

## **Supplementary Information for “Scalable Unitary Computing using Time-Parallelized Photonic Lattices”**

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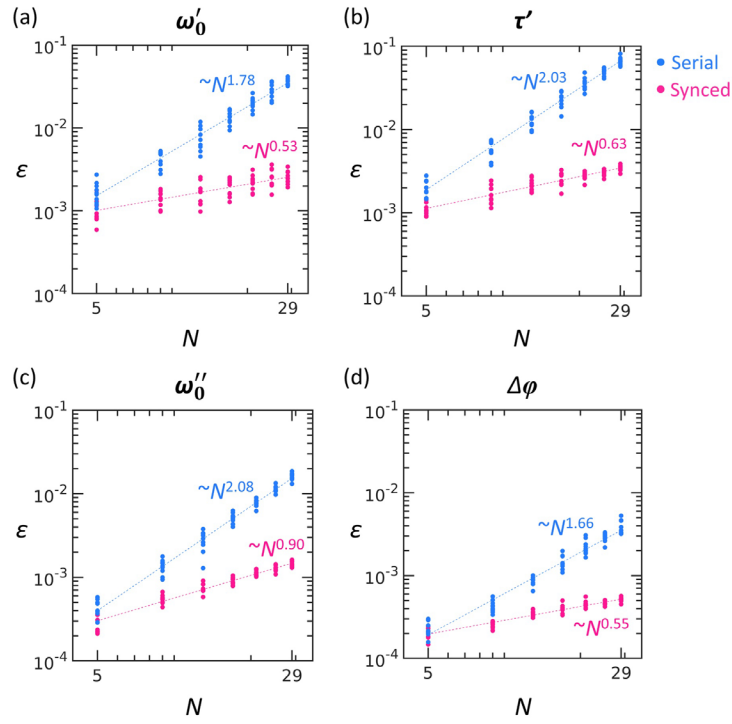
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**Note S1. Fidelity analysis on system size**

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Figure S1 shows the scaling behaviours of errors  $\varepsilon$  with respect to  $N$  for different origins of system defects: resonance (Fig. S1a) and lifetime (Fig. S1b) perturbations, resonator radiation loss (Fig. S1c), and the altered zero-field condition of loop couplers (Fig. S1d). We observe scaling behaviours well approximated by power-law fitting (dashed lines in Fig. S1a-d). Notably, the synchronization scheme consistently yields superior fidelity as compared to the serial implementation.



**Fig. S1. Fidelity scaling.** (a-d) Scaling of errors with respect to the system size  $N$ : (a) resonance fluctuations with  $\sigma = 10^{-7}$ , (b) lifetime fluctuations with  $\sigma = 10^{-3}$ , (c) resonator radiation loss with  $\sigma = 10^{-8}$ , and (d) phase-shift defects in loop couplers with  $\sigma = 10^{-5}$ . At each  $N$ , we examine 10 realizations of random Haar matrices. Dashed lines denote the power-law fitting. All the other parameters are the same as those in Fig. 4 in the main text.