

## Testing Related to Production Techniques

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# Cup drawing predictions for a 6016-T4 aluminum alloy

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**Abstract:** This study investigates the interplay between process and computation parameters affecting the accuracy of finite element analysis (FEA) results for cup manufacturing. By revisiting the Esaform-2021 benchmark, this research aims to elucidate the impact of process parameters on FEA accuracy and recommend strategies for enhancing cup drawing fidelity. By conducting a parametric study focusing on the force–displacement behavior of a 6016-T4 alloy cup drawing process, an “optimized” force–displacement curve was obtained, demonstrating improved agreement with reference results. Die clearance, friction coefficient, time step size, and termination time are used in parametric finite element study. Key findings from the parametric study can be concluded that die clearance significantly affects punch force; a die clearance of 1.4 mm yielded the best match with experimental results, attributed to reduced blank-stuck phenomenon compared to smaller clearances. The friction coefficient showed a direct impact; a friction coefficient of  $\mu = 0.1$  accurately replicated the experimental peak force, highlighting the sensitivity of force predictions to friction parameters. Time step size and termination time demonstrated minimal influence on FEA results, suggesting prioritization of parameters accelerating solution time. Finally, the relationships between process and FEA computation parameters and predictions were revealed for more realistic cup drawing process prediction accuracy.

**Keywords:** parametric modeling; cup drawing; aluminum alloy; process parameters; numerical parameters

## 1 Introduction

Earing is a common defect that can affect the quality of the final product in sheet metal forming, specifically characterized by the formation of non-uniform wavy edges at the flange of the drawn cup. Earing arises from the anisotropic mechanical properties of sheet metal, typically caused by the grain structure developed during the rolling process. The yield stress and plastic flow behavior vary depending on the loading direction relative to the rolling direction, leading to non-uniform material flow during drawing [1]–[3]. The number of ears typically corresponds to the crystallographic texture of the sheet metal, with four ears being the most common for cubic crystal structures [4], [5]. Optimizing process parameters such as draw ratio, blankholder force, and lubrication can help control material flow and mitigate earing formation [6]–[8]. Ipekoglu et al. [9] investigated the effect of different blank holder forces on the product quality. Koowattanasuchat et al. [10] employed response surface methodology to predict the thickness value and specific locations of the draw cup. They correlated the blank holder force with the thinning behavior of the drawn cups. Ünal and Özek [11] investigated the impact of the die and blank angles on the quality of the final product in cup-deep drawing processes. They reported that the angular deep drawing process led to better quality when compared to the conventional dies. Singh et al. [12] conducted a study on blank shape optimization to reduce the earing amount in the cup drawing process. They obtained good approximations.

Therefore, accurate analyses of the cup drawing process are crucial for ensuring the quality of the final product. Numerical techniques like finite element analysis have made it possible to predict force-stroke behavior and earing in cup drawing. Still, the accuracy of these predictions depends heavily on the calculation parameters used in the simulation [13]–[17]. Understanding the individual and combined effects of these calculation parameters is vital for optimizing FEA models and achieving accurate predictions of the cup drawing behavior of materials. Careful selection, calibration, and sensitivity analysis are necessary to balance computational efficiency with prediction accuracy, guide process optimization, and ultimately lead to high-quality

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sheet metal parts with minimal earing defects. In recent decades, researchers have focused on developing more realistic material models to enhance the accuracy of process simulations [18]–[22]. In the sheet metal cup drawing process, the force-stroke curve refers to a graphical representation of the drawing force plotted against the punch stroke during the deformation of the sheet metal blank. It provides valuable insights into the forming behavior of the material, process stability, and potential challenges. Experimental force-stroke curves can be employed to validate and calibrate FEA models for accurate process simulation.

Finite element analysis (FEA) has become a mainstay in the realm of sheet metal forming, offering valuable insights into the complex interplay of forces and material behavior during processes like cup drawing. However, the accuracy of these predictions relies not only on the sophistication of the FEA model but also on a delicate balance between process parameters and calculation settings. This study meticulously navigates this intricate landscape, delving into the specific case of cup drawing to refine our understanding of how these factors influence the reliability of FEA results. The Esaform-2021 cup drawing benchmark was studied to present enhanced prediction accuracy. This established platform provides a robust testing ground, allowing us to systematically explore the impact of various parameters on the predicted force–displacement behavior of a 6016-T4 alloy cup drawing process. Throughout this exploration, we leverage the power of parametric studies, meticulously varying both process and FEA calculation parameters to uncover their influences.

## 2 Summary of experimental studies

In Esaform-2021 [23], a cylindrical cup drawing test is performed on 6016-T4 aluminum alloy. Thirteen research groups from different universities participated in this benchmark study, including the authors of this research (USakarya). Within the scope of this benchmark, the mechanical tests were conducted in different universities from different countries, such as the University of Aveiro, Tokyo University of Agriculture and Technology (TUAT), the University of Porto, and the University of Liege. These tests cover the uniaxial tensile tests (University of Aveiro, TUAT), monotonic and reversal shear tests (University of Liege), and cup drawing tests (University of Porto). The research groups participating in this benchmark endeavored to understand the earing phenomenon of a highly anisotropic aluminum alloy 6016-T4 under ironing conditions.

They utilized or implemented different material models mainly focusing on the anisotropic yield criteria in different finite element software and tried to predict the ear formation in cup drawing. However, the necessity of an advanced anisotropic yield criterion is emphasized under the ironing condition since the ironing phenomenon hinders the accurate prediction of the formation.

The experimental deep drawing cylindrical cup tests were performed using a 300 kN hydraulic universal testing machine. Die tools consist of a die, a blank holder, a stopper, and a punch (cylindrical). Die tool geometries are summarized in Figure 1. Blank diameter and initial blank thickness were used as 107.54 mm and 0.98 mm, respectively. Blank holder force was applied as 40 kN. Punch stroke speed was considered 0.5 mm/s, and punch stroke was 54 mm for fully drawn cup. As a result of experiments a force–displacement curve is obtained to use as a reference for finite element analysis results with a 50 Hz data acquisition. The experimental force–displacement curve and an experimental sample are shown in Figure 2. As the figure shows, some polished regions occur at the upper locations of the cylindrical cup. This situation shows there is an ironing occurrence in the process, which can be seen with the plateau in the force–displacement curve.

The second part of the experimental studies was uniaxial tensile tests to obtain the mechanical properties of the aluminum alloy for plasticity modeling. The uniaxial tensile tests were performed at the Tokyo University of Agriculture and Technology (TUAT) with the sheet metals from the same batch with cup drawing test samples. Standard specimens (JIS Z 2241) with 50 mm gauge length and 12.5 mm gauge width were conducted. Tensile tests were performed at a strain rate of  $10^{-3} \text{ s}^{-1}$  by a Shimadzu-Autograph AG Model tensile test machine with 250 kN capacity. Test samples are generated with a  $15^\circ$  interval angle from the rolling direction (RD). A mechanical extensometer was used to obtain displacements, and for the Lankford parameters another test group was performed, which was up to 10 % nominal strain.

## 3 Parametric finite element modeling

In this stage of the study, parametric modeling of the cup drawing process was performed. As a beginning, process conditions and die geometries were used as given in the benchmark cup drawing process report to obtain a reference finite element result. Eta/Dynaform explicit commercial finite element software was used in reference simulation.

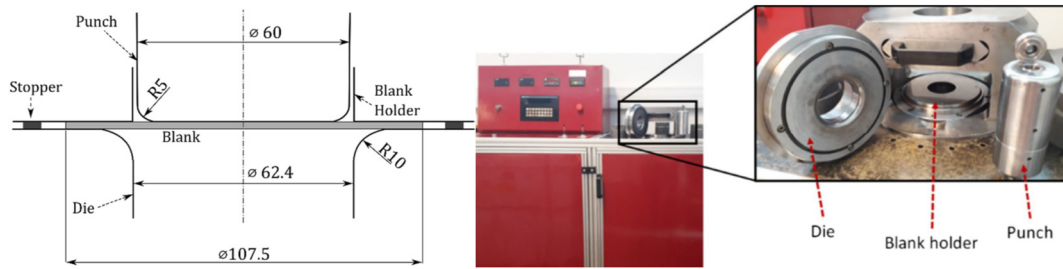


Figure 1: Die tool geometries of cup drawing process [23].

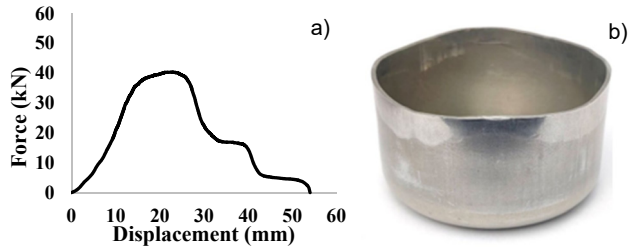


Figure 2: Cup drawing process, a) force-displacement curve, b) experimental sample [23].

In sheet metal forming analysis, the incremental finite element solution technique is often utilized to handle material nonlinearity, contact conditions, and large deformation. This method splits the analysis into small increments, with the solution at each step obtained by adding the incremental deformation to the previous solution. The incremental deformation is calculated assuming that the deformation during each time increment is small enough to be considered linear. The explicit time-integration scheme is widely used in sheet metal forming analysis for its

computational efficiency and ease of implementation [24]–[26]. This scheme calculates the element stiffness matrix and nodal forces at each time step based on the current values of nodal displacements, velocities, and accelerations. The element stresses and strains are then calculated using the updated nodal forces and the current values of element strains. These updated material properties include yield stress and hardening modulus. The explicit scheme has been successful in sheet metal forming simulations, including deep drawing, stretch forming, and bending. However, the explicit time-integration scheme is challenging. The explicit scheme has stability and accuracy issues in sheet metal forming analysis. The stability issue occurs when the time step size is too large, leading to unstable solutions and nonphysical results. Meanwhile, the accuracy issue occurs when the time step size needs to be increased, leading to excessive computational time and memory requirements. Therefore, choosing an appropriate time step size ensures stability and accuracy in sheet metal forming analysis. Nevertheless, explicit schemes have a more straightforward structure and are easier to implement than implicit FE

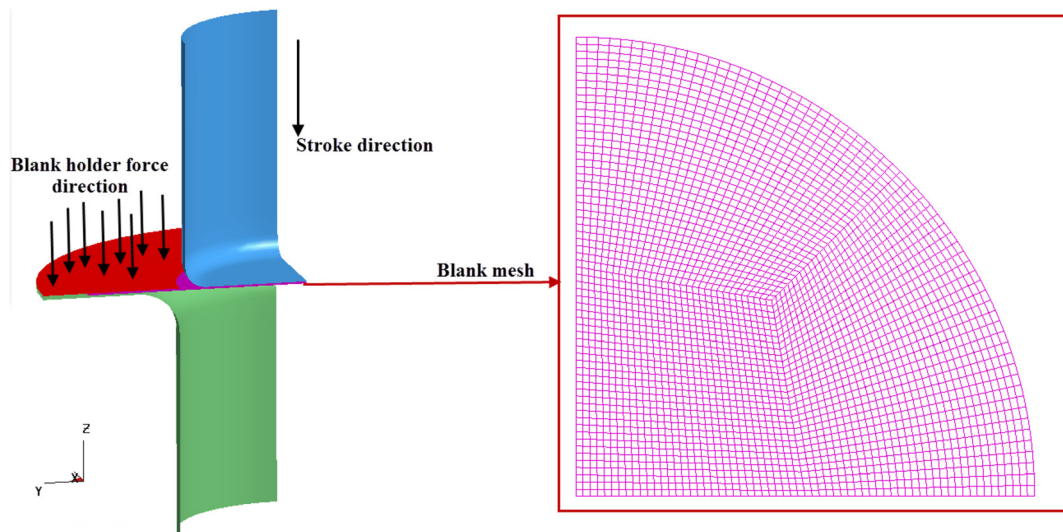
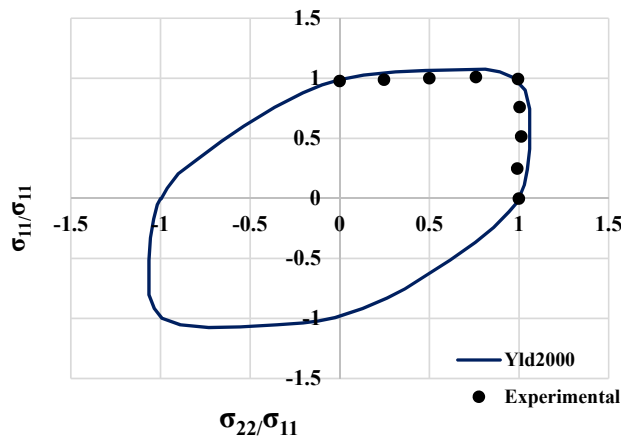


Figure 3: Finite element model of the cup drawing process.

**Table 1:** Parameters used as inputs for Yld2000 model.

Yld2000	$\alpha_1$	$\alpha_2$	$\alpha_3$	$\alpha_4$	$\alpha_5$	$\alpha_6$	$\alpha_7$	$\alpha_8$
Tokyo University	0.9238	0.9967	0.9365	1.0227	1.0303	1.0075	0.8385	1.3761

**Figure 4:** Yield locus obtained with Yld2000 criterion for 6016-T4 alloy.

schemes. Furthermore, explicit schemes are more suitable for problems with many elements or nodes, where implicit schemes become computationally expensive.

In this study, full integration shell elements and seven integration points through thickness were used for blank mesh design. The cup drawing process was studied as a quarter model. 3,072 quadratic shell elements were generated for the quarter blank part. The finite element model of the cup drawing process is shown in Figure 3.

In plasticity modeling Yld2000 yield criterion [27] was used for determining material behavior in finite element analyses. The Yld2000-2D yield function was defined as:

$$|X'_1 - X'_2|^m + |2X'_2 + X'_1|^m + |2X'_1 + X'_2|^m = 2\bar{\sigma}^m \quad (\text{MPa}^m) \quad (1)$$

with

$$X'_{1,2} = \frac{1}{2} \left( X'_{xx} + X'_{yy} \pm \sqrt{(X'_{xx} - X'_{yy})^2 + 4X'^2_{xy}} \right) \quad (\text{MPa}) \quad (2)$$

and similar expression with the appropriate double prime indices for  $X''_{1,2}$ : (MPa). The relations giving the components of  $X'$ : (MPa) and  $X''$ : (MPa) in terms of the in-plane components of the Cauchy stress deviator are:

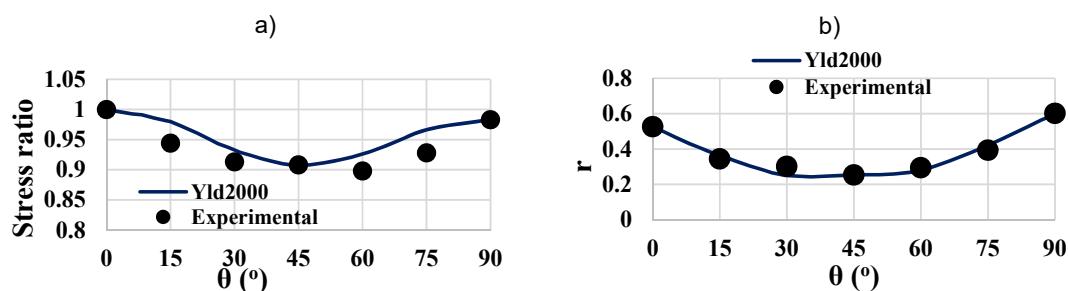
$$\begin{bmatrix} X'_{xx} \\ X'_{yy} \\ X'_{xy} \end{bmatrix} = \begin{bmatrix} \alpha_1 & 0 & 0 \\ 0 & \alpha_2 & 0 \\ 0 & 0 & \alpha_7 \end{bmatrix} \begin{bmatrix} s_{xx} \\ s_{yy} \\ s_{xy} \end{bmatrix} \quad (\text{MPa}) \quad (3)$$

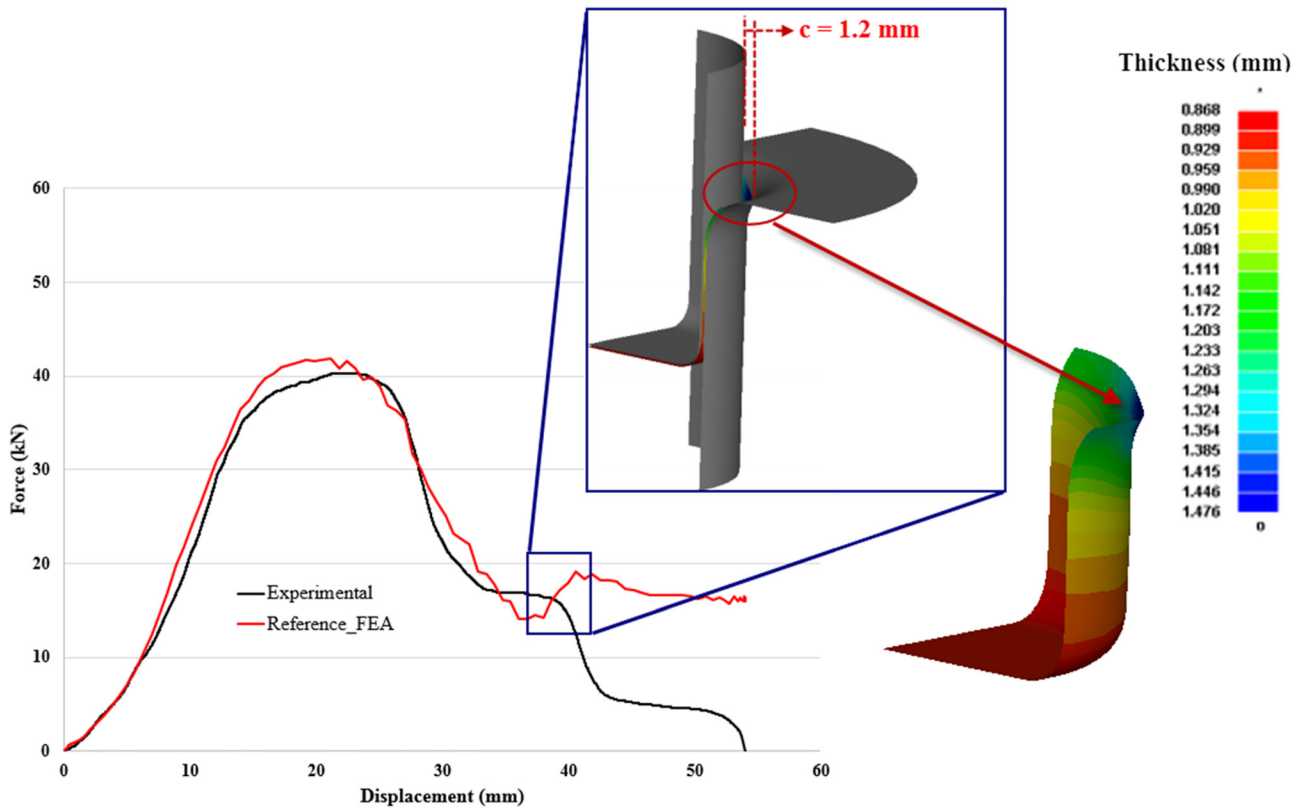
$$\begin{bmatrix} X''_{xx} \\ X''_{yy} \\ X''_{xy} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 4\alpha_5 - \alpha_3 & 2\alpha_6 - \alpha_4 & 0 \\ 2\alpha_3 - 2\alpha_5 & 4\alpha_4 - \alpha_6 & 0 \\ 0 & 0 & 3\alpha_8 \end{bmatrix} \begin{bmatrix} s_{xx} \\ s_{yy} \\ s_{xy} \end{bmatrix} \quad (\text{MPa}) \quad (4)$$

with  $\alpha_j$  (–),  $j$ : 1...8 (–): Independent anisotropy coefficients involved in the formulation of Yld2000-2D [23].

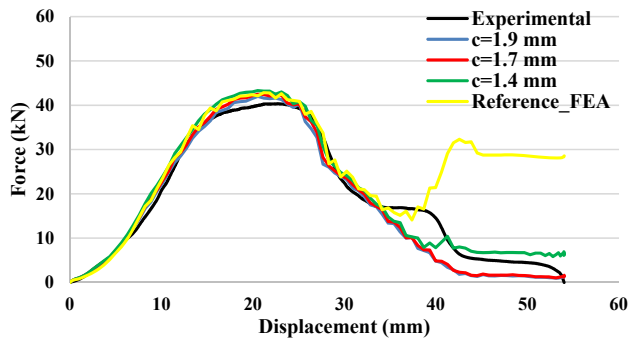
Yield locus and angular variations of stress ratios and Lankford coefficients ( $r$  values) were predicted using the Yld2000 yield criterion for 6016-T4 alloy. Prediction results were compared with the experimental results obtained at Tokyo University. Yld2000 parameters of the 6016-T4 alloy is presented in Table 1. Figures 4 and 5 shows the yield locus and angular variations of stress ratios and Lankford coefficients ( $r$  values) comparisons. As it can be seen from these figures the Yld2000 criterion can accurately define the directionality of stress and Lankford coefficients.

After finite element analyses, a force–stroke curve comparison was obtained to understand the current status of the reference data. The comparison result is given in Figure 6. It is seen that the finite element analyses have good

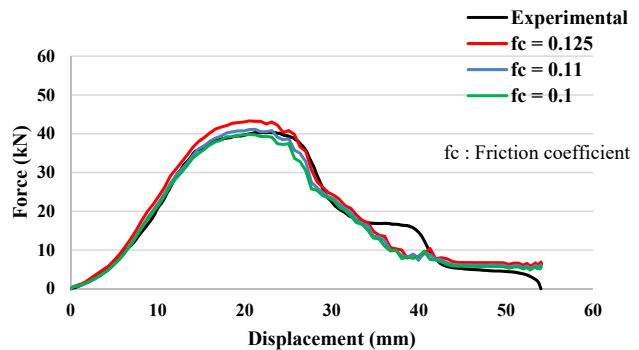
**Figure 5:** Angular variation of, a) stress ratio, b)  $r$  values obtained with Yld2000 plasticity model for 6016-T4 alloy.



**Figure 6:** Force-displacement curve comparison of reference finite element analyses with experimental data.



**Figure 7:** Die clearance 'c' effect on force-displacement curves of cup drawing process.



**Figure 8:** Friction coefficient effect on force-displacement curves of cup drawing process.

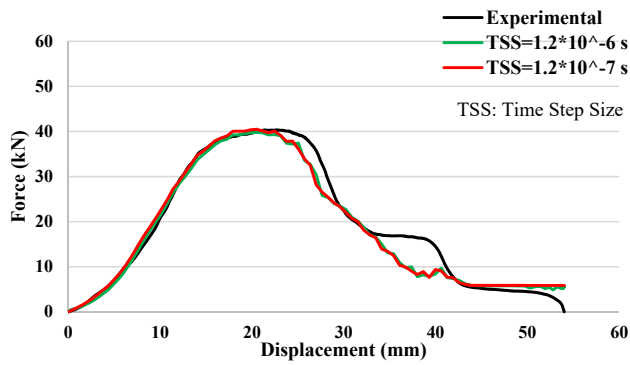
agreement with experimental data until the blank disposes of the blank holder. When flange areas were drawn into the die cavity, sheet thickness became approximately 1.48 mm. However, the clearance between the die and the punch was given as 1.2 mm, so in this stage, thick areas of the blank are stuck in this clearance, and the punch force increases due to this situation.

A parametric study was organized to eliminate this situation. Firstly, die geometry was investigated through die clearance. Die clearance was studied as 1.9, 1.7, and 1.4 mm, and then the finite element analyses were performed with

the same parameters as the reference simulation. It is seen that the die clearance has a strong effect on punch force (Figure 7), and the clearance value of 1.4 mm showed a good agreement with the experimental data, and this value is selected for further finite element analyses.

Still, it can be seen in Figure 7 that maximum force values are overpredicted with different die clearance values. For this reason, the friction situation is addressed to have a better agreement with the experimental data. For this purpose, the friction coefficient is used with three different





**Figure 9:** Time step size effect on force-displacement curves of cup drawing process.

values: 0.125, 0.11, and 0.1. In reference to finite element analyses, the friction coefficient was used as 0.125. Force-displacement curves with different friction coefficients are given in Figure 8. It can be clearly seen that maximum force values decrease when using a lower friction coefficient, and a friction coefficient of 0.1 is in good agreement with the

experiment. For this reason, the friction coefficient is used as 0.1 for further finite element analyses.

It is known that the finite element calculation parameters affect prediction results like process conditions [28]–[30]. For this situation, in the second part of the parametric study, time step size and termination time effects were investigated via force-displacement curves of the cup drawing process. The time step size roughly corresponds to the transient time of an acoustic wave through an element using the shortest characteristic distance [31]. For the shell elements, the time step size can be written by Eq.(5).

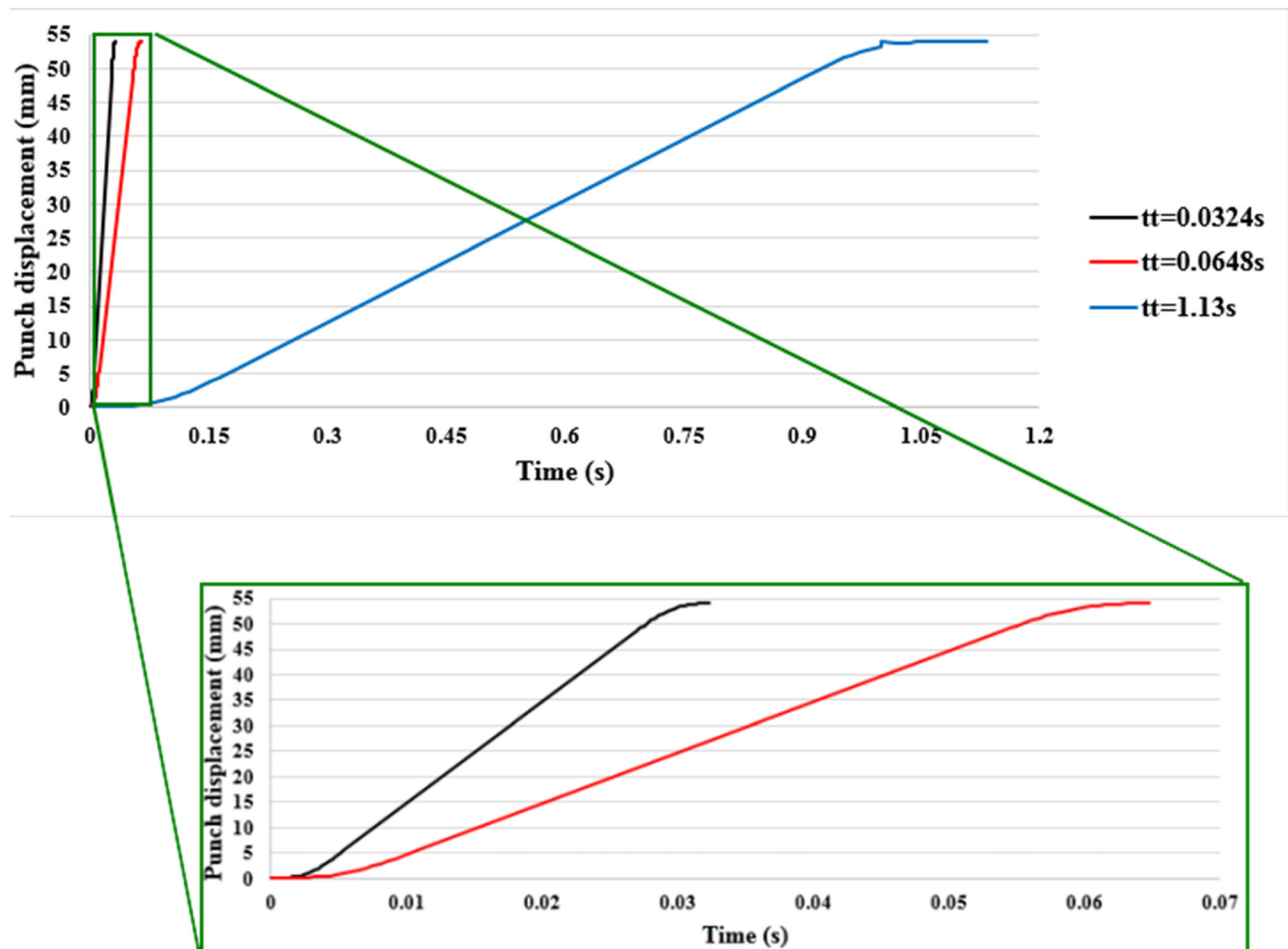
$$\Delta t_e = \frac{L_s}{c} \quad (-) \quad (5)$$

with  $L_s$ : Characteristic length and  $c$ : Sound speed.

Sound speed can be calculated according to Equation (6).

$$c = \sqrt{\frac{E}{\rho(1-\nu^2)}} \quad (\text{mm s}^{-1}) \quad (6)$$

In reference finite element analyses, the time step size was used as 0.0000012 s as a default, and in the parametric study,



**Figure 10:** Punch displacement-time curves for different finite element termination. Time (tt).

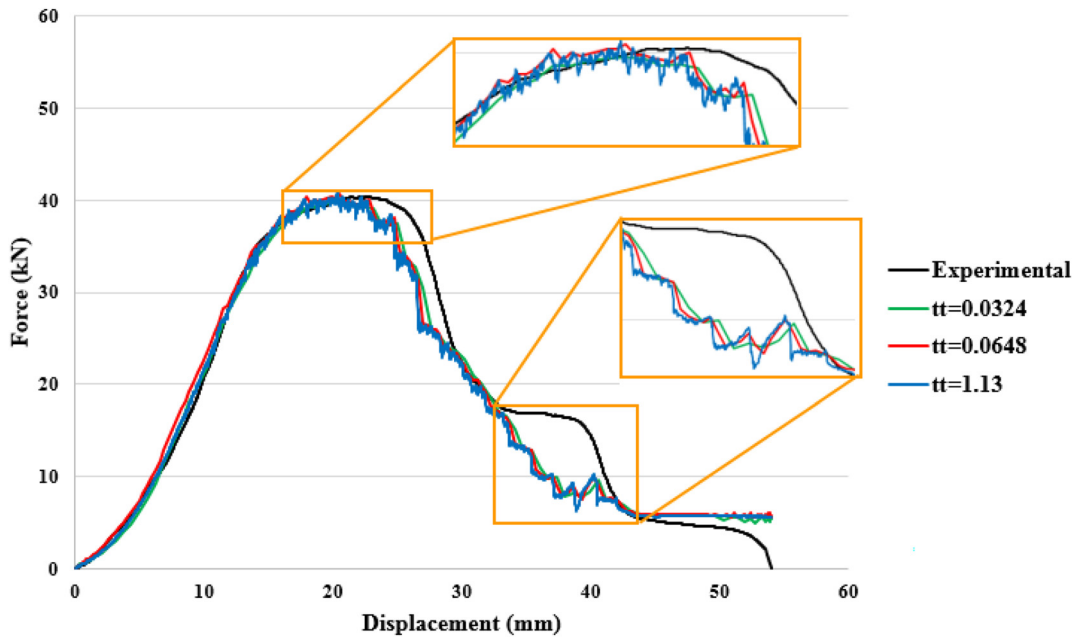


Figure 11: Termination time (tt) effect on force–displacement curves of cup drawing process.

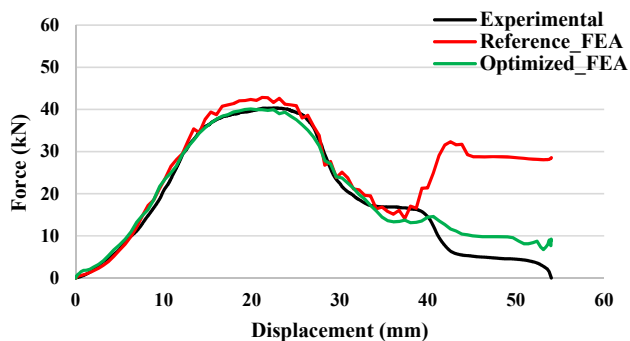


Figure 12: Comparison of force–displacement curves obtained with reference finite element analyses and finite element analyses after parametric study.

0.00000012 s was used to decrease the time step size. Force–displacement curves for different time step size can be seen in Figure 9. It can be seen from the figure that the time step sizes does not have an efficient effect on punch force predictions.

The second variable is chosen as the termination time of the simulation. In reference simulation, punch movement was completed with 0.0324 s. For the parametric study, this time step was used as 0.0648 s and 1.13 s. Punch movement curves can be seen in Figure 10 for different termination times. Finite element analyses were performed for these values, and force–displacement curves are compared in Figure 11. It is seen that the increasing termination time causes a data increase, and the force–displacement curves

show more vibrations. However, there is no influence on punch force values. As a result, 0.0324 s termination time was found suitable for further analyses since it saves an important amount of calculation time.

As a result, the parametric study showed that the die clearance and the friction coefficient have an efficient effect on punch stroke; however, calculation parameters showed poor effort.

## 4 Conclusions

The study aimed to examine the effect of process and calculation parameters on the accuracy of finite element analysis results for cup drawing. Therefore, an application study was conducted using the Esaform-2021 cup drawing benchmark, with the goal of providing insights into how process parameters influence the accuracy of finite element analyses and suggesting ways to develop more realistic models to improve cup drawing predictions' accuracy. Specifically, this study focused on predicting the force–displacement behavior of the 6016-T4 alloy cup drawing process through a parametric study based on process and finite element calculation parameters. As a result, an improved force–displacement curve named “optimized” was obtained and compared to reference results (Figure 12).

Based on the parametric study with plasticity model validation, these results were concluded:

- Die clearance has a significant impact on punch force in finite element analyses. In this study, the material's initial thickness was 0.9 mm, and it thickened by approximately 1.48 mm when flowing into the die cavity (initial clearance was 1.2 mm). This thickening caused an increase in punch force due to the blank stuck. A clearance of 1.4 mm performed well in finite element analyses compared to the experimental results for the cup drawing process used in this study.
- The friction coefficient has a direct effect on punch force. Dry friction ( $\mu = 0.125$ ) and friction coefficients of  $\mu = 0.11$  and  $\mu = 0.1$  were studied to achieve agreement with experimental results. Using lower friction coefficients decreased punch force, and a value of  $\mu = 0.1$  matched the experimental results, particularly for the maximum force value.

The authors also investigated time step size and termination time as finite element calculation parameters. However, it was found that these parameters do not efficiently affect the finite element analysis results. Therefore, the parameters that brought the minimum solution time were specified and used.

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**Informed consent:** Not applicable.

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