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Thermodynamic Modeling of the $\text{CaO-SiO}_2\text{-M}_2\text{O}$ ($\text{M}=\text{K,Na}$) Systems

Abstract: The aim of the present study is the CALPHAD modeling of the systems $\text{CaO-SiO}_2\text{-M}_2\text{O}$ ($\text{M}=\text{K,Na}$) based on a careful review of the available literature data – phase diagram and thermodynamics – as well as own experiments. The heat capacities (C_p) of three compounds, CaSiO_3 , $\text{K}_2\text{Ca}_2\text{Si}_2\text{O}_7$ and $\text{K}_8\text{CaSi}_{10}\text{O}_{25}$ (determined using drop calorimetry), were included in the optimization of the ternary phase diagram $\text{CaO-SiO}_2\text{-K}_2\text{O}$.

Keywords: thermodynamics, phase diagram, modeling, molten slag

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1 Introduction

The aim of the Virtual High Temperature Conversion Processes (VIRTUHCON) project is the theoretical modeling of high temperature conversion processes such as metallurgy and gasification. The thermodynamic properties of molten silicates (slag) are important input quantities for the modeling of phenomena in process engineering and geoscience where SiO_2 (silica) is a prime component. Although the alkaline oxides normally appear in minor quantities, they can significantly change the behavior of the slag properties because of their low melting temperatures thereby considerably lowering the liquidus temperature of the molten oxide mixture. Therefore, information on phase diagram and thermochemistry of alkaline oxide containing systems is required to help scientists in the design or development of new materials and processes. However, experimental difficulties abound in alkaline bearing systems because alkaline oxides are difficult to

handle and prone to surface hydrolysis when exposed to air. CALPHAD modeling is therefore considered a suitable choice to provide phase diagram and thermochemical information where experiments can only be performed with difficulty.

The phase diagram and thermochemical information of the $\text{K}_2\text{O-SiO}_2$ and $\text{Na}_2\text{O-SiO}_2$ systems have already been thermodynamically evaluated in the literature [1–7]. There, the liquid phase was described using the modified quasi-chemical model [8] and the modified associate species model [9]. In the present work, the ionic two-sublattice model [10–11] is applied to describe the liquid phase in these systems as this model allows an adequate representation of the thermodynamic properties for complex liquids such as slag. Furthermore, this model allows coupling a large database for oxides to simple metal systems. A detailed literature review of these two systems can be found in [11], while new assessments of the $\text{K}_2\text{O-SiO}_2$ and $\text{Na}_2\text{O-SiO}_2$ systems were recently carried out by Schmetterer et al. and Zhang et al. [12, 13].

The thermodynamic parameters of the CaO-SiO_2 system have been optimized several times [14–17]. Recently, we performed a survey of literature data for the C_p of the calciumsilicate phases [18] and made a new determination of the C_p of Pseudowollastonite (CaSiO_3 – see Table 1) which was found to be in good agreement with the literature. These results were included in our thermodynamic description of this system.

However, no phase diagram and thermochemical information for the $\text{K}_2\text{O-CaO}$ and $\text{Na}_2\text{O-CaO}$ systems are available so that the thermodynamic descriptions of these two systems had to be based on simple extrapolations of the Gibbs energy functions of the pure oxides compounds.

Literature for the ternary systems is scarce; the key papers for experimental investigations are from Morey et al. [19] for the $\text{K}_2\text{O-CaO-SiO}_2$ system and Morey and Bowen [20] for the $\text{Na}_2\text{O-CaO-SiO}_2$. In their reports the authors provided liquidus temperatures obtained from optical inspection of samples after quenching from various temperatures and reported the existence and composition of several ternary compounds. However, the experiments were mostly confined to the SiO_2 rich part. Six ternary compounds in this $\text{CaO-K}_2\text{O-SiO}_2$ system, CaK_2SiO_4 , $\text{CaK}_4\text{Si}_3\text{O}_9$, $\text{CaK}_8\text{Si}_{10}\text{O}_{25}$, $\text{Ca}_3\text{K}_2\text{Si}_6\text{O}_{16}$, $\text{Ca}_2\text{K}_2\text{Si}_6\text{O}_{15}$

Phase	Thermodynamic parameters (J/mol)
Ca ₂ K ₂ Si ₂ O ₇	$G_{Ca_2K_2Si_2O_7} = -4 \times 10^6 + 1878.85T$ $-296.52202T \ln T - 0.0213315T^2$ $+ 1447659.99T^{-1}$
CaK ₄ Si ₃ O ₉	$G_{CaK_4Si_3O_9} = -3.73 \times 10^5 + 10T$ $+ 2GK2O + 3GSI02 + GCAO$
CaK ₈ Si ₁₀ O ₂₅	$G_{Ca_2K_2Si_2O_7} = -5733236.456 + 1475.356T$ $-1049T \ln T - 9.6487 \times 10^6 T^{-1}$
CaK ₄ Si ₆ O ₁₅	$G_{CaK_4Si_6O_{15}} = -3.93 \times 10^5 + 9.005T$ $+ 2GK2O + 6GSI02 + GCAO$
Ca ₃ K ₂ Si ₆ O ₁₆	$G_{Ca_3K_2Si_6O_{16}} = -4.65 \times 10^5 + 8.04T$ $+ GK2O + 6GSI02 + 3GCAO$
Ca ₂ K ₂ Si ₆ O ₁₅	$G_{Ca_2K_2Si_6O_{15}} = -3.704 \times 10^5 + 10.01T$ $+ GK2O + 6GSI02 + 2GCAO$
Ca ₂ K ₂ Si ₉ O ₂₁	$G_{Ca_2K_2Si_9O_{21}} = -3.72 \times 10^5 + 10.01T$ $+ GK2O + 9GSI02 + 2GCAO$
CaNa ₂ SiO ₄	$G_{CaNa_2SiO_4} = -2.2015 \times 10^5 + 48.85T$ $+ GNA2O + GSI02 + GCAO$
Ca ₃ Na ₈ Si ₅ O ₁₇	$G_{Ca_3Na_8Si_5O_{17}} = -4.93015 \times 10^5 + 70.0025T$ $+ 4GNA2O + 5GSI02 + 3GCAO$
Ca ₂ Na ₂ Si ₂ O ₇	$G_{Ca_2Na_2Si_2O_7} = -3.40009 \times 10^5 + 64.0018T$ $+ GNA2O + 2GSI02 + 2GCAO$
Ca ₂ Na ₂ Si ₃ O ₉	$G_{Ca_2Na_2Si_3O_9} = -3.98009 \times 10^5 + 70.0018T$ $+ GNA2O + 3GSI02 + 2GCAO$
CaNa ₄ Si ₃ O ₉	$G_{CaNa_4Si_3O_9} = -4.54 \times 10^5 + 108.037T$ $+ 2GNA2O + 3GSI02 + GCAO$
Ca ₃ Na ₂ Si ₆ O ₁₆	$G_{Ca_3Na_2Si_6O_{16}} = -4.904 \times 10^5 + 70T$ $+ GNA2O + 6GSI02 + 3GCAO$

Table 1: Thermodynamic parameters of CaO-SiO₂-M₂O (M=K, Na) systems

and Ca₂K₂Si₉O₂₁ were reported by Morey et al. [19]. However, they did not give any structural information in their work. Toropov and Borisenko [21] and Yung et al. [22] indicted the existence of the compound CaK₄Si₆O₁₅ based on X-Ray studies. Recently, the possible existence of CaK₂SiO₄ was checked [23], but the evaluations of the powder diffractograms obtained after synthesis experiments clearly indicated that for a 1:1:1 bulk composition K₂Ca₂Si₂O₇ is the dominant potassium calcium silicate up to the melt formation. There is no thermochemical information available in this ternary system. The CaO-Na₂O-SiO₂ system had been studied first by Morey and Bowen [20] who mentioned the existence of four ternary compounds Ca₃Na₂Si₆O₁₆, Ca₂Na₂Si₃O₉, CaNa₄Si₃O₉, and CaNa₂SiO₄. Segnit [24] had obtained the new compound Ca₃Na₈Si₅O₁₇ and Ca₂Na₂Si₂O₇ in the parts of this ternary system richer in CaO and Na₂O. The compound Ca₈Na₄Si₅O₂₀ had been found by Toropov and Arakelyan [25]. Later, Fedorov and Brodskina [26] considered this phase to be a mixture of a solid solution with Ca₂SiO₄ and CaNa₂SiO₄ instead of an individual compound. The six ternary compounds from the literature were considered in this work. The phase

diagram and thermochemical information is also limited in this ternary system to the work from Morey and Bowen [20]. Further experimental phase diagram data and thermodynamic properties have not been determined until now.

The goal of the present work is to describe the current knowledge about the thermodynamic properties of the M₂O-CaO-SiO₂ (M=K, Na) ternary systems which are constituents of the complex Al₂O₃-CaO-MgO-SiO₂-M₂O (M=K, Na) system. The optimization of these ternary systems is the first step in the estimation of thermodynamic properties and phase diagrams of the subsequent multicomponent systems.

2 Thermodynamic modeling

2.1 Liquid phase

It can be assumed that Ca²⁺, K⁺, Na⁺, O²⁻, SiO₄⁴⁻, SiO₂⁰ and Va⁻ exist in the liquid phase of the CaO-M₂O-SiO₂ (M=K, Na) systems, and that the electric neutrality is maintained depending on the relative amounts of positive or negative ions for a given temperature. The two-sublattice model for the ionic solution suggested by Hillert et al. [10] can be used to express the Gibbs energy of this system. This model utilizes two sublattices, one for cations and the other for anions, neutral species and vacancies. Thus, the formula unit of the CaO-M₂O-SiO₂ (M=K, Na) systems can be expressed as

$$(Ca^{+2}, M^{+1})_P (O^{2-}, SiO_4^{4-}, SiO_2^0, Va^{-})_Q \quad (M=K, Na)$$

where Va⁻ denotes the vacancies. The indices *P* and *Q* represent the mole number of cations and anions of the two sublattices in order to maintain the electric neutrality, as described by Eqs. (1) and (2)

$$P = 2y_{O^{2-}} + 4y_{SiO_4^{4-}} \quad (1)$$

$$Q = y_{M^{+1}} + 2y_{Ca^{+2}} \quad (2)$$

Although this model yields complicated thermodynamic expressions, in practice, all calculations are carried out automatically using thermodynamic software packages such as Thermo-Calc [27]. The Gibbs energy of the liquid in this system is given by Eq. (3)

$$G_m = \sum \sum y_i y_j {}^0G_{ij} + Q \sum y_k {}^0G_k + PRT \sum y_i \ln y_i + QRT (\sum y_j \ln y_j + \sum y_k \ln y_k) + {}^F G_m \quad (3)$$

where i is a cation, Ca^{+2} or K^{+1} or Na^{+1} , j is an anion, O^{-2} or SiO_4^{-4} , and k is neutral as in SiO_2^0 , ${}^E G_m$ represents excess Gibbs energy. The last term, ${}^E G_m$, can be expressed by Eq. (4)

$${}^E G_m = \sum_{v=0}^{v=s} y_i y_j y_k \sum_{v=0}^{v=n} {}^v L_{i,j,k} (y_j - y_k)^v + \sum_{v=0}^{v=n} y_i y_j y_k y_l {}^v L_{i,j,k,l} (y_i - y_j)(y_k - y_l) \quad (4)$$

where i, j, k and l is a cation or anion or neutral as in SiO_2^0 . $L_{i,j,k}$ and $L_{i,j,k,l}$ are the interaction parameters between two sub-lattices that were optimized in this work.

2.2 Solid phases

In the CALPHAD technique, the thermodynamic properties of each solid phase are represented by the parameters S_{298} (the entropy of the solid at 298.15 K), $C_p(T)$ (the heat capacity of the solid) and ΔH_{298} (the change in enthalpy of the solid) where

$$C_p = a + bT + cT^{-2} \quad (5)$$

The Gibbs energy values are given in relation to the enthalpy of selected reference states for the elements at 298.15 K according to Eq. (6). This state is denoted by SER (Stable Element Reference)

$${}^0 G - H^{SER} = A + B/T + CT + DT \ln T + ET^2 + \dots \quad (6)$$

with the parameters A, B, C, D and E being optimized, i.e. determined in such a way that the calculated phase diagram matches the experimental information.

In the current work, the Gibbs functions of three compounds $K_2Ca_2Si_2O_7$ and $K_8CaSi_{10}O_{25}$ were based on our own heat capacity data from drop calorimetry. The thermodynamic parameters of other compounds were assessed based on the phase relations from the work of Morey et al. [19]. So far, the interpretation of the results concerning the existence and formation of certain phases had to rely exclusively on the only available phase equilibrium study of the K_2O - CaO - SiO_2 ternary system that was published 80 years ago by Morey et al. [19]. The optimization of the CaO - M_2O - SiO_2 ($M=K, Na$) systems was carried out using the PARROT module of the Thermo-Calc software [27]. This module works by minimizing the square sum of the differences between experimental and calculated values. In the

optimization procedure, each set of experimental data was given a certain weight. The weights were changed systematically during the optimization until most of the experimental data could be accounted for within the claimed uncertainty limits.

The parameters for the liquid phase were first optimized using the experimental liquidus temperatures. The thermodynamic parameters of the solid compounds were assessed next by using the phase diagram data and the heat capacities. All of the parameters were finally evaluated together to give a reasonable description of these systems.

The thermodynamic parameters from the optimization are listed in Table 1.

3 Results and discussions

Seven ternary compounds were included in the CaO - K_2O - SiO_2 system. The Cp data from our own measurement for the compounds $K_2Ca_2Si_2O_7$ and $K_8CaSi_{10}O_{25}$ were considered in this optimization. The calculated liquidus temperatures are shown in Fig. 1, which is in good agreement with the experimental results from Morey et al. [19] in the respective composition range. It has, however, to be noted that the K_2O -rich part is extrapolated and not supported by experimental data. Comparing our calculated results with the experimental results, it can be found that there are differences between the experimental data [19] and

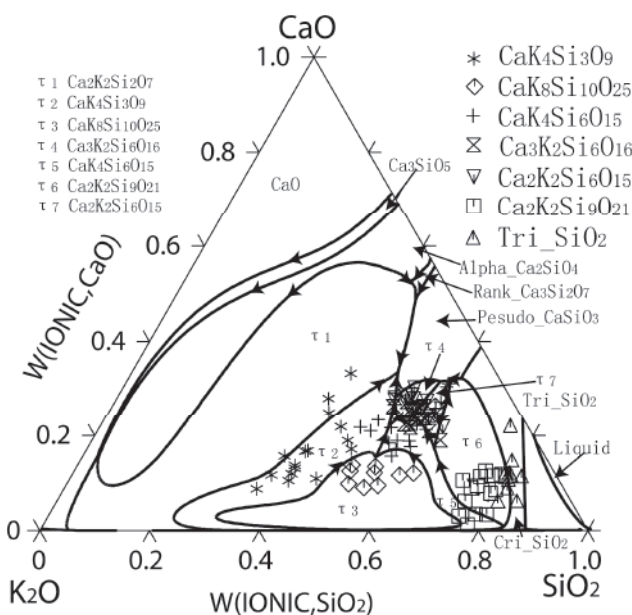


Fig. 1: Calculated phase diagram of CaO - K_2O - SiO_2 system

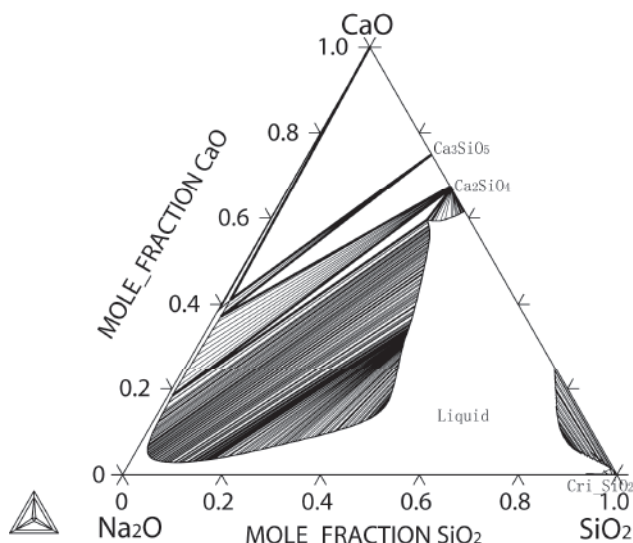
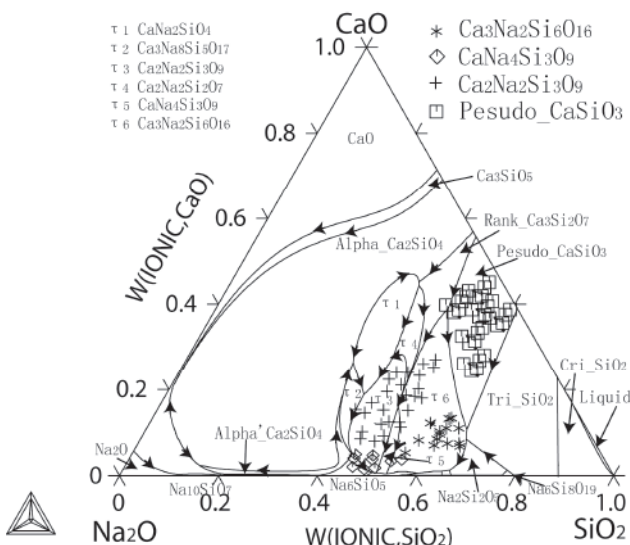


Fig. 4: Calculated isothermal section at 2000 K in CaO-Na₂O-SiO₂ system



cluded in the calculation. Figure 4 shows the calculated isothermal section at 2000 K, where the liquid miscibility gap close to the SiO_2 corner extends into the ternary system. With increasing temperature the boundary of the miscibility gap will shift toward the CaO-SiO_2 binary system. The calculated invariant reactions on this system were shown in Table 2. The isothermal section at 1273 K is given in Fig. 5, where five ternary compounds, $\text{Ca}_2\text{Na}_2\text{Si}_2\text{O}_7$, $\text{CaNa}_2\text{SiO}_4$, $\text{Ca}_2\text{Na}_2\text{Si}_3\text{O}_9$, $\text{CaNa}_4\text{Si}_4\text{O}_9$, $\text{Ca}_3\text{Na}_2\text{Si}_6\text{O}_{16}$, are stable. The calculated vertical section ($\text{Na}_2\text{SiO}_4\text{-CaSiO}_3$) of this ternary system is given in Fig. 6 and shows good agreement between the present calculation and the measurements [20].

4 Conclusions

Based on the previous assessments and our own optimization of the sub-binary systems, the thermodynamic properties and phase equilibria of the $\text{CaO-M}_2\text{O-SiO}_2$ ($\text{M}=\text{K, Na}$) systems have been assessed. The two-sublattice model for ionic solutions can be used to describe these two ternary systems. In addition, the experimentally determined heat capacities of three solid compounds were included in the dataset. Reasonable agreement between calculated and experimental data has been achieved.

Nevertheless, the need of more experimental information for the phase diagrams and thermodynamic properties is desirable in order to have more detailed and confident phase diagram description. Experimental work in

Reaction	Type	T/K	Ref
$L + \text{Ca}_2\text{K}_2\text{Si}_2\text{O}_7 \rightleftharpoons \text{Pesudo_CaSiO}_3 + \text{CaK}_4\text{Si}_3\text{O}_9$	U	1073	[19]
		1061	This work
$L \rightleftharpoons \text{Pesudo_CaSiO}_3 + \text{CaK}_4\text{Si}_3\text{O}_9 + \text{Ca}_3\text{K}_2\text{Si}_6\text{O}_{16}$	E	1050	[19]
		1049	This work
$L + \text{Pesudo_CaSiO}_3 + \text{Ca}_2\text{K}_2\text{Si}_6\text{O}_{15} \rightleftharpoons \text{Ca}_3\text{K}_2\text{Si}_6\text{O}_{16}$	P	1273	[19]
		1257	This work
$L + \text{CaK}_8\text{Si}_{10}\text{O}_{25} \rightleftharpoons \text{CaK}_4\text{Si}_3\text{O}_9 + \text{CaK}_4\text{Si}_6\text{O}_{15}$	U	1170	[19]
		1157	This work
$L + \text{Ca}_2\text{K}_2\text{Si}_9\text{O}_{21} \rightleftharpoons \text{Ca}_2\text{K}_2\text{Si}_6\text{O}_{15} + \text{CaK}_4\text{Si}_6\text{O}_{15}$	U	1098	[19]
		1065	This work
$L + \text{Ca}_2\text{K}_2\text{Si}_6\text{O}_{15} \rightleftharpoons \text{Ca}_3\text{K}_2\text{Si}_6\text{O}_{16} + \text{CaK}_4\text{Si}_6\text{O}_{15}$	U	1223	[19]
		1234	This work
$L + \text{Pesudo_CaSiO}_3 \rightleftharpoons \text{Ca}_3\text{Na}_2\text{Si}_6\text{O}_{16} + \text{Tri_SiO}_2$	U	1323	[20]
		1354	This work
$L + \text{Ca}_2\text{Na}_2\text{Si}_2\text{O}_7 \rightleftharpoons \text{Ca}_3\text{Na}_2\text{Si}_6\text{O}_{16} + \text{Ca}_2\text{Na}_2\text{Si}_3\text{O}_9$	U	1423	[20]
		1417	This work
$L + \text{Ca}_3\text{Na}_2\text{Si}_6\text{O}_{16} + \text{Ca}_2\text{Na}_2\text{Si}_3\text{O}_9 \rightleftharpoons \text{CaNa}_4\text{Si}_3\text{O}_9$	P	1157	[20]
		1170	This work

Table 2: Invariant reactions of CaO-SiO₂-M₂O (M=K, Na) systems

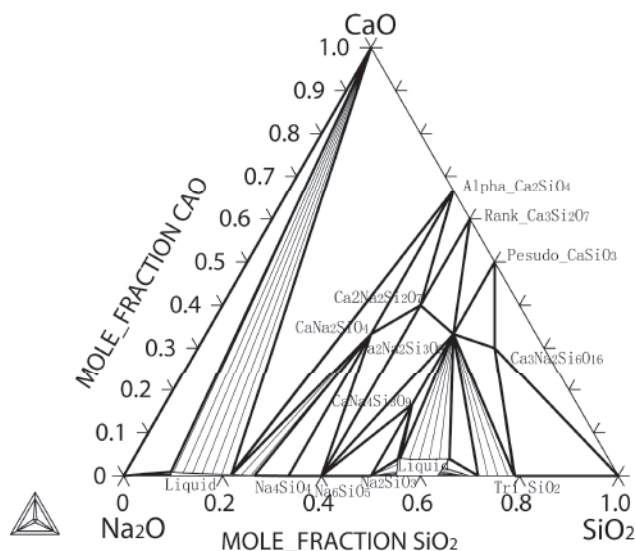


Fig. 5: Calculated isothermal section at 1273 K

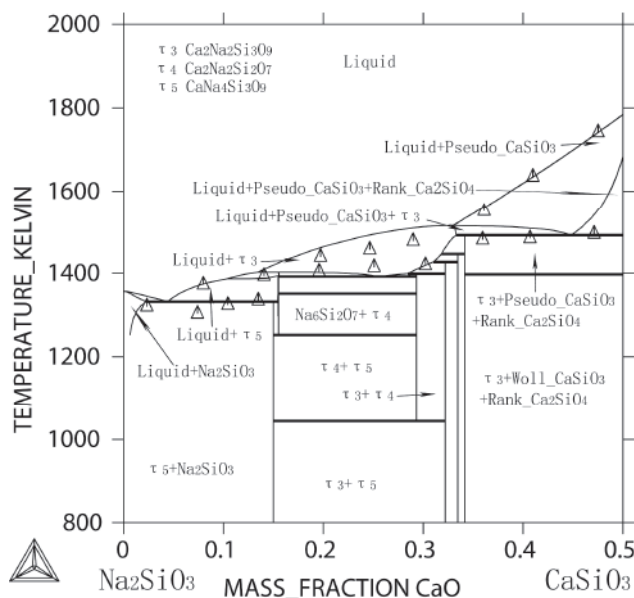


Fig. 6: Calculated vertical section (Na₂SiO₃-CaSiO₃)

the CaO-M₂O-SiO₂ (M=K, Na) systems is therefore strongly encouraged.

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