Original article

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Wood-adhesive bond loaded in mode II: experimental and numerical analysis using elasto-plastic and fracture mechanics models

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Abstract: The goal of the study was to analyze fracture properties of adhesive bond using a three-point endnotched flexure test and the compliance-based beam method. Critical strain energy release rates (G_{Uc}) and cohesive laws were obtained for adhesive bonds made of European beech (Fagus sylvatica L.) and adhesives such as EPI, MUF, PRF and PUR. The experiments were assisted with FE analyses employing three different material models of wood: elastic (Elas), symmetric elasto-plastic (EP) and elasto-plastic with different compressive and tensile yield stresses parallel to fiber (EP+). The highest mean G_{IIC} was achieved for PUR (5.40 Nmm⁻¹) and then decreased as follows: 2.33, 1.80, 1.59 Nmm⁻¹ for MUF, EPI, and PRF, respectively. The failure of bondline was brittle and occurred at bondline for EPI, MUF and PRF, and ductile and commonly occurring in wood for PUR adhesive. The FE simulations employing cohesive models agreed well with the experimental findings for all adhesives. FE model with Elas material was found accurate enough for EPI, MUF and PRF adhesives. For PUR adhesive, the model EP+ was found to be the most accurate in prediction of maximal force. The impact of friction between lamellas may be up to 4.2% when varying friction coefficient from 0 to 1. The impact of the grain angle distortion (α) with respect to longitudinal specimen axis showed its high influence on resulting stiffness and maximal force. It was found that three-point endnotched test is suitable for EPI, MUF, and PRF, while it is less appropriate for a bond with PUR adhesive due to notable plastic behavior.

Keywords: adhesive bond; beech wood; cohesive law; elasto-plastic material; mode II; strain energy release rate.

1 Introduction

Adhesive bonding of wood in any shape and size is necessary for production of modern wood products. For the production of high-performance wood composites, a fundamental understanding of adhesive bond behavior and properties, including involved materials, is essential (Stoeckel et al. 2013). Mechanical tests of adhesive materials are primarily made on a macroscopic scale (e.g., following EN 302-1 2013), but microscopic investigations also bring important findings about adhesive bond, especially when coupled with X-ray μ CT (McKinley et al. 2018). Adhesive-wood complex is a very complicated mechanical system where many local events such as non-uniform cracking in adherend/adhesive, fiber bridging, etc. occur and, therefore, use of full-field technique such as digital image correlation (DIC) is advantageous when analyzing strains and crack openings around the bond area (Brault et al. 2013; Kamke et al. 2014; McKinley et al. 2019). An adhesive bond between adherents is strongly affected by the quality of manufacturing, which, consequently, significantly affects the physical properties of the bond and its service life in a material or construction. To investigate mechanical performance of adhesive bonds, lap shear test is often employed to reveal the basic properties such as shear strength of wood-adhesive complex. Adhesive bond can have similar and higher bearing capacity and stiffness to bonds using dowels connecting lamellas in laminated beams (Jelušič and Kravanja 2018). Another important property of adhesive bond is the fracture energy that needs

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to be spent on adhesive bond to initiate and propagate the crack in wood-adhesive complex. Fracture energy, specifically strain energy release rate (G), can be studied in three fundamental modes: mode I (tension), mode II (in-plane shear) and mode III (out-of-plane shear) as well as in mixed modes (Anderson 1995).

In the last two decades, the measurement of G in mode II (G_{II}) has undergone a big development from simple analytical models, over superposition, to models considering crack tip openings and compliance-based methods (Arrese et al. 2010; Wang and Qiao 2004; Yoshihara 2005). Models including crack propagation phenomena are most accurate because of their direct relation to strain energy release. This approach was successfully proved for both synthetic and wood-based composites (Matsumoto and Nairn 2009: Wang et al. 2009) and modified wood (Kutnar et al. 2008). Mode II fracture is often tested in bending by employing end-notched flexural tests (ENF), either in three-point (3ENF) or four-point (4ENF) schemes, or so-called end loaded split (ELS) tests (Silva et al. 2007). All reveal comparable and reliable data if certain qualitative measurement conditions and sample dimensions, such as span-to-height ratio, are met (Schuecker and Davidson 2000; Yoshihara 2001). Yoshihara and Ohta (2000) found that fracture properties of wood are dependent on a ratio of initial crack length and half span, which has to be considered in experimental designs. De Moura et al. (2006) employed a so-called equivalent crack length approach (ECLA) and incorporated it into the compliancebased beam method (CBBM). This combination was shown to be advantageous because it did not require tracking of crack propagation, which can be conveniently derived directly from the current compliance. Also, using Iosipescu specimen geometry and Arcan test was successfully demonstrated to reveal fracture properties of orthotropic materials (Khansaria et al. 2019; Murata et al. 2017).

Use of ECLA on pine wood was shown by Silva et al. (2006), who also developed the finite element (FE) model of crack propagation for wood in mode II that was successfully verified by ECLA. For medium density fiberboard, ECLA shows that fracture toughness in mode II continuously increased during crack propagation (Yoshihara 2010). Because of its relative ease, ENF in combination with ECLA is well suited for analysis of wood-adhesive bonds, too (Xavier et al. 2011), and for determination of cohesive zone models of a material (Silva et al. 2014; Xavier et al. 2014) or for adhesive bonds of composite materials (Fernandes et al. 2013). Cohesive laws are especially important as input data in numerical modeling of composite materials and structures. Using DIC and FEM may conveniently provide data enabling separation of mode I and mode II without considering local elastic mechanical properties as shown in

Meite et al. (2013). More recently, Clerc et al. (2019) showed a simplified four-point ENF test to examine G_{II} for the adhesive bond of wood and PRF and one-component PUR adhesives without the need for DIC. They showed that performance of all adhesive bonds has similar behavior under quasi-static loading in mode II.

In the last two decades, environmental aspects and considerations have pushed forestry to plant more broadleaved species that, consequently, initiated innovations in development of wood-based composites (WBCs) for glued timber structures (Vallée et al. 2017). Therefore, WBCs, such as Glued-Laminated Timber (GLT), cross-laminated timber (CLT) and laminated veneer lumber (LVL), made from various hardwoods were developed, including hybrid softwood-hardwood compositions (Fortuna et al. 2019: Franke 2016: Pollmeier 2019: Tapia and Aicher 2018). Due to their advantageous properties, they can replace steel elements (e.g., trusses). Therefore, knowledge about mechanical performance of adhesive bond with hardwoods, including fracture properties, is necessary to utilize its potential in timber structures as well as to increase the use of local raw materials that will be crucial for next generations.

The general goal of the study was to provide more insight into fracture properties of adhesive bond for beech wood glued by various adhesives loaded in mode II. The specific objectives are: (i) to carry out 3ENF tests of adhesive bonds with Emulsion Polymer Isocyanate (EPI), Melamine-Urea Formaldehyde (MUF), Phenol-Resorcinol Formaldehyde (PRF) and Polyurethane (PUR) adhesives: (ii) to compute strain energy release rate of adhesive bond using ECLA and DIC data; (iii) to assess whether 3ENF tests are suitable for all the tested adhesives; (iv) to develop and validate finite element model of the test including contact and cohesive zone model; (v) to assess whether elastoplastic material models of wood bring higher accuracy into FE modeling of crack growth for given adhesives, and (vi) to perform FE sensitivity analyses to examine an influence of friction and fiber angle on the outputs of 3ENF test.

2 Materials and methods

European beech wood (Fagus sylvatica L.) was used to prepare all the samples for testing. The samples were conditioned and submitted to 3ENF test. All tests were accompanied with a stereoscopic system to obtain optical data about the displacement slip around the crack tip (w) that was calculated by DIC later on.

2.1 Test specimens

Test specimens were cut from a defect-free board of European beech by cutting with standard band and circular saws. For the 3ENF test, the specimens were prepared with dimensions of $17 \times 20 \times 500 \text{ mm}^3$ in radial (R), tangential (T) and longitudinal (L) directions, respectively, according to Yoshihara (2001) as orthotropic blocks and with the necessary span-to-height ratio to induce stable crack propagation and insignificant plastic deformation due to contact with supports and loading head (Figure 1). An artificial crack of length ≈ 182 mm was introduced in *L* direction at the end of the specimen across the whole width of the specimen. All the specimens were weighed and dimensionally measured prior to the mechanical testing and without crack introduced. Test groups were defined as follows: (i) bond with EPI adhesive (Advantage EP-915 FS); (ii) bond with MUF adhesive (Prefere 4535); (iii) bond with PRF adhesive (Cascosinol 1711 with hardener 2520); and (iv) bond with PUR adhesive (PURBOND PR 3105). Lamellas were bonded using the recommended amount, pressure, time and temperature (20 °C) for particular adhesive as follows: EPI – 400 g/m², 1.4 MPa, 120 min; MUF – 460 g/m², 1.4 MPa, 270 min; PRF – 535 g/m², 1.0 MPa, 240 min; PUR - 790 g/m², 1.2 MPa, 120 min.

2.2 Physical testing

3ENF tests were performed on a universal testing machine (UTM) Zwick/Roell Z050 equipped with a 50 kN load cell; the load rate was set to 3 mmmin⁻¹ (Figure 1b). A deflection of the specimen was measured using cross-head of the UTM. The 3ENF provided force-deflection data that were further processed using CBBM and ECLA to obtain fracture properties. Before testing, Teflon paper was inserted into the crack to reduce friction between lamellas. At the side of the samples, a stochastic black-and-white speckle pattern was applied before testing to create the area of interest (AoI) for later computation of displacement slip using DIC (Figure 1a). All 3ENF tests were recorded at a 2 Hz acquisition rate by means of an optical stereo-vision system consisting of two 9MPx CCD cameras focusing on one side of the AoI. The optical system was synchronized with the UTM. The images were further processed in 3D-DIC software Aramis 2016 (GOM Inc.) to obtain the full-field displacements and compute the strains over the AoI. The analysis used a subset size of $27 \times 27 \text{ px}^2$ and a step size of 3 px. Postprocessing of the DIC results provided the displacement slip (w) that was obtained from two points at the introduced crack tip, one above and one below the assumed neutral axis (Figure 1a). The displacement slip is calculated from $w_{II} = |u^+ - u^-|$, where u^+ is for the upper component, u^- is for the lower component and both are in horizontal directions. After removing invalid measurements, such as for weakly bonded specimens, the total count was 17, 19, 16 and 20 specimens for EPI, MUF, PRF and PUR adhesive, respectively.

2.3 Calculation of strain energy release rate

The theoretical derivation of the strain energy release rate (G_{II}) by 3ENF and equivalent crack length (a_{eqv}) has been described by Yoshihara (2010), and Fernandes et al. (2013), so it is omitted here only for principal steps. The ECLA procedure does not require crack length monitoring during the test and leads to direct derivation of G_{II} respecting Irwin-Kies equation, which is for strain energy release rate as follows:

$$G_{\rm II} = \frac{9P^2 a_{eqv}^2}{16b^2 h^3 E_f} \tag{1}$$

where P is force (N), a_{eav} is equivalent crack length (m), b and h are specimen width and height (m) respectively, E_f is flexural elastic modulus. The main advantage of such a data reduction scheme is that the *R*-curve, i.e., $G_{II} = f(a_{eqv})$, can be obtained solely from the forcedeflection (P/δ) curve. To obtain the G_{II} w_{II} curve, the procedure shown in Xavier et al. (2014) was followed. To derive the cohesive law, the G_{II} - w_{II} curve was truncated at the beginning of the steady-state crack propagation (i.e., at maximal force). The truncated G_{II} - w_{II} curve was then differentiated to obtain the cohesive law in mode II. For this purpose, a continuous logistic function O(t) (Eq. (2)) was used to approximate the data points in the reconstruction of the fracture cohesive law. The logistic fit (Q) searched for parameters t, R and α with lowest residuals according to:



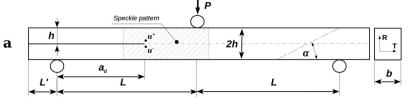


Figure 1: (a) Scheme of sample geometry for 3ENF test with marked AoI for DIC analysis and two points (u^+, u^-) for obtaining displacement slip; L = 230 mm, L' = 20 mm, $a_0 = 182 \text{ mm}, b = 17 \text{ mm}, h = 10 \text{ mm}, \alpha \text{ is}$ fiber angle, R and T denote radial and tangential directions, respectively. The solid line represents crack, the dashed line represents adhesive bond. (b) Experimental setup at universal testing machine including stereovision set accompanied with lights.

$$Q = \frac{Q_{\inf}}{1 + e^{-\alpha \cdot \{t - R\}}}$$
 (2)

where Q is the logistic function, Q_{\inf} is curve maximum, t is quasitime, R is symmetric inflection point, α is time decay constant. Once the continuous function of $G_{II}(w_{II})$ was obtained, the G_{II} was differentiated to obtain cohesive law as follows:

$$\sigma_{II} \frac{\partial G_{II}}{\partial W_{II}} \tag{3}$$

where σ_{II} is stress (Pa) and w_{II} is displacement slip (m). Above mentioned calculations were made on an averaged force-deflection (P/δ) curve. The average P/δ curve was obtained by calculating arithmetic mean P/δ curve from all specimens in the group. Average curve was subsequently fitted by polynomial of 6th degree, which resulted in representative P/δ curve for each group. These curves were further processed to calculate G_{II} and critical strain-energy release rate (G_{IIc}). To examine the differences between studied group mean values, single and multiple one-way analysis of variance test (one-way ANOVA) was used, assuming significance level of 0.05. The multiple 1way ANOVA was made using 'multcompare' function. This test provided answers whether adhesive groups differ in terms of $P_{\rm max}$ and δ . Postprocessing, statistical analyses and other calculations were performed in Matlab 2014b (Mathworks Inc.).

2.4 Numerical modeling

The physical test carried out at UTM was modeled using finite element method (FEM) implemented in software Ansys 19.1 R1 (ANSYS Inc., USA). The 3D sample and boundary conditions reflected the physical test at UTM, so the geometry included the sample, steel supports and loading head (Figure 2). The wood material was modeled using quadratic finite element SOLID95, and the adhesive bond was modeled using cohesive zone model (CZM) and finite element IN-TER204. The traction-separation behavior in CZM was modeled using bilinear function, and the G_{II} for this function was taken as a mean value from the measurement for given adhesive. Lamellas below and above the introduced crack were covered by quadratic contact elements (CONTA170 and TARGE174) to simulate their interaction during the bending test. This contact pair was modeled as flexible-to-flexible. The contact of wood with steel supports and loading head was modeled as rigid-to-flexible, so deformation of steel parts was neglected. The element size was set to 3 mm in longitudinal direction, but around supports and load head, the FE mesh was refined. Element size of 2 mm was set thickness-wise, so each lamella consisted of five elements in thickness. The total number of elements/nodes, including contact and cohesive ones, was 18000/55366. After validation of the FE model based on the comparison with experimentally obtained data, FE sensitivity analyses were performed to analyze an influence

of: (i) friction coefficient between wooden lamellas (μ_{WW}) by varying it from 0 to 1; (ii) fiber angle with respect to the longitudinal axis of the specimen (α) from 0° to 18°; (iii) fiber angle with respect to the cross-section axes from 0° to 90°. The sensitivity analysis was performed to examine the impact of these three parameters on resulting P/δ curves, namely stiffness and $P_{\rm max}$.

Within the FE analyses, three material models of beech wood (Table 1) were employed: (i) orthotropic elastic model (Elas); (ii) orthotropic elasto-plastic model with the same compression and tension yield stresses (EP) and (iii) orthotropic elasto-plastic model with different compression and tension yield values (EP+). The first two models were taken from Milch et al. (2016). The third one was developed based on the second model using a procedure that aimed to extend the difference between compression and tension yield values while preserving Hill plasticity conditions (Hill 1983). The coefficient of friction between steel supports, loading head and wood was set constant to $\mu_{sw} = 0.33$, and the same value was used for wood-wood interaction between wooden lamellas (μ_{ww}), except for analysis of impact of μ_{ww} on resulting P/δ response.

3 Results and discussion

3.1 End-notched flexural tests

The analytical calculation of strain energy release rate (G_{II}) follows the equivalent crack length approach (ECLA) for determination of the resistance curve (R-curve) that is explicitly determined from the experimental forcedisplacement (P/δ) curves (Figure 3). Figure 3 shows that slopes of the elastic zone for all samples is more or less within the same range no matter what adhesive was used; the scatter in stiffnesses may be explained by natural variability of wood properties rather than the type of adhesive. Mean values and standard deviations (in brackets) for flexural stiffnesses (E_f) , as calculated according to Eq. (3) in Silva et al. (2014), are 16.1 GPa (251 MPa), 15.6 GPa (563 MPa), 19.0 GPa (434 MPa) and 16.9 GPa (327 MPa) for EPI, MUF, PRF, and PUR adhesive, respectively. Multiple one-way ANOVA test for E_f revealed that all groups do not have significantly different means (at $\alpha = 0.05$). The moisture content (MC) level of all groups was also proved as statistically equal using an ANOVA test and was in a range of 10.5-11.0%; the same holds true for the density having mean values between 705 and 728 kg/m³. These

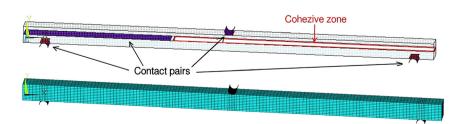


Figure 2: Geometrical and finite element model of the 3ENF test.

Table 1: Material models of beech wood used in FE simulations (moisture content 12%).

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Elas
                                                    E_L = 13439, E_R = 1880, E_T = 1031, G_{LR} = 1608, G_{RT} = 460, G_{LT} = 1059 [MPa]
                                                    v_{LR} = 0.073, v_{RT} = 0.360, v_{LT} = 0.043 [-]. Taken from Milch et al. (2016).
EP (MPa)
                                                   Elas, \sigma_{L,Te} = \sigma_{L,Co} = 47.5, \sigma_{R,Te} = \sigma_{R,Co} = 9.49, \sigma_{T,Te} = \sigma_{T,Co} = 8.11, E_{L,Te,Tan} = E_{L,Co,Tan} = 10.39, E_{R,Te,Te,Tan} = E_{L,Te,Te,Tan} = 10.39, E_{R,Te,Te,Tan} = E_{L,Te,Te,Tan} = 10.39, E_{R,Te,Te,Te,Tan} = 10.39, E_{R,Te,Te,Te,Tan} = 10.39, E_{R,Te,Te,Te,Tan} = 10.39, E_{R,Te,Te,Te,Te,Tan} = 10.39
                                                    _{Tan} = E_{R,\ Co,\ Tan} = 22.36, E_{T,\ Te,\ Tan} = E_{T,\ Co,\ Tan} = 14.38, E_{LR,\ Tan} = 16.08, E_{RT,\ Tan} = 7.61, E_{LT,\ Tan} = 10.59, \sigma_{LR} = 12.6, \sigma_{RT} = 14.2, \sigma_{LT} = 12.6
                                                    Taken from Milch et al. (2016).
EP+
                                                    Elas, \sigma_{L,Te} = 114, \sigma_{L,Co} = 47.5, \sigma_{R,Te} = 8.03, \sigma_{R,Co} = 9.49, \sigma_{T,Te} = 8.59, \sigma_{T,Co} = 8.11, E_{L,Te},
(MPa)
                                                    T_{Tan} = 0.001, E_{L, Co, Tan} = 10.39, E_{R, Te, Tan} = 0.001, E_{R, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Co, Tan} = 22.36, E_{T, Te, Tan} = 0.001, E_{T, Te, Te, Tan} = 0.001
                                                    T_{AB} = 14.38, E_{LR, T_{AB}} = 16.08, E_{RT, T_{AB}} = 7.61, E_{LT, T_{AB}} = 10.59, \sigma_{LR} = 12.6, \sigma_{RT} = 14.2, \sigma_{LT} = 12.6
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 E_i is normal elastic modulus, G_{ij} is shear elastic modulus, v_{ij} is Poisson's ratio, $\sigma_{i,Te}$ is yield stress in tension, $\sigma_{i,Ce}$ is yield stress in compression, σ_{ij} is shear yield stress, $E_{i, Te, Tan}$ is normal tangent modulus in tension, $E_{iCo, Tan}$ is normal tangent el. modulus in compression, $E_{ij, Tan}$ is shear tangent el. modulus. Indices i and j characterize anatomical directions L, R, and T. Elas is orthotropic elastic model, EP orthotropic elasto-plastic with same tension and compression behavior, and EP+ is orthotropic elasto-plastic with different behavior in compression and tension parallel to fiber.

results imply that adhesive type did not influence mean E_f for the groups. Further, the highest maximal force (P_{max}) and maximal deflection at P_{\max} (δ_{\max}) was achieved for PUR adhesive that also possesses significant plastic region between yield point and P_{max} . This fact implies that PUR group has the highest apparent fracture toughness (i.e., area under the P/δ curve), which can be attributed to adhesive properties having a larger range of elastic and plastic deformation compared to other studied adhesives. On the other hand, EPI and PRF adhesives showed the most brittle-like behavior because deflection at P_{max} is lowest, so they would likely have the lowest apparent fracture toughness among studied adhesives.

Variability of P_{max} and δ_{max} for all adhesive groups is shown in the box plots in Figure 4. As seen in the EPI, MUF and PRF are more alike, contrary to PUR that has a significantly higher median value (red line in box plot). A oneway ANOVA test for adhesive groups revealed the same findings for both P_{max} and δ_{max} . For both physical quantities, significant differences between mean values were found only between PUR and all other adhesives ($\alpha = 0.05$). This phenomenon can be attributed to both higher elastic and plastic capacity of adhesive and plastic deformation that occurred in wood due to bending. PUR adhesive belongs with the elastomeric adhesives that show rigidity comparable to other used adhesives, but it also shows higher flexibility due to the aliphatic portions of the polymer, which could contribute to this behavior (Troughton 2009). Martins et al. (2019) examined the same groups of adhesives as in the presented study, but they did so only in terms of shear strength according to EN 14080. Their results showed very similar shear strengths and force vs. deflection diagrams in terms of both elastic and plastic ranges of strain for all adhesives, which is slightly different from findings of this study where PUR group had the highest P_{max} . However, PUR group results may be partially attributed to significant plastic strains developed in wood

due to bending. It is also necessary to mention Martins et al. (2019) used a different test, with higher strain rate (failure till 20 s) and different wood species (Maritime pine), so the comparison with this case is only partially valid. The effect of the bonding pressure on P_{max} was not studied in this work, but Santos et al. (2019) found no differences in shear strength of Maritime pine elements glued with PUR adhesive in this respect. Despite the pressure applied to the analyzed adhesives being slightly different, due to their specific technical recommendations, it is assumed it did not influence the test to a great extent, so it will not be discussed further. Mean relative difference between deflections at P_{max} obtained by cross-head and DIC was 2.57%.

3.2 DIC analysis

Optical image series were processed with 3D-DIC software (Aramis), which provided displacements in three directions with respect to fiber direction (L, R, T), normal strains in two directions (ε_{LL} , ε_{RR}) and shear strain (ε_{LR}). Since mode II is shear mode, ε_{LR} is the best to show strain concentration at the bondline (Figure 5a). Figure 5a clearly shows the shear opening and deformation at the adhesive bondline and, further, two points below and above the crack tip (green dots) that enabled obtaining displacement slip (w_{II}) . The typical experimental horizontal displacements $(u^+ \text{ and } u^-)$ for these two points are plotted in Figure 5b. It shows that the horizontal displacement below and above the sample's ideal neutral axis (NA) follows different paths which, consequently, creates the w_{II} ; it may also identify linear zones and a moment of P_{max} where the specimen failed. The position of these points is crucial for further correct calculations of G_{II} . These points should be located as close as possible to a crack tip that is ideally located at the NA. However, to achieve this for bonded

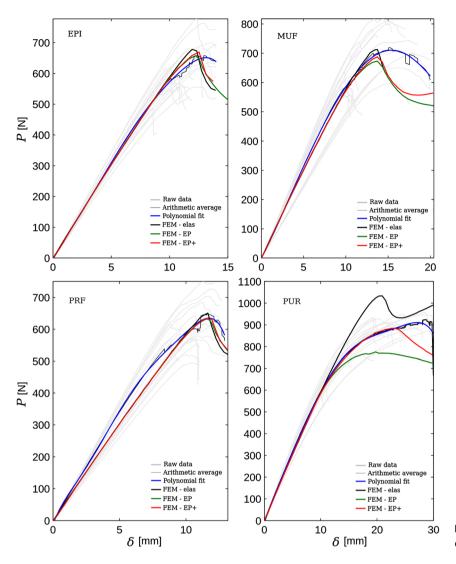


Figure 3: Experimental and numerical P/δ curves for tested adhesives.

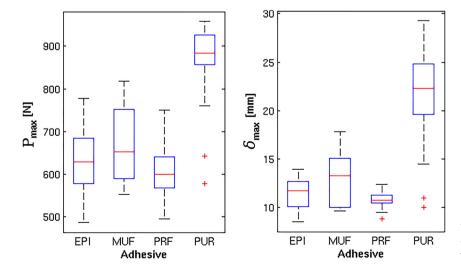


Figure 4: Box plots showing variability for tested adhesives in terms of P_{max} (left) and $\delta_{
m max}$ (right). The red line denotes median value, plus denotes outliers.

wood lamellas is very difficult due to variability of wood properties, their geometry and possible different elastic moduli in tension and compression as found for various species, for instance for beech at MC below 13% (Ozvhar et al. 2013) or for cherry and walnut (Bachtiar et al. 2017). In addition to the unknown position of the NA, these uncertainties contribute to the fact that it is very difficult to obtain true fracture toughness in mode II for wood-bonded specimens. Figure 5c shows three pairs of points above and below NA and their horizontal displacements vs. relative time (pseudo-time of analysis) obtained from FE model that has symmetry of both material properties and geometry with respect to the NA. Curves are paired from outer to inner, and they demonstrate that the closer the pair of points is to the NA, the greater the displacement slip (w_{II}) is, in this case, w_{II} is 2, 4 and 6 mm. The w_{II} is important for deriving a track-separation model, as seen below.

The w versus deflection for all specimens, including the averages for all adhesive groups, is presented in Figure 6. For the EPI, MUF and PRF adhesives, it shows mild increase with loading, and at the point of reaching elastic limit, the curves start progressing steeply. PUR group does not have such rapid change of steepness at the elastic limit. As visible, scatter of the w is very high, especially after reaching the elastic limit. The scatter is caused by progression of the crack at the bondline that often has a tooth-like effect on a curve. Progression of the crack was not studied for individual specimens, so it is not possible to say whether it happened in the wood or adhesive for a given tooth-like step. Looking at the PUR, it may also be noticed that the polynomial curve experiences an inflection point at a deflection of about 25 mm. This is caused by w data and could be removed by limiting to a certain maximal deflection. However, because the $P_{\rm max}$ was achieved for several specimens after deflection of 25 mm, it would not be consistent to do this within the group and, therefore, it was left it as it is. The question that arises from results of PUR (Figures 3 and 6) is whether the methodology used is convenient for testing woodadhesive bonds made with PUR or PUR-like adhesives, i.e., adhesives with large elastic and plastic strain capacity. Furthermore, using 3D-DIC cannot fully assist in exploration of microcracking at adhesive bond loaded in mode II at such a level of observation. Wood-adhesive bond is a very different situation compared to the adhesive bonds in man-made composites (e.g., carbon-adhesive) where identification of differences for adhesives of various toughness is possible, including the pattern of microcracking because the crack predominantly propagates through adhesive (Bradley 1991). Therefore, displaying

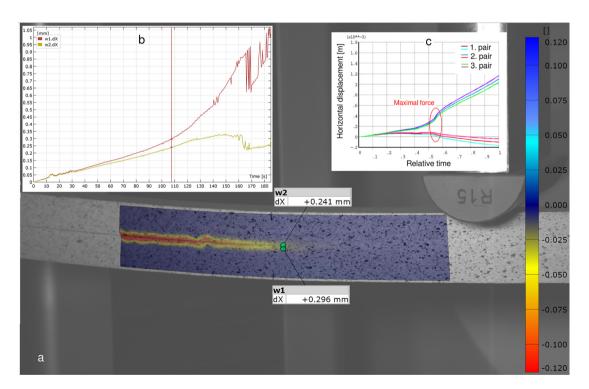


Figure 5: (a) Shear strain (ε_{xv}) computed using DIC with the two points used for calculation of displacement slip highlighted (w). (b) Graph showing displacements in horizontal direction vs. time for the two green points at crack tip; (c) horizontal displacements from FE simulation for 3 pairs of points with various vertical distance from the crack tip.

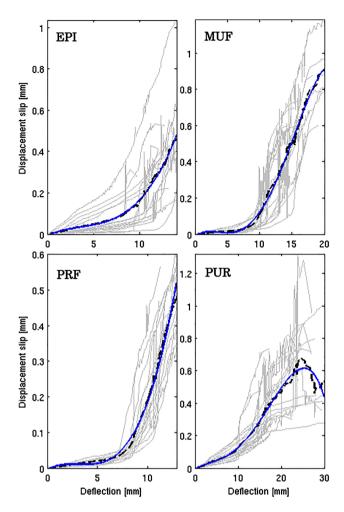


Figure 6: Displacement slip (*w*) vs. deflection for tested adhesives. Raw data are plotted as grey. The black dashed line represents arithmetic average of curves, and the blue solid line is polynomial fit of 6th degree.

raw data is important and useful for wood-adhesive bondline because it may reveal common phenomena within individual specimen's behavior.

3.3 Strain energy release rate and cohesive model

The procedure of ECLA and Eq. (1) for average P/δ curves and average w enabled to obtain a relationship between G_{II} and equivalent crack length (a_{eq}) . The result of this procedure is shown in Figure 7a as four average curves for particular adhesive groups. The curves include mean critical strain energy release rate G_{IIc} (denoted as red asterisk), which attributes for $P_{\rm max}$. The mean G_{IIc} is 1.80, 2.33, 1.59 and 5.40 Nmm⁻¹ for EPI, MUF, PRF and PUR, respectively. PUR has the highest G_{IIc} because the $P_{\rm max}$ was achieved

much later after reaching the elastic limit for other groups of adhesives. All obtained mean values of G_{IIc} are higher than the value for clear beech wood (1.41 Nmm⁻¹) at similar MC presented by Sebera et al. (2019). However, with respect to wood variability, it can be claimed that only EPI, MUF and PUR have likely significantly higher G_{IIc} than mentioned value of clear wood due to a presence of adhesive bond. The increase of shear stiffness and shear strength due to a presence of adhesive bondline may happen; for instance, it was reported for balsa wood tested in pure shear using Iosipescu specimens (Osei-Antwi et al. 2013). Such increase is attributed to higher rigidity and shear strength of adhesive compared to wood at loaded plane. From a practical perspective, it is important to know that adhesive bond enhances stiffness and strength

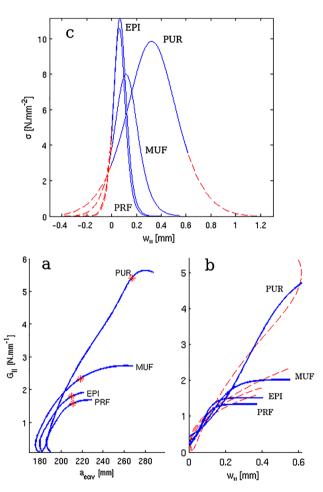


Figure 7: (a) Average strain energy release rate (G_{II}) vs. average equivalent crack length (a_{eq}) . Red asterisk denotes average critical strain energy release rate at P_{\max} (G_{IIc}) . (b) Average G_{II} vs. average displacement slip (w_{II}) . Red lines represent data up to G_{IIc} and blue lines represent logistic function fitted to the averaged curves. (c) Cohesive model computed by differentiating logistic functions (blue part of the curves) shown in Figure 7b and extrapolated cohesive model using Gaussian fit from Table 1 (red dashed parts of curves).

of beam elements which might be used to an advantage when designing timber construction elements.

Using Eq. (2) enabled to find parameters to fit the relationships of G_{II} vs. w_{II} with a logistic function. This functional fit, together with average curves ending at G_{IIc} , is plotted in Figure 7b. The use of logistic function decreased the value of G_{IIc} , which is the value logistic function asymptotically converges to on a given range.

It may also be noticed that those fits do not start at zero of the y-axis, which is due to the fact that the best logistic fit to the G_{II} vs. w_{II} data was used. Differentiation of the logistic curves following Eq. (3) led to a cohesive model for studied adhesives (Figure 7c). The fact that logistic curves do not have a zero tangent at position of x = 0 resulted in cohesive models that do not start at zero y-axis (stress) positions (see blue sections of the curves in Figure 7c). Such cohesive models are not complete; i.e., the area under the curves is not equal to the G_{IIC} , so they need to be extrapolated up to y = 0. For this, the Gaussian model of 2nd order (GM2) was used, and the result of the fit is listed in Table 1 and plotted as red dashes on the cohesive model in Figure 7c. The GM2 has a form of $a_1 \times e(-((x-b_1)/c_1)$ ^2) + $a_2 \times e(-((x - b_2)/c_2)^2)$, where x is variable and e is Euler's number. It is also necessary to mention a certain error affecting the derivation of G_{II} stemming from the fact that residual stresses in specimens were neglected. This also implies that obtained toughness is apparent and not true. However, assessing this issue is out of the scope of this study; a method to address this problem was published for double cantilever beams loaded in mode I (Nairn 2000).

3.4 FE model

Cohesive models for all adhesives in the form of 2nd order Gaussian function in Table 2 can be easily transformed into the bilinear cohesive model (BCM) because the Gaussian fit is an evenly symmetric function. The BCM presented in Table 2 was used in FE simulations of the physical test for all adhesives. The results of the simulations are shown in Figure 3 as three solid lines (black for Elas, green for EP and red for EP+). FE prediction of force-displacement response

in the elastic part of the test is sufficient compared to polynomial fit (blue line); only the PRF group shows a certain bump in the middle of the elastic part due to using arithmetic average as the base for polynomial fit. An agreement of FE model with the experiments regarding stiffness is determined by an orthotropic material model taken from the literature (Milch et al. 2016). This implies that wood used in this work had very similar properties as one in the Milch et al. (2016), despite the fact that both woods came from different growing positions within the region of Central Europe.

The prediction of FE models in terms of relative difference (RD) regarding the maximal force (P_{max}) is shown in Table 3. It shows that using the elastic model with cohesive zone predicts P_{max} very accurately for EPI, MUF and PRF groups (RD <5%), but for the PUR adhesive it reaches RD about 13.5%. The EP material model predicts $P_{\rm max}$ within the same accuracy as the elastic one (RD <5.2%), except for the PUR, which has RD of about 15%. This is due to the fact that wood in PUR group started to plasticize parallel to the fiber before reaching stress needed to open the crack. The crack in PUR group opened later at higher load levels and propagated less than for other adhesive groups. This is clearly visible from the green line in Figure 3 that shows the scenario of beech wood with the same tensile and compressive yield stresses. The FE model with EP+ material predicts P_{max} with the lowest RD's (<3.4%); although for EPI, MUF and PRF adhesive, it sometimes exceeds RD compared to Elas and EP material models. The biggest improvement in using EP+ was achieved for PUR adhesive, whose RD decreased to -3.35%. This means the material model with different tensile and compressive yield stresses is the most suitable for modeling PUR-like adhesives for this test. Illustration of this phenomenon when using EP+ material model for the 3ENF test is depicted in Figure 8. It shows that when using elastic material only (Figure 8a), the maximal deflection, and also maximal compressive strain (3rd principal strain \approx 0.013), occur in the middle of the specimen; meanwhile, when using EP+ material (Figure 8b), the maximal deflection and compressive strain (3rd principal strain ≈ 0.037) occur away from the specimen center

Table 2: Coefficients for 2nd order Gaussian fits (R>0.99 for all) and data for bilinear cohesive model.

| Group | a ₁ | a ₂ | b ₁ | b ₂ | <i>c</i> ₁ | <i>c</i> ₂ | G _{lic} (Nmm ⁻¹) | $\sigma_{\sf max}$ (MPa) | w _{max} (mm) |
|-------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|---------------------------------------|--------------------------|-----------------------|
| EPI | 5.062 | 6.096 | 0.06555 | 0.06649 | 0.09984 | 0.05697 | 1.51 | 11.2 | 0.25 |
| MUF | 4.433 | 3.56 | 0.1166 | 0.1153 | 0.1068 | 0.187 | 2.02 | 7.99 | 0.43 |
| PRF | 5.783 | 4.816 | 0.06234 | 0.06144 | 0.05283 | 0.09262 | 1.33 | 10.6 | 0.24 |
| PUR | 3.693 | 6.161 | 0.3222 | 0.324 | 0.204 | 0.3507 | 4.69 | 9.85 | 0.80 |

 $[\]sigma_{\rm max}$ is the peak of the bilinear model and $w_{\rm max}$ is displacement slip at the $\sigma_{\rm max}$.

near the introduced crack tip due to reaching yield stress in compression parallel to fiber in the upper part of lamellas. This phenomenon was also observed within the experiments with the PUR group that showed the highest deflection and failure at the crack tip (Figure 8c).

To evaluate the most precise material model of wood for all adhesive bonds altogether, the summation of absolute values of RD's for a given material model can be used (see ΣRD in Table 3). Then, the EP+ performs the best, followed by Elas and EP. However, for a quick, simple, valid and sound prediction of P_{max} , the orthotropic elastic material model is a high-quality choice for EPI, MUF and PRF adhesive bonds. To model adhesive bonds made with PUR, this work suggests using orthotropic elastoplastic material models of wood with different tensile and compressive yield stresses. This holds true especially for Mode II-dominating problems or problems of bending where induced stresses might get higher yield than stress parallel to fiber of wood. This work implies that used geometrical configuration needs to be modified for testing PUR adhesive bond to achieve deformations only at adhesive bond, i.e., without having plastic strains at surface fibers of specimen. It has been shown that using orthotropic elasto-plastic material models to analyze phenomena occurring when wooden elements are mechanically loaded has become a valid approach leading to more precise predictions. This was demonstrated for clear pine wood (Pěnčík 2015), spruce and beech wood (Milch et al.

Table 3: Relative differences of FE models (%) for various material models of beech wood (constant friction coefficient and no fiber angle distortion), ΣRD is summation of absolute values of RD's of all groups for given material model.

| Material model | EPI | MUF | PRF | PUR | ΣRD |
|----------------|------|-------|-------|-------|-------|
| Elas | 4.15 | 0.28 | 2.52 | 13.5 | 20.45 |
| EP | 0.92 | -5.14 | -0.16 | -14.8 | 21.04 |
| EP+ | 2.74 | -3.27 | -0.47 | -3.35 | 9.83 |

2017), and glulam beams made from softwoods with various connection surfaces (Uzel et al. 2018).

3.5 Friction

In the experiment, Teflon paper to reduce the friction between non-glued lamellas was used since it affects the measurement of force and displacement and, consequently, the obtained G_{II} values. The FE model enabled analysis of the impact of friction coefficient between lamellas (μ_{WW}) on stiffness and P_{max} of the specimen. The friction between specimen and steel grips was kept at constant value of μ_{SW} = 0.33. Varying μ_{WW} from 0 to 1 resulted in an increase in P_{max} of ~4.3% and increase of stiffness (P/δ) of ~2.5%. The impact μ_{WW} on both is depicted in Figure 9a; only a scenario with EPI adhesive was computed to illustrate this effect. This means that it is physically justified to insert Teflon paper into the crack to obtain more precise results. The Teflon paper should be located right above the support where the highest contact pressure occurs (Figure 9b). Visual comparison of the two most typical failures that occurred is shown in Figure 9c. It shows that the failure of adhesive bond with PUR adhesive occurred primarily in wood (Figure 9c left); meanwhile, for EPI adhesive (Figure 9c right), it showed brittle-like failure at adhesive-wood interface, which was found to be a typical failure of PRF and MUF groups, too.

3.6 Fiber angle

The specimens for 3ENF test are relatively long (0.5 m) and, therefore, there is higher probability that fiber direction will not be precisely aligned with specimen main axis. Therefore, the impact of fiber angle distortion on $P_{\rm max}$ and stiffness response with respect to longitudinal axis was analyzed using Elas and EP+ material models because

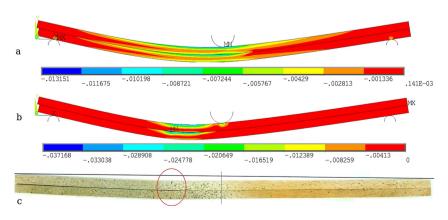


Figure 8: (a) Computed 3rd principal strain at max. deflection for PUR adhesive with Elas material. (b) Computed 3rd principal plastic strain for PUR at $\delta_{\rm max}$ with EP+ material. (c) Typical specimen from PUR group with denoted specimen center (grey line) and the $\delta_{\rm max}$ at crack tip (red ellipse), photographed after the test.

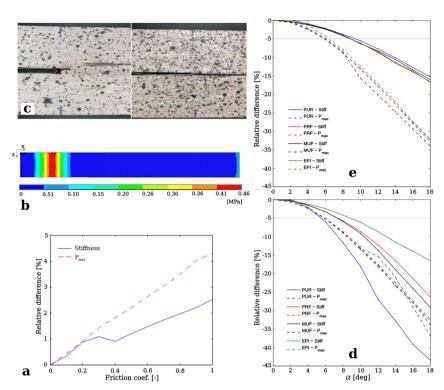


Figure 9: (a) FE analysis of impact of μ_{WW} on stiffness and P_{max} . (b) FE computed friction stress (Pa) at introduced crack (red zone is located right above the support, top view). (c) Typical failure for PUR (left) and EPI & PRF (right). (d) FE analysis of impact of α on stiffness and P_{max} using EP+ material. (e) FE analysis of impact of α on stiffness and P_{max} using Elas material.

these two were shown to be the best to simulate the 3ENF test for given adhesives. Results of these 80 simulations are displayed in Figure 9d and 9e. Figure 9e shows scenarios with Elas material, and it reveals the P_{max} is more impacted by angle distortion than stiffness on average, e.g., at 6° angle distortion, P_{max} is reduced by 5%; meanwhile, stiffness is reduced the same at an angle of 9°. It is clear that by using Elas material, all the adhesive groups behave very alike. On the contrary, using EP+ material shows that the more brittle the adhesive bond is, the less impact the fiber angle has on $P_{\rm max}$. For instance, for PUR, the 5% or RD is reached at 6°, but for EPI, this RD is achieved at 9°. The impact of grain angle on stiffness using EP+ is similar when Elas material is used. This concludes in a finding that adhesive bonds made by various adhesives react differently to grain angle distortion. If angle distortion below 4° is kept, the impact will be maximally 2.5% in RD for all the adhesives in terms of P_{max} and even lower in terms of stiffness. FE analysis of the effect of fiber angle distortion at specimen cross section (RT plane) on stiffness and P_{max} is not shown since it does not influence the behavior as much; changing the angle at RT plane from 0 to 90° impacted resulting P_{max} until 2% and stiffness below 1%.

4 Conclusions

The presented work deals with an experimental and numerical assessment of fracture behavior for adhesive bond

loaded in mode II using 3-point end-notched flexure tests when various adhesives are used. The work showed results for materials commonly used in wood composites and timber structures, and it also demonstrated applicability of the test to determine fracture properties of wood composites that are suitable for numerical modeling. The work resulted in several important findings that can be concluded as follows:

- Adhesive bond with EPI, PRF and MUF showed rather brittle behavior as the failure and crack occurred primarily at the interface of adhesive and wood. These three adhesives can be conveniently investigated by 3-point end-notched flexure test to obtain apparent fracture toughness and strain energy release rate (*G_{II}*).
- Adhesive bond with PUR showed substantial nonlinear response due to plastic strains occurring in specimens' outermost fibers and PUR elastomeric nature. This phenomenon was also confirmed by numerical analysis and, altogether, results suggest modifying the test configuration to reveal more accurate values of G_{IIc} for bondline made with PUR. Failure and crack propagation in specimens with PUR bondline occurred mostly in wood.
- For EPI, MUF and PRF, elastic material model with cohesive zone offers accurate prediction of maximal force (relative difference below 5%) and character of failure.
- For PUR adhesive, elastic and elasto-plastic model with same tension and compression yields parallel to grain do not offer such high accuracy (relative

- difference ~13.5%) compared to model with distinguished yield stresses in tension and compression parallel to fiber (rel. diff. ~3.4%).
- Friction between wooden lamellas in 3-point endnotched flexure test has negligible effect on stiffness (max. \sim 2%) and minor effect on P_{max} (max. \sim 4%). However, to get a more accurate G_{IIC} , introducing any material to reduce friction in between lamellas is recommended.
- Grain angle distortion with respect to longitudinal specimen axis impacts the flexural stiffness and P_{max} variously depending on adhesive type. In general, having fiber angle below 4° results in a maximal relative difference of 2.5%.

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