % Er-doped samples compared to negligible ETU rate  $w_{11} = 40 \text{ s}^{-1}$  for 0.01 % Er-doped sample. Such ETU rate parameters are slightly higher than those reported for  $\text{GeGaS:Er}$  glasses which is explained by the additional energy transfer processes from  $\text{Er}^{3+}$  ions to a host matrix due to merging of  $\text{Er}^{3+}: {}^4F_{7/2}, {}^2H_{11/2}, {}^6S_{3/2}$  green emitting levels with fundamental absorption of a host matrix. Nevertheless, the  $\text{GeGaAsS:Er}$  glasses are promising candidates for UCPL applications as they have improved glass-forming ability and thermal properties compared to  $\text{GeGaS:Er}$  glasses and higher visible transparency than  $\text{GeGaSbS:Er}$  glasses.

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