



Research Article

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Using Monarch Butterfly Optimization to Solve the Emergency Vehicle Routing Problem with Relief Materials in Sudden Disasters

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Abstract: China has one of the highest rates of natural disasters in the world. In recent years, the Chinese government has placed a high value on improving emergency natural disaster relief. The goal of this research was to resolve a key issue for emergency natural disaster relief: the emergency vehicle routing problem (EmVRP) with relief materials in sudden disasters. First, we provided a description of the EmVRP, and defined the boundary conditions. On this basis, we constructed an optimization model of EmVRP with relief materials in sudden disasters. To reach the best solution in the least amount of time, we proposed an enhanced monarch butterfly optimization (EMBO) algorithm, incorporating two modifications to the basic MBO: a self-adaptive strategy and a crossover operator. Finally, the EMBO algorithm was used to solve the EmVRP. Our experiments using two examples EmVRP with relief materials in a sudden-onset disaster proved the suitability of EMBO. In addition, an array of comparative studies showed that the proposed EMBO algorithm can achieve satisfactory solutions in less time than the basic MBO algorithm and seven other intelligent algorithms.

Keywords: Emergency vehicle routing problem; relief materials; sudden disasters; intelligent algorithms; monarch butterfly optimization; self-adaptive; crossover operator

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1 Introduction

When natural disasters occur, an efficient logistics system is vital for emergency relief work. Although rapid advances in science and technology have improved our ability to predict some natural disasters with increasing certainty, sudden natural disasters are still a major threat to the survival of regional populations and to the maintenance of social and economic development. Even when a disaster can be predicted in advance, obstacles such as short warning times and long transport distances make it difficult to protect threatened populations in the interval between the forecast and the event. Therefore, an efficient emergency natural disaster relief logistics system is key to providing rescue and post-disaster relief for many people.

Studies of emergent natural disaster relief logistics systems have concentrated primarily on two areas of concern [75]. First, researchers have explored methods for evaluating the degree of impact of a natural disaster. The evaluation results determine the level of demand for emergency relief, and the logistics of distribution. Second, studies have examined the topologies of emergency logistics distribution networks, including the emergency vehicle routing problem (EmVRP). This paper focuses on finding the most efficient way to assign vehicles to bring relief materials and goods to disaster sites from various storage areas such as depots, railway stations, airports, and docks.

One of the most representative studies on emergency logistics was the LP (linear programming) model proposed by Rathi *et al.* [41]. In that study, the authors assigned each vehicle to each route to obtain the optimal network. A traditional optimization algorithm was adopted in this model, but the process fell easily into the local optimum. Equi *et al.* [8] studied the optimal number of trips and the number of vehicles needed to complete each travel route in the context of a given number of supply centers. While it may be feasible to target those receiving relief after a nat-

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ural disaster, it is difficult to differentiate the amount of relief provided among beneficiaries. This is because much of the relief consists of food, clothing, and medicine, all goods for which the absorptive capacity of households is limited. Empirical tests using data from Honduras following Hurricane Mitch confirm this hypothesis. The probability of receiving relief was negatively correlated with wealth and positively correlated with assets losses (with a higher weight placed on losses than pre-disaster wealth) and the fact that households suffered damage to their dwelling. By contrast, controlling for whether households suffered damage to their dwelling, the amount of relief received was related neither to pre-Mitch wealth, nor to assets losses [36].

Current studies of the EmVRP have provided greater depth by considering changes of various factors in the models, and by using more advanced algorithms. However, studies that consider a combination of the EmVRP and the logistics of emergency materials distribution are still relatively scarce. Moreover, the models that have been produced to date for the mechanisms and optimization of emergency distribution have not been able to meet real-world demands in terms of objective function and boundary conditions [75].

In contrast, the monarch butterfly optimization (MBO) algorithm proposed by Wang *et al.* in 2015 [55] is a novel and promising swarm-based intelligent method [48]. Although the MBO algorithm was proposed only two years prior to the writing of this paper, some researchers have implemented several in-depth studies from algorithm improvements and engineering application [12–14].

In fact, the EmVRP with relief materials in sudden disasters is an NP-hard problem [75] that is difficult to solve using traditional methods. In this paper, we proposed an enhanced monarch butterfly optimization (EMBO) algorithm to tackle the EmVRP problem. In the EMBO algorithm, the crossover operator used in evolutionary algorithms (EAs) is incorporated into the basic MBO algorithm to generate a new offspring population for the next generation. In addition, the self-adaptive scheme is used to establish the butterfly adjusting rate. We used the proposed EMBO algorithm to solve the EmVRP with relief materials in sudden disasters, and we provided comparative studies between the basic MBO algorithm and seven other intelligent algorithms to demonstrate the superiority of EMBO in terms of accuracy.

The remainder of this paper is structured as follows. The next section reviews the related preliminaries, including the EmVRP and MBO algorithm. Section 3 provides the description of the EmVRP with relief materials in sudden disasters, followed by the main framework of MBO and the

proposed EMBO algorithm, as shown in Section 4. Subsequently, Section 5 details how to use EMBO to solve the EmVRP with relief materials in sudden disasters. Then, in Section 6, an array of experiments on EmVRP are carried out. The final section summarizes our current work, and provides our future work orientation.

2 Preliminaries

2.1 EmVRP

In the Introduction above, we described briefly some of the prior work focused on EmVRP. In this section, we review examples of other significant contributions to the field.

Hale and Mober [23] studied the selection of emergency logistics supply nodes, with particular attention to the number of nodes (sites) for storage of emergency supplies. Their research proposed a quantitative model. For vehicle routing within a time window (VRPTW) involving a limited number of vehicles, Lau *et al.* [30] constructed a model and put forward the related solutions. In addition, they implemented a substantial number of fundamental studies on the variants of the traditional VRP problem.

Based on the features of multi-resource and multi-point rescue, Dai *et al.* [6] constructed a mathematical model to solve the multi-resource emergency problem. Fu *et al.* [15] divided emergency logistics distribution issues into three categories: road conditions, vehicle conditions, and the state of materials. They proposed a static, dynamic, and functional model in accordance with each emergency issue category. To address actual challenges of VRP with time windows, Li [32] put forward a method based on affinity group match, and further proved that the immune algorithm can provide an effective solution for routing vehicle within a time frame.

Özdamar *et al.* [38] studied distribution decision support systems after natural disasters. A model was established by considering disaster relief materials comprehensively, regarding vehicles as both relief materials and transportation resources. In addition, Ghiani [21], Iko [24], and Özyurt [39] proposed several different algorithms to solve the EmVRP problem.

Though many scholars have carried out several in-depth studies regarding emergency relief, few of them has used swarm intelligence algorithm to solve emergency vehicle routing problem with relief materials in sudden disasters. In this paper, one of the most representative swarm intelligence algorithms, called monarch butter-

fly optimization (MBO), is introduced to solve emergency vehicle routing problem with relief materials in sudden disasters. Next, the mainframe of MBO algorithm will be provided.

2.2 MBO algorithm

Since MBO [55] was proposed, many scholars have explored this approach. In this section, some of the most representative work regarding MBO is summarized and reviewed.

Yi *et al.* [70] combined quantum computation theory into MBO algorithm, and proposed a novel quantum-inspired MBO methodology, called QMBO, by incorporating quantum computation into the basic MBO algorithm. In QMBO, a certain number of the worst butterflies were updated by quantum operators. The path planning navigation problem for Unmanned Combat Air Vehicles (UCAVs) was modeled into an optimization problem, and then its optimal path could be obtained by the proposed QMBO algorithm. Furthermore, B-Spline curves were utilized to refine the obtained path, making it more suitable for UCAVs. The UCAV path obtained by QMBO was studied and analyzed in comparison with the basic MBO. The experimental results showed that QMBO can find a much shorter path than MBO.

Ghetas *et al.* [20] incorporated the harmony search (HS) algorithm into the basic MBO algorithm, and proposed a variant of MBO, called MBHS, to deal with the standard benchmark problems. In MBHS, the HS algorithm was considered as a mutation operator to improve the butterfly adjusting operator, with the aim of accelerating the convergence rate of MBO.

Feng *et al.* [10] presented a novel binary MBO (BMBO) method used to address the 0-1 knapsack problem (0-1 KP). In BMBO, each butterfly individual was represented as a two-tuple string. Several individual allocation techniques were used to improve BMBO's performance. In order to keep the number of infeasible solutions to a minimum, a novel repair operator was applied. The comparative study of BMBO with other optimization techniques showed the superiority of the former in solving the 0-1 KP.

Wang *et al.* [62] put forward another variant of the MBO method in combination with GCMBO. In GCMBO, two modification strategies, including a self-adaptive crossover (SAC) operator and a greedy strategy, were utilized to improve its search ability.

Feng *et al.* [14] combined chaos theory [50] with the basic MBO algorithm, and then proposed a novel chaotic MBO (CMBO) algorithm. The proposed CMBO algorithm

enhanced the search effectiveness significantly. In CMBO, in order to tune two main operators, the best chaotic map was selected from 12 maps. Meanwhile, some of the worst individuals were improved by using a Gaussian mutation operator to avoid premature convergence.

Ghanem and Jantan [19] combined ABC with elements from MBO to propose a new hybrid metaheuristic algorithm named Hybrid ABC/MBO (HAM). The combined method used an updated butterfly adjusting operator, considered to be a mutation operator, with the aim of sharing the information with the employee bees in ABC.

Wang *et al.* [59] proposed a discrete version of MBO (DMBO) that was applied successfully to tackle the Chinese TSP (CTSP). They also studied and analyzed the parameter butterfly adjusting rate (BAR). The chosen BAR was used to find the best solution for the CTSP.

Feng *et al.* [12] proposed a type of multi-strategy MBO (MMBO) technique for the discounted 0-1 knapsack problem (DKP). In MMBO, two modifications, including neighborhood mutation and Gaussian perturbation, were utilized to retain the diversity of the population. An array of experimental results showed that the neighborhood mutation and Gaussian perturbation were quite capable of providing significant improvement in the exploration and exploitation of the MMBO approach, respectively. Accordingly, two kinds of NMBO were proposed: NCMBO and GMMBO, respectively.

Feng *et al.* [13] combined MBO with seven kinds of DE mutation strategies, using the intrinsic mechanism of the search process of MBO and the character of the differential mutation operator. They presented a novel DEMBO based on MBO and an improved DE mutation strategy. In this work, the migration operator was replaced by a differential mutation operator with the aim of improving its global optimization ability. The overall performance of DEMBO was fully assessed using thirty typical discounted 0-1 knapsack problem instances. The experimental results demonstrated that DEMBO could enhance the search ability while not increasing the time complexity. Meanwhile, the approximation ratio of all the 0-1 KP instances obtained by DEMBO was close to 1.0.

Wang *et al.* [49] proposed a new population initialization strategy in order to improve MBO's performance. Firstly, the whole search space is equally divided into N_p (population size) parts at each dimension. Subsequently, two random distributions (T and F distribution) are used to mutate the equally divided population. Accordingly, five variants of MBOs are proposed with a new initialization strategy.

Feng *et al.* [11] presented OMBO, a generalized opposition-based learning (OBL) [56] MBO with Gaussian

perturbation. The authors used the OBL strategy on the portion of the individuals in the late stage of evolution, and used Gaussian perturbation on the individuals with poor fitness in each evolution. OBL guaranteed the higher convergence speed of OMBO, and Gaussian perturbation avoided the possibility of falling into a local optimum. For the sake of testing and verifying the effectiveness of OMBO, three categories of 15 large-scale 0-1 KP cases from 800 to 2,000 dimensions were used. The experimental results indicated that OMBO could find high-quality solutions.

Chen *et al.* [4] proposed a new variant of MBO by introducing a greedy strategy to solve dynamic vehicle routing problems (DVRPs). In contrast to the basic MBO algorithm, the proposed algorithm accepted only butterfly individuals that had better fitness than before implementation of the migration and butterfly adjusting operator. Also, a later perturbation procedure was introduced to make a trade-off between global and local search.

Meng *et al.* [34] proposed an improved MBO (IMBO) for the sake of enhancing the optimization ability of MBO. In IMBO, the authors divided the two subpopulations in a dynamic and random fashion at each generation, instead of using the fixed strategy applied in the original MBO approach. Also, the butterfly individuals were updated in two different ways for the sake of maintaining the diversity of the population.

Faris *et al.* [9] modified the position updating strategy used in the basic MBO algorithm by utilizing both the previous solutions and the butterfly individuals with the best fitness at the time. For the sake of fully exploring the search behavior of the Improved MBO (IMBO), it was benchmarked by 23 functions. Furthermore, the IMBO was applied to train neural networks. The IMBO-based trainer was verified on 15 machine learning datasets from the UCI repository. The experimental results showed that the IMBO algorithm could enhance the learning ability of neural networks significantly.

Ehteram *et al.* [7] used the MBO algorithm to address the utilization of a multi-reservoir system for the sake of improving production of hydroelectric energy. They studied three periods of dry (1963-64), wet (1951-52), and normal (1985-86) conditions in a 4-reservoir system. The experiments indicated that MBO can generate more energy when compared with particle swarm optimization (PSO) and a genetic algorithm (GA).

Xue *et al.* [67] added a self-adaptive strategy to the basic ABC algorithm in accordance with the global optimal solution, so a new variant of ABC named SABC-GB was proposed. SABC-GB has shown its superiority to other meta-heuristic algorithms when dealing the complicated optimization problems.

In addition to the MBO algorithm studied in this paper, many other intelligent algorithms [65] have been proposed, such as elephant herding optimization (EHO) [33, 57], simulated annealing (SA) [27], evolutionary strategy (ES) [2], particle swarm optimization (PSO) [26, 44], moth search (MS) algorithm [47], bat algorithm (BA) [35, 68], differential evolution (DE) [43, 53], biogeography-based optimization (BBO) [42, 52], krill herd (KH) [16, 51, 54], cuckoo search (CS) [5, 69], artificial bee colony (ABC) [25, 64], genetic algorithm (GA) [22], fireworks algorithm (FWA) [46], earthworm optimization algorithm (EWA) [61], and harmony search (HS) [18, 63]. These algorithms are used widely in various engineering applications [73, 74].

In this paper, the model of emergency vehicle routing problem with relief materials in sudden disasters is provided. Also, we will further improve the performance of the basic MBO algorithm by introducing the self-adaptive strategy and crossover operator to form a novel enhanced MBO (EMBO) algorithm. The proposed EMBO algorithm is then used to tackle EmVRP problem in comparison with the basic MBO algorithm and seven other intelligent algorithms.

3 EmVRP with relief materials in sudden disasters

3.1 Problem description

If the scale of a sudden natural disaster is large, the distribution of emergency materials may require a variety of transport modes as well as the conversion of various transportation modes. In our current work, we focused on one mode of transportation only, assuming that relief supplies brought by rail, air, and water had already arrived at train stations, airports, and docks in the general disaster area. Therefore, those terminals (depots, railway stations, airports, and docks) were also seen as material storage facilities. Our goal was to determine how to assign vehicles from parking areas (such as garages) to transport relief materials and goods from the various storage sites (depots, railway stations, airports, and docks) to the primary disaster points. An overview of the whole system involved in the emergency VRP with materials in sudden disasters is shown in Fig. 1 [75].

As shown in Fig. 1, the emergency relief material distribution system is a three-layer structure. Transporting the materials is essentially a vehicle routing problem involving movement from multiple parking areas (garages) to multiple storage sites, and then to multiple disaster

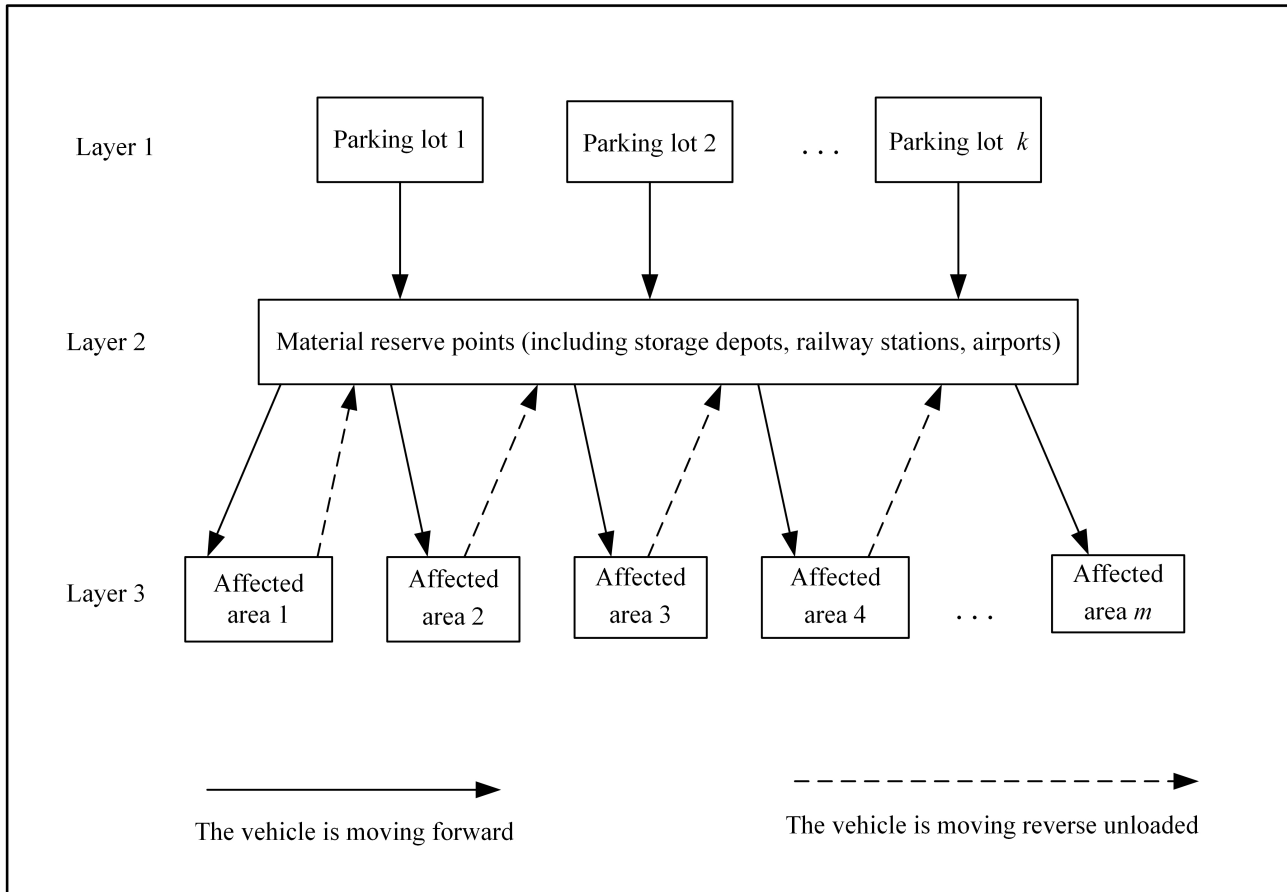


Figure 1: The structure of three hierarchy of vehicle scheduling for emergency relief goods.

points. Layer 1 includes the parking areas; all the vehicles assigned to carrying relief materials start from the parking lots. The number of vehicle types may vary, but the number is known.

Layer 2 is made up of the material reserve storage sites, including all wharfs, train stations, airports, and similar facilities. We assume that the relief supplies at each reserve point are varied, and that the number of certain types of materials is unchanged during the emergency period. The bottom layer, Layer 3, comprises the affected areas that are the destinations for relief distribution. After a disaster, demand for all kinds of emergency supplies will be generated at all the impact points according to the disaster assessment. This demand will determine the need to move reserves at all levels and locations, which in turn will call for a certain number of vehicles to begin distribution of aid materials.

From Layer 1 to Layer 2, there is vehicle flow only, with no material flow, i.e., the vehicles run from Layer 1 to Layer 2, but they are not loaded. Moreover, this flow is one-way, with the vehicles moving only from the parking areas to the various material reserve sites. They do not return to

the parking areas during the emergency period. However, both vehicle flow and material flow occur between Layer 2 and Layer 3. Materials move in a one-way unidirectional flow from Layer 2 to Layer 3, while the vehicles form a two-way flow between these two layers. After a vehicle arrives at a disaster point, it does not immediately return to the parking areas, but instead remains in the arrival spot on standby. Once a new distribution task is ordered, the vehicle will go back to the appropriate material storage site to be loaded and start a new distribution.

Therefore, after a vehicle arrives at an affected area from a reserve area, there are two possible states for the vehicle. Either it remains in the impacted area waiting for new orders, or it may be given a new task immediately, in which case it returns right way to the reserve to begin the next round of distribution, as shown by the dotted line in Fig. 1. In our current work, we assumed that the vehicle is running along the unloaded reverse flow. In this process, the flow of vehicles is significantly different from that of common commercial logistics.

Both materials and vehicles flow between Layers 2 and 3. However, there is no connection between each point

of the same layer because the demand for supplies after a sudden disasters is much greater than the normal customer demand for small batches commonly encountered in business logistics. This difference also is reflected by the characteristics of the emergency relief supplies demanded by the affected points. The primary goal of post-disaster distribution is to meet the needs of all the disaster sites as much as possible while shortening the running time of the entire distribution system. In this way, losses are reduced at each disaster point, and the cost of vehicle operations is reduced as well. Vehicles can be reused throughout the distribution system, i.e., the vehicle flow is repeated between the second and the third layers until all the needs of the disaster sites are met.

3.2 Definition and explanation of boundary conditions of model

Under the guidance of the distribution system model of the EmVRP with relief materials in sudden disasters, the boundary conditions of the vehicle distribution system are defined as follows:

(1) There are multiple supply points and demand points in the network. The supply and demand of emergency materials are known at each point, and the total supply can meet the needs of the affected areas.

(2) There are many parking areas, and each parking area may have a variety of vehicles. The number of parked vehicles is sufficient to meet the need for materials distribution, and each vehicle has a number.

(3) There are a variety of emergency supplies to be delivered. Each is different in weight and volume, and each has different loading efficiency. It is assumed that the loading efficiency of the material at the supply site is the same as the unloading efficiency at the disaster site.

(4) Each disaster site can be served by multiple vehicles.

(5) Each delivery task carries only one kind of material.

(6) After the completion of a distribution task, if the vehicle still has supplies, then it will continue to complete the delivery task; otherwise, it will return to the starting point at the parking area to wait for the next dispatch.

(7) There is neither vehicle flow nor material flow between the points of each layer.

3.3 The model of the EmVRP with relief materials in sudden disasters

The model of the emergency VRP with relief materials in sudden disasters consists mainly of four parts: the symbol definition, objective function, constraint condition, and the model description.

(1) Symbol definition

The model of the EmVRP with relief materials in sudden disasters includes the definition of five kinds of symbols: set, parameters related to transportation, parameters related to relief materials, parameters related to distance, and decision variables.

1) Set

The set of materials/goods: $\mathbf{G} = \{G_1, G_2, \dots, G_p\}$;

The set of supply sites (i.e., relief materials reserve sites/points, material storage sites/points): $\mathbf{S} = \{S_1, S_2, \dots, S_n\}$;

The set of disaster sites (affected areas/points): $\mathbf{D} = \{D_1, D_2, \dots, D_m\}$;

The set of parking areas (garages, parking lots): $\mathbf{K} = \{K_1, K_2, \dots, K_k\}$;

The set of vehicles: $\mathbf{L} = \{L_1, L_2, \dots, L_l\}$;

The set of edges: $\mathbf{E} = \{(k, i)(i, j) | k \in \mathbf{K}, i \in \mathbf{S}, j \in \mathbf{D}\}$.

2) Parameters related to transportation

V_l : the maximum volume of the vehicle l ;

cap_l : the maximum dead weight tonnage of the vehicle l ;

v_l : the speed of the vehicle l .

3) Parameters related to relief materials

w_g : the unit weight of material type g ;

c_g : the unit volume of material type g ;

t_g : the time needed for loading and unloading material g .

4) Parameters related to distance

d_{ki} : the distance from the parking area to the material supply site;

d_{ij} : the distance between the supply site and the demand point.

5) Decision variables

x_{ijg} : the quantity of material g that is conveyed from the supply site i to j by vehicle l ;

$$z_{lijg} = \begin{cases} 1 & \text{Vehicle } l \text{ delivers } g \text{ from supply site } i \text{ to } j \\ 0 & \text{Otherwise} \end{cases},$$

$l \in \mathbf{L}, i \in \mathbf{S}, j \in \mathbf{D}, g \in \mathbf{G}$

$$y_{lki} = \begin{cases} 1 & \text{Vehicle } l \text{ passes edge } (k, i) \\ 0 & \text{Otherwise} \end{cases}, l \in \mathbf{L}, k \in \mathbf{K}, i \in \mathbf{S}$$

$$y_{lij} = \begin{cases} 1 & \text{Vehicle } l \text{ passes edge } (i, j) \\ 0 & \text{Otherwise} \end{cases}, l \in \mathbf{L}, i \in \mathbf{S}, j \in \mathbf{D}$$

(2) Objective function

$$\min T = \sum_{l \in \mathbf{L}} \sum_{k \in \mathbf{K}} \sum_{i \in \mathbf{S}} \frac{d_{ki}}{v_l} y_{lki} \quad (1)$$

$$+ \sum_{l \in \mathbf{L}} \sum_{i \in \mathbf{S}} \sum_{j \in \mathbf{D}} \sum_{g \in \mathbf{G}} t_g x_{lij} y_{li} z_{lijg} \quad (2)$$

$$+ 2 \times \sum_{l \in \mathbf{L}} \sum_{i \in \mathbf{S}} \sum_{j \in \mathbf{D}} \frac{d_{ij}}{v_l} y_{lij} \quad (3)$$

$$+ \sum_{l \in \mathbf{L}} \sum_{i \in \mathbf{S}} \sum_{j \in \mathbf{D}} \sum_{g \in \mathbf{G}} t_g x_{lij} y_{lj} z_{lijg} \quad (4)$$

(3) Constraint condition

$$x_{lij} w_g \leq cap_l \quad (5)$$

$$x_{lij} c_g \leq V_l \quad (6)$$

$$\sum_{g \in \mathbf{G}} z_{lijg} = 1 \quad (7)$$

$$\sum_{i \in \mathbf{S}} y_{lki} = 1 \quad (8)$$

$$y_{lki} \in \{0, 1\}, y_{lij} \in \{0, 1\}, z_{lijg} \in \{0, 1\} \quad (9)$$

$$y_{li} \in \{0, 1\}, y_{lj} \in \{0, 1\} \quad (10)$$

$$1 \leq l \leq |\mathbf{L}|, 1 \leq i \leq |\mathbf{S}|, 1 \leq j \leq |\mathbf{D}|, 1 \leq g \leq |\mathbf{G}| \quad (11)$$

(4) Model description

For the model of the EmVRP with relief materials in sudden disasters, the goal is to meet the needs of the affected points in the shortest total running time possible. The total running time of a vehicle includes the travel time from the parking areas to material reserve sites, travel time from material reserve areas to the affected areas, loading time at reserve sites, and unloading time at the affected areas.

For the objective function in the model of the EmVRP with relief materials in sudden disasters, Eq. 1 represents the time from the parking area to the reserve site; Eq. 2 represents the loading time at the reserve site; Eq. 3 represents the time from the material reserve site to the affected site; and Eq. 4 represents the unloading time of the material at the affected area. In our current work, we suppose the vehicles will take the same time moving from the affected point to reserve point.

For the constraint conditions, Eq. 5 means that the goods transported by each vehicle cannot exceed the maximum load capacity of the vehicle; Eq. 6 means that the goods delivered by each vehicle should not exceed the maximum volume of the vehicle; Eq. 7 means that each vehicle carries only one material at a time from the material reserve site to the affected area; Eq. 8 means that the vehicles starting from the garage can only reach a material reserve site, which is a one-way non-circular flow between the first and second layers; and Eqs. 9-10 indicate that the variables of this problem satisfy the 0-1 integer constraint. Eq. 11 represents the range of the indexes in constraints. $|\cdot|$ represents the number of elements contained in a set.

To solve the problem of the model constructed in this paper, it is necessary to construct a heuristic algorithm with simple operation and excellent search performance. At present, the heuristic algorithms used to solve the vehicle scheduling problem include primarily the genetic algorithm (GA), neural network method, ant colony algorithm (ACO), tabu search (TS), and simulated annealing algorithm (SA). Among them, the most popular strategies involve the application of modern intelligent algorithms to vehicle scheduling. Many scholars have proven that the performance achieved using intelligent algorithms is better than the results from other traditional optimization algorithms. Therefore, this paper employed a new intelligent algorithm, monarch butterfly optimization (MBO), to solve the above-established EmVRP model. The required solutions can be represented by a butterfly individual, while a butterfly individual can be represented by different parking areas, reserve sites, and the affected areas.

3.4 Difference between emergency VRP and regular VRP

Emergency VRP is a special vehicle routing activity caused by outbreak of emergencies. Due to its suddenness and lack of information, it is quite different from that of regular VRP (RVRP) [29].

The goal of RVRP is to minimize costs or maximize profits [75]. The distribution network is permanent, and its network structure is designed by the needs of the customer [75]. Participants are mainly all kinds of economic entities closely related to each other, such as manufacturers, distributors and transport companies [75]. The driving force of logistics is demand, and facilities planning, fleet size and vehicle routing need to be planned in the long, medium and short term, respectively [75]. The quantity and variety of materials are limited, the means of transportation are

used for a long time, and the information in the external environment is full and not easy to change [75].

The goal of emergency VRP is to meet the requirements of minimizing the delay time (primary goal) and minimizing the cost (secondary goal) [75]. The distribution network of logistics facilities is temporary, the network structure is simple and the functions are simplified [75]. The main participants are not closely linked to the interests of institutions or organizations, such as government departments, non-governmental organizations, donors and institutions that are temporarily established [75]. The driving force of logistics is divided into two kinds, the reflection stage is system propelling, and the recovery stage is demand promotion [75]. Usually, resource reserve planning is made [75]. In wartime or emergency, material transportation and vehicle scheduling plan are urgent, making the best possible decisions under shorter term and limited information, and the plan scheme will often change greatly in the implementation process [75]. There are the quantity and variety of material stock, the means of transportation are temporarily collected, the information in the external environment is inadequate and easy to change [75].

4 Enhanced MBO algorithm

In this part of our research, we proposed a new variant of the basic MBO approach, called the enhanced MBO (EMBO), that includes a crossover operator and self-adaptive strategy. First, we will describe the main framework of the original MBO approach, and then we will give a full description of the proposed EMBO approach.

Here, t is the current generation. $rand$ is a random number. N_p is the number of butterflies in the population, and p is the ratio of butterflies in Subpopulation 1. BAR is the butterfly adjusting rate. Cr is the crossover rate.

4.1 MBO algorithm

4.1.1 Migration operator

The number of butterflies located at Land 1 and Land 2 can be calculated as $\text{ceil}(p * N_p)$ (NP_1 , Subpopulation 1) and $N_p - NP_1$ (NP_2 , Subpopulation 2), respectively. We can use SP1 and SP2 to denote Subpopulation 1 and Subpopulation 2, respectively. Here, $\text{ceil}(x)$ rounds x to the nearest

integer not less than x . Therefore, when $r \leq p$, then $x_{i,k}^{t+1}$ is generated by the following equation [55]:

$$x_{i,k}^{t+1} = x_{r_1,k}^t, \quad (12)$$

where $x_{i,k}^{t+1}$ is the k th element of x_i , and $x_{r_1,k}^t$ is the k th element of x_{r_1} . Butterfly r_1 is chosen from SP1 in a random fashion. In Eq. 12, r can be given in the following form:

$$r = rand * peri, \quad (13)$$

where $peri$ is the migration period [55]. In comparison, when $r > p$, then $x_{r_1,k}^t$ can be given by

$$x_{i,k}^{t+1} = x_{r_2,k}^t, \quad (14)$$

where $x_{r_2,k}^t$ is the k th element of x_{r_2} , and butterfly r_2 is chosen from SP2 in a random fashion.

4.1.2 Butterfly adjusting operator

For butterfly j , if $rand$ is not more than p , the k th element k can be given as [55]

$$x_{j,k}^{t+1} = x_{best,k}^t, \quad (15)$$

where $x_{j,k}^{t+1}$ is the k th element of x_j . Similarly, $x_{best,k}^t$ is the k th element of the best individual x_{best} . On the other hand, when $rand$ is bigger than p , it can be expressed as

$$x_{j,k}^{t+1} = x_{r_3,k}^t, \quad (16)$$

where $x_{r_3,k}^t$ is the k th element of x_{r_3} . Here, $r_3 \in \{1, 2, \dots, NP_2\}$.

In this case, when $rand$ is bigger than BAR , it can be calculated in another form [55]:

$$x_{j,k}^{t+1} = x_{j,k}^{t+1} + \alpha \times (dx_k - 0.5), \quad (17)$$

where dx is the walk step of butterfly j .

According to the above description, the structure of MBO can be provided in Algorithm 1.

4.2 EMBO algorithm

MBO has been shown to have its own advantages over other intelligent algorithms for benchmarking and other application engineering problems [55]. However, as mentioned before, sometimes MBO may be stuck at local optima on certain problems [55]. In this paper, a self-adaptive strategy and crossover operators were combined with the basic MBO approach for the sake of enhancing the search

Initialization. Set the generation counter $t = 1$, and set the maximum generation t_{\max} , NP_1 , NP_2 , BAR , $peri$, and p ;

Population evaluation. Calculate the fitness according to the objective function;

while $t < t_{\max}$ **do**

Sort the butterfly population;

Divide population into SP1 and SP2;

for $i = 1$ to NP_1 **do**

 Implement migration operator;

end

for $j = 1$ to NP_2 **do**

 Implement butterfly adjusting operator;

end

Calculate the fitness of newly-generated butterfly individuals;

$t = t + 1$;

end

Print the final solution.

Algorithm 1: Monarch Butterfly Optimization

ability of MBO. This enhanced MBO (EMBO) algorithm will be described in detail later in this paper.

4.2.1 Self-adaptive butterfly adjusting operator

One of the most important parameters in the basic MBO algorithm is the butterfly adjusting rate (BAR). In MBO, the value of BAR is the same as for p , which is unchanged during the whole optimization process. Here, a self-adaptive scheme is introduced first to adjust the parameter BAR . The value of BAR changes self-adaptively as the optimization process continues between the initial value BAR_0 and the maximum 1, as given mathematically below:

$$BAR = BAR_0 + (1 - BAR_0) \times \frac{t}{t_{\max}}, \quad (18)$$

where BAR_0 is the initial butterfly adjusting rate; t and t_{\max} are the current and maximum generation, respectively.

From Eq. 18, we can see, though BAR is always changing during the whole MBO process, its value remains in the range $[BAR_0, 1]$.

4.2.2 Crossover operator

As we are aware, for EAs, two of the most important operators are the crossover operator and mutation operator [37], both of which have a great influence on the behavior and performance of EAs [3, 58, 60]. In the present work, we introduced the crossover operator origin-

ally used in EAs to the butterfly adjusting operator of the basic MBO algorithm. The introduced crossover operator fully explores the information of the butterfly individual, which can be given as shown:

$$x_{j2}^{t+1} = x_{j1}^{t+1} \times (1 - Cr) + x_j^t \times Cr \quad (19)$$

where x_{j2}^{t+1} is another butterfly by x_{j1}^{t+1} and x_j^t . For the sake of description, the butterfly individual generated by the standard butterfly adjusting operator is called x_{j1}^{t+1} .

At the same time, the crossover rate (Cr) is a critical factor for how the crossover operator behaves, which determines the performance of the EAs to some extent. A substantial number of strategies have been designed to adjust the crossover rate, with the goal of improving the EAs' search effectiveness. In the present work, a self-adaptive scheme was used to adjust the crossover rate. Therefore, according to the fitness of butterfly j in SP2 ($f(x_j^t)$), the self-adaptive crossover rate can be calculated as shown below.

$$Cr = 0.8 + 0.2 \times \frac{f(x_j^t) - f(x_{best})}{f(x_{worst}) - f(x_{best})}, \quad (20)$$

where x_{best} and x_{worst} are the best and the worst butterfly with the fitness of $f(x_{best})$ and $f(x_{worst})$, respectively. In addition, from Eq. 20, the minimum and maximum of the crossover rate Cr are 0.2 and 0.8, respectively.

Up to now, two butterfly individuals (x_{j1}^{t+1} and x_{j2}^{t+1}) have been generated. Next, we discuss how to select one as the newly-generated butterfly $x_{j,new}^{t+1}$ for the next gener-

ation. In this paper, we used a greedy scheme that could be expressed as

$$x_{j,new}^{t+1} = \begin{cases} x_{j_1}^{t+1}, & f(x_{j_1}^{t+1}) < f(x_{j_2}^{t+1}) \\ x_{j_2}^{t+1}, & f(x_{j_2}^{t+1}) < f(x_{j_1}^{t+1}) \end{cases}, \quad (21)$$

where $f(x_{j_1}^{t+1})$ and $f(x_{j_2}^{t+1})$ are the fitness of the butterfly $x_{j_1}^{t+1}$ and $x_{j_2}^{t+1}$, respectively.

After incorporating the crossover operator and self-adaptive scheme into the butterfly adjusting operator, an updated butterfly adjusting operator, called the self-adaptive butterfly adjusting (SABA) operator, was then proposed, as shown in Algorithm 2.

According to the previous description, the main step of the EMBO algorithm is given in Algorithm 3.

5 The EMBO for emergency VRP with relief materials in sudden disasters

The original MBO approach was designed for continuous optimization problems [55], while the EmVRP studied in this paper is a classical discrete optimization problem. Therefore, the main framework of EMBO must be adjusted in many aspects to tackle the EmVRP, including individual encoding and decoding. Next, we demonstrate how to use EMBO to solve the EmVRP.

5.1 Individual coding and initial solutions construction

In our work, we utilize an improved natural number coding strategy [75]. A butterfly individual is a string representing an emergency relief material transportation scheme. In general, a butterfly individual is also called a chromosome in EAs.

A butterfly individual is made up of two substrings. The first substring has an element that represents the vehicle number. If there are K vehicles, the first element is an integer selected from 1 to K . The second substring has $3n$ elements, and n represents the number of tasks completed by the vehicle. For example, vehicle 2 at parking area 1 arrives at material storage site I_3 to transport material G_1 to the affected area J_2 . Then vehicle 2 goes to material storage site I_1 to transport material G_2 to the affected area J_4 . This process can be represented as $K_1 - I_3 - G_1 - J_2 - I_1 - G_2 - J_4$, and its corresponding butterfly individual can be expressed as 2-3-1-2-1-2-4. The $(3n - 1)$ th ele-

ment represents the number of the material reserve site, the $(3n)$ th element represents the material type number, and the $(3n + 1)$ th element represents the number of the disaster site (affected area). The element segments of all vehicles are arranged in parallel from small to large in order to form a single butterfly individual.

Suppose there are 3 vehicles that are numbered 1, 2, 3, located in the parking lot K_2 , K_1 , and K_3 , respectively; there are 2 materials that are numbered G_1 and G_2 ; there are 2 reserve sites that are numbered I_1 and I_2 ; and there are 3 disaster sites that are numbered J_1 , J_2 , and J_3 . The following butterfly individuals can be generated:

Butterfly individual 1:

$$\left\{ \begin{array}{l} 1 - 2 - 1 - 1 - 1 - 2 - 2 - 2 - 1 - 3 \\ 2 - 1 - 2 - 3 \\ 3 - 2 - 1 - 2 - 1 - 2 - 1 - 1 - 2 - 2 \end{array} \right\} \quad (22)$$

Its corresponding solution is:

$$\left\{ \begin{array}{l} K_2 - I_2 - G_1 - J_1 - I_1 - G_2 - J_2 - I_2 - G_1 - J_3 \\ K_1 - I_1 - G_2 - J_3 \\ K_3 - I_2 - G_1 - J_2 - I_1 - G_2 - J_1 - I_1 - G_2 - J_2 \end{array} \right\} \quad (23)$$

Butterfly individual 2:

$$\left\{ \begin{array}{l} 1 - 1 - 2 - 3 - 1 - 2 - 2 \\ 2 - 3 - 2 - 1 \\ 3 - 1 - 1 - 3 - 1 - 2 - 1 - 2 - 2 - 2 \end{array} \right\} \quad (24)$$

Its corresponding solution is:

$$\left\{ \begin{array}{l} K_2 - I_1 - G_2 - J_3 - I_1 - G_2 - J_2 \\ K_1 - I_3 - G_2 - J_1 \\ K_3 - I_1 - G_1 - J_3 - I_1 - G_2 - J_1 - I_2 - G_2 - J_2 \end{array} \right\} \quad (25)$$

Butterfly individual 1 represents vehicle 1 from parking lot K_2 , which arrives at material storage site I_2 to transport material G_1 to the affected area J_1 . Then vehicle 1 goes to material storage site I_1 to transport material G_2 to the affected area J_2 . Vehicle 2 from parking lot K_1 arrives at material storage site I_1 to transport material G_2 to the affected area J_3 . Vehicle 3 from parking lot K_3 arrives at material storage site I_2 to transport material G_1 to the affected area J_2 , and then vehicle 3 goes to material storage site I_1 to transport material G_2 to the affected area J_2 . When the above transportation tasks have been completed, all requirements of all the affected areas will have been met. Butterfly individual 2 can be explained in the same way.

Calculate the butterfly adjusting rate BAR by using Eq. 18.

```

for  $j = 1$  to  $NP_2$  do
  Compute the walk step  $dx$ .
  Calculate the weighting factor.
  for  $k = 1$  to  $D$  do
    if  $rand \leq p$  then
      | Generate  $x_{j1,k}^{t+1}$  by Eq. 15.
    end
    Choose a butterfly in SP2 (say  $r_3$ ) in a random fashion.
    Generate  $x_{j1,k}^{t+1}$  by Eq. 16.
    if  $rand > BAR$  then
      |  $x_{j1,k}^{t+1} = x_{j1,k}^{t+1} + \omega \times (dx_k - 0.5)$ .
    end
  end
  Generate  $x_{j2}^{t+1}$  by implementing crossover operator by Eq. 19.
  Generate  $x_{j,new}^{t+1}$  through greedy strategy by Eq. 21.
end

```

Algorithm 2: SABA operator

Initialization. Set the generation counter $t = 1$, and set the maximum generation t_{\max} , NP_1 , NP_2 , BAR_0 , $peri$, and p .

Population evaluation. Evaluate the butterfly individuals with their objective functions.

```

while  $t < t_{\max}$  do
  Sort the butterfly population.
  Divide population into SP1 and SP2.
  for  $i = 1$  to  $NP_1$  do
    | Generate  $x_{i,new}^{t+1}$  by implementing migration operator.
  end
  For all individuals in SP2, implement the updated butterfly adjusting operator to generate  $x_{j,new}^{t+1}$  as Algorithm 2.
  Evaluate the butterfly population.
   $t = t + 1$ .
end
Print the final solution.

```

Algorithm 3: EMBO approach

Now, we will describe how to generate the initial solutions. First, vehicle l is selected randomly from the parking areas. This selection will be considered the starting point. Second, the reserve site S_i ($i = 1, 2, \dots, n$) is selected randomly from reserve site set \mathbf{S} . Finally, the affected area D_j ($j = 1, 2, \dots, m$) is selected randomly from the affected area set \mathbf{D} . This selection process is repeated until a whole butterfly individual is constructed, so the initial solution of the EmVRP is obtained. After all the butterfly individuals have been generated, the initial butterfly population is formed.

5.2 The EMBO for emergency VRP with relief materials in sudden disasters

In this section, we discuss how to use EMBO to solve the EmVRP with relief materials in sudden disasters. First, the initialization process is implemented, including the parameters and initial population, as described previously. Next, the optimization process is implemented to update butterfly individuals in the population. Then the newly generated butterfly individuals are evaluated according to the objective functions. The implementation of the EMBO algorithm is repeated until the given requirements are met. Finally, the optimal butterfly individual is decoded in order to get the final solution scheme for the

EmVRP with relief materials in sudden disasters as given in Algorithm 4.

In Algorithm 4, Line 4 encoding is essentially the population initialization process needed so that the EMBO algorithm can solve the EmVRP. Through this encoding, the initial population is generated. Line 4 describes the decoding process that transforms the butterfly individual into the actual solution scheme for the EmVRP. Encoding and decoding are opposite processes.

6 Simulation results

In this portion of our work, we used the proposed EMBO algorithm to solve the EmVRP with relief materials in sudden disasters. In addition, to show the advantages of the EMBO algorithm, we performed several studies comparing the basic MBO algorithm with seven other intelligent algorithms. Finally, to show the robustness of the proposed EMBO algorithm, we reviewed the effects of parametric settings on the performance of EMBO.

6.1 An EmVRP with relief materials in sudden disasters (case 1)

To test our approach, we solved a hypothetical EmVRP with relief materials in a sudden-onset disaster [75] that can be described as follows. Suppose a sudden natural disaster occurred. There are 4 disaster spots in need of emergency materials. These locations can be identified as J_1, J_2, J_3 , and J_4 , respectively. The relief materials have been transported to the local airport and railway station by aircraft and railway. There are a total of 3 reserve sites, denoted by I_1, I_2 , and I_3 , respectively, including the airport and railway station together with the local relief supply reserve area. A total of 20 vehicles are collected, and they are located randomly in 3 parking locations numbered K_1, K_2 , and K_3 . There are 4 kinds of materials to be delivered: tents, quilts, clothing, and food, represented as G_1, G_2, G_3 , and G_4 , respectively. The number of tasks to be completed by each vehicle is not more than 5. Tables 1-5 provide the related information for the above EmVRP example.

Table 3: The demand of emergency supplies in every affected point.

Affected point	Tent	Quilt	Clothes	Food
J_1	2000	10000	6000	3000
J_2	5000	20000	6000	8000
J_3	3000	10000	8000	4000
J_4	4000	10000	6000	5000

Table 4: Reserves of emergency supplies in every reserve point.

Reserve point	Tent	Quilt	Clothes	Food
I_1	4000	200000	8000	8000
I_2	3000	10000	6000	4000
I_3	8000	20000	12000	9000

Table 5: The distance between every point.

Distance (km)	I_1	I_2	I_3	J_1	J_2	J_3	J_4
K_1	45	60	70				
K_2	60	50	80				
K_3	70	80	60				
I_1				60	50	70	80
I_2				70	60	55	65
I_3				100	80	50	60

6.2 The shortest time used by nine algorithms on the EmVRP with relief materials in sudden disasters

For the sake of carrying out a fair comparison, all the approaches were compiled using MATLAB R2017a (9.2) running under the Windows 10 Enterprise operating system on a PC with an Intel(R) Core(TM) i5-4590 CPU operating at 3.30 GHz, 8.00GB of RAM, and a hard drive of 1024 GB.

In all experiments for MBO and EMBO, we used the same parameter settings: probability $p = 5/12$, elitism number $Keep = 2$, $BAR_0 = (\sqrt{5}-1)/2$, population size $N_P = 50$, dimension $D = 320$, and maximum generation $t_{\max} = 100$.

In this paper, the proposed EMBO algorithm will be compared with seven intelligent algorithms when dealing with emergency vehicle routing problem with relief materials in sudden disasters. The seven comparative algorithms

Initialization. Set the generation counter $t = 1$, and set the maximum generation $t_{\max}, NP_1, NP_2, BAR_0, peri$, and p .

Encoding. Initialize the population according to the encoding method in Section 5.1.

Population evaluation. Calculate the shortest time used by each butterfly individual.

while $t < t_{\max}$ **do**

Sort the butterfly population.

Divide population into SP1 and SP2;

for $i = 1$ to NP_1 **do**

 Generate $x_{i,new}^{t+1}$ by implementing migration operator.

end

For all individuals in SP2, implement the updated butterfly adjusting operator to generate $x_{j,new}^{t+1}$ as Algorithm 2.

Calculate the shortest time used by each butterfly individual.

$t = t + 1$.

end

Decoding. Decode the optimal butterfly individual in order to get the final best solution scheme for the emergency VRP.

Print the final optimal scheduling scheme solution.

Algorithm 4: EMBO algorithm for emergency VRP with relief materials in sudden disasters

Table 1: Related parameters of vehicles.

Vehicle number	Parking lot	Speed (km/h)	Load capacity (ton)	Volume (m ³)
1	K ₂	50	4	30
2	K ₁	45	5	34
3	K ₂	55	3	27
4	K ₃	40	6	40
5	K ₁	50	4	30
6	K ₂	55	3	27
7	K ₃	35	7	45
8	K ₂	50	4	30
9	K ₁	45	5	34
10	K ₂	45	5	34
11	K ₃	40	6	40
12	K ₁	45	5	34
13	K ₂	55	3	27
14	K ₃	40	6	40
15	K ₁	50	4	30
16	K ₂	55	3	27
17	K ₃	35	7	45
18	K ₂	50	4	30
19	K ₁	45	5	34
20	K ₂	45	5	34

can be described below. ABC (artificial bee colony) [25] is an intelligent optimization algorithm based on the smart behavior of honey bee swarm. BA (bat algorithm) [17] is a new powerful and efficient meta-heuristic optimization algorithm inspired by the echolocation behavior of bats with varying pulse rates of emission and loudness. BBO

(biogeography-based optimization) [42] is a new evolution algorithm developed for the global optimization inspired by the immigration and emigration of species between islands (or habitats) in search of more compatible islands. CS (cuckoo search) [69] is a meta-heuristic optimization algorithm inspired by the obligate brood parasitism of some

Table 2: Related parameters of emergency supplies.

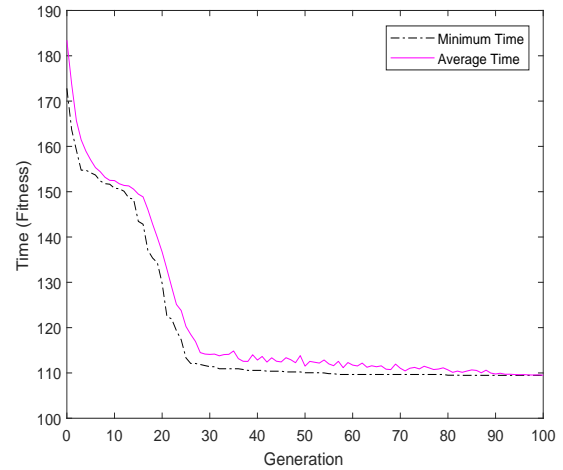
Materials	Tent	Quilt	Clothes	Food
Weight (<i>kg</i>)	30	6	5	10
Volume (<i>m</i> ³)	1.1	0.15	0.3	0.5
Unit material loading (unloading) time (<i>min</i>)	0.2	0.2	0.1	0.1

cuckoo species by laying their eggs in the nests of other host birds (of other species). DE (differential evolution) [43] is a simple but excellent optimization method that uses the difference between two solutions to probabilistically adapt a third solution. An ES (evolutionary strategy) [2] is an algorithm that generally distributes equal importance to mutation and recombination, and that allows two or more parents to reproduce an offspring. PSO (particle swarm optimization) [26, 71, 72] is also a swarm intelligence algorithm which is based on the swarm behavior of fish, and bird schooling in nature.

The parameters for the other seven algorithms were set as follows.

- For ABC, the population size $N_p = 50$, the number of food sources $FoodNumber = N_p/2$, maximum search times $limit = 100$.
- For BA, loudness $A = 0.5$, pulse rate $r = 0.5$, and scaling factor $\varepsilon = 0.001$.
- For BBO, habitat modification probability = 1, immigration probability bounds per gene = [0, 1], step size for numerical integration of probabilities = 1, maximum migration rate for each island = 1, and mutation probability = 0.005.
- For CS, the discovery rate $p_a = 0.25$.
- For DE, the weighting factor $F = 0.5$, and crossover constant $CR = 0.5$.
- For ES, the number of offspring produced in each generation $\lambda = 10$, and the standard deviation for changing solutions is $\sigma = 1$.
- For PSO, the inertial constant = 0.3, the cognitive constant = 1, and the social constant for swarm interaction = 1.

For one implementation of EMBO, the convergent trend of the best and average time of the EMBO approach is shown in Fig. 2. In Fig. 2, the best and mean time after 100 generations were 109.4341 and 109.489, respectively. Furthermore, the EMBO algorithm converged to the least time after about 20 generations. These findings indicated that the EMBO algorithm could solve the emergency VRP problem well.

**Figure 2:** The convergent trend of the best and average time for EMBO algorithm.

In addition, the shortest time over 30 independent runs was obtained by EMBO and the eight other intelligent algorithms, and the results are displayed in Table 6. From Table 6, although EMBO had the biggest std value, it is clear that EMBO was able to complete the task with the least time among the nine intelligent algorithms for the average, best, and worst performance. For the other eight intelligent algorithms, BBO, CS, and DE had similar performances that were inferior only to the EMBO algorithm. Also, MBO performed similarly to PSO, which was better than ABC, BA, and ES.

The convergent trend of the average time obtained by the nine algorithms is shown in Fig. 3. From Fig. 3, it is clear that EMBO converged in the fastest fashion among the nine intelligent algorithms. This convergent trend was consistent with the results provided in Table 6.

6.3 Another EmVRP with relief materials in sudden disasters (case 2)

Like case 1 studied in Section 6.1, another emergency VRP problem is further used to verify our proposed EMBO algorithm. In case 2, there are 5 disaster spots in need of

Table 6: The least time used by nine intelligent algorithms for the emergency VRP with relief materials in sudden disasters.

	ABC	BA	BBO	CS	DE	EMBO	ES	MBO	PSO
Best	158.31	154.10	142.64	143.43	142.52	109.06	163.93	152.08	157.19
Mean	162.96	161.27	145.69	145.26	144.68	118.18	165.89	154.51	159.03
Worst	167.35	167.86	148.29	150.21	146.10	140.77	167.25	158.24	162.23
Std	2.2516	3.1246	1.6231	1.3777	0.8202	13.2842	0.8953	1.5353	1.4138

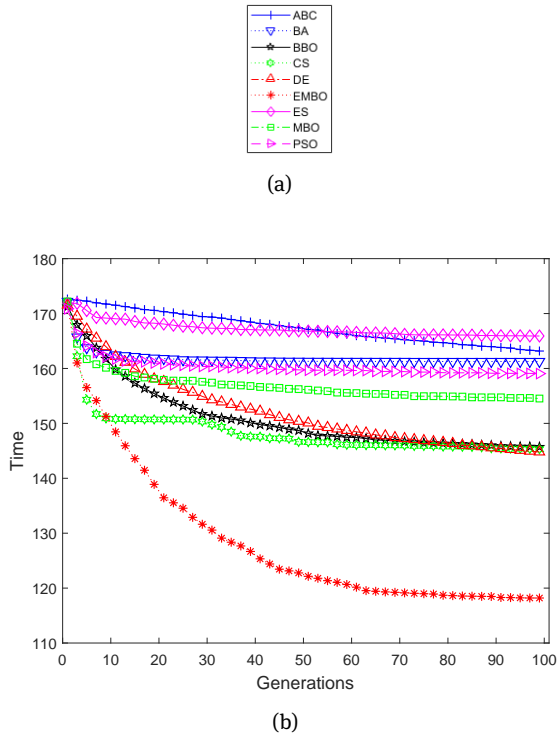


Figure 3: Results obtained by nine algorithms.

emergency materials. These locations can be identified as $J_1, J_2, J_3, J_4,$ and $J_5,$ respectively. The relief materials have been transported to the local airport and railway station by aircraft and railway. There are a total of 4 reserve sites, denoted by $I_1, I_2, I_3,$ and $I_4,$ respectively. A total of 25 vehicles are collected, and they are located randomly in 3 parking locations numbered $K_1, K_2,$ and $K_3.$ There are 4 kinds of materials to be delivered: tents, quilts, clothing, and food, represented as $G_1, G_2, G_3,$ and $G_4,$ respectively. The number of tasks to be completed by each vehicle is not more than 5. The parameters of emergency supplies used in case 2 is the same with case 1, as shown in Table 2. Tables 7-10 provide the other related information for case 2.

Table 8: The demand of emergency supplies in every affected point for case 2.

Affected point	Tent	Quilt	Clothes	Food
J_1	3000	9000	7000	4000
J_2	6000	19000	7000	7000
J_3	4000	9000	9000	5000
J_4	5000	9000	7000	4000
J_5	4000	11000	6500	5000

Table 9: Reserves of emergency supplies in every reserve point for case 2.

Reserve point	Tent	Quilt	Clothes	Food
I_1	5000	19000	9000	9000
I_2	4000	11000	7000	5000
I_3	9000	21000	11000	10000
I_4	7000	20000	10000	9000

Table 7: Related parameters of vehicles for case 2.

Vehicle number	Parking lot	Speed (km/h)	Load capacity (ton)	Volume (m ³)
1	K ₁	45	5	34
2	K ₂	45	5	34
3	K ₃	50	4	30
4	K ₂	35	7	45
5	K ₁	55	3	27
6	K ₃	50	4	30
7	K ₂	40	6	40
8	K ₁	55	3	27
9	K ₃	45	5	34
10	K ₂	40	6	40
11	K ₁	45	5	34
12	K ₂	45	5	34
13	K ₃	50	4	45
14	K ₂	35	7	27
15	K ₁	55	3	30
16	K ₃	50	4	40
17	K ₂	40	6	27
18	K ₁	55	3	34
19	K ₂	45	5	30
20	K ₂	50	4	28
21	K ₁	45	5	29
22	K ₂	55	3	38
23	K ₃	50	6	43
24	K ₂	40	3	31
25	K ₁	55	5	37

Table 10: The distance between every point for case 2.

Distance (km)	l ₁	l ₂	l ₃	l ₄	J ₁	J ₂	J ₃	J ₄	J ₅
K ₁	50	65	70	75					
K ₂	65	55	50	85					
K ₃	75	85	65	65					
l ₁					55	55	70	75	60
l ₂					65	65	60	60	55
l ₃					95	85	55	55	80
l ₄					65	55	60	70	90

For the software, hardware environments and parameter settings used in nine intelligent algorithms, they are the same with case 1.

In addition, the shortest time over 30 independent runs was obtained by EMBO and the eight other intelligent algorithms, and the results are displayed in Table 11. From Table 11, it is clear that EMBO was able to complete the task with the least time among the nine intelligent algorithms for the average, best, and worst performance. Also, EMBO

had the smallest Std value for this case. For the other eight intelligent algorithms, BBO, BA, and MBO had similar performances that were inferior only to the EMBO algorithm. Comparing with case 1, EMBO algorithm takes less time to complete the task, and the reason is that five more vehicles are added to case 2.

Table 11: The least time used by nine intelligent algorithms for case 2.

	ABC	BA	BBO	CS	DE	EMBO	ES	MBO	PSO
Best	137.03	96.13	91.00	102.65	104.84	85.66	114.38	93.72	119.67
Mean	148.29	113.33	95.38	108.85	113.96	86.39	119.28	99.19	140.33
Worst	164.45	126.22	100.37	110.78	125.30	87.97	122.79	104.32	155.02
Std	6.6743	6.9830	2.0991	1.5518	5.4081	0.5022	2.1377	2.6460	7.4307

6.4 Parameter study

As we are aware, for all the intelligent algorithms, the parameter setting is of significant importance to their performance. In this section, the effectiveness of the initial butterfly adjusting rate BAR_0 , probability p , elitism $Keep$, population size N_p , and maximum generation t_{max} are analyzed for the proposed EMBO algorithm on case 1.

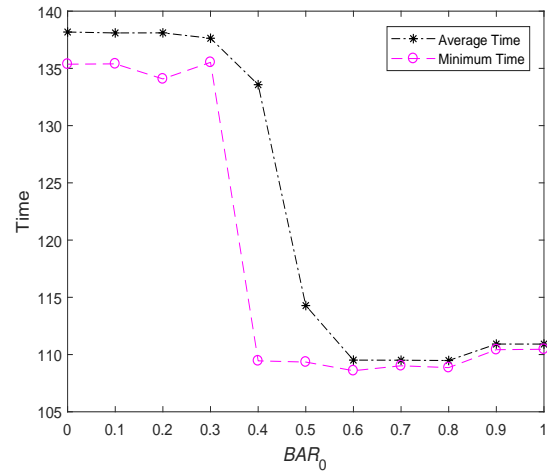
6.4.1 Influence of the initial butterfly adjusting rate BAR_0 for EMBO

First, we examined the initial butterfly adjusting rate BAR_0 . The other parameters were set as follows: elitism number $Keep = 2$, probability $p = 5/12$, population size $N_p = 50$, and maximum generation $t_{max} = 100$. The final times required by EMBO with different values of BAR_0 were recorded as shown in Table 12 and Fig. 4. From Table 12, when BAR_0 was equal to 0.6 or 0.7, EMBO could find the optimal scheduling scheme with the least time. Looking carefully at Fig. 4, we can observe that the performance of EMBO was significantly improved with the increment of BAR_0 . However, EMBO had a similar performance when BAR_0 was between 0.6 and 1.0. Considering matters overall, we set the initial butterfly adjusting rate BAR_0 to $(\sqrt{5}-1)/2$ for this present work.

It should be mentioned that the initial butterfly adjusting rate BAR_0 was between 0 and 1.0. When the initial butterfly adjusting rate $BAR_0 = 0$, the updating Eq. 18 would degenerate into the following equation:

$$BAR = \frac{t}{t_{max}}. \quad (26)$$

In this case, the butterfly adjusting rate BAR is changing in a linear fashion. On the other hand, when the initial butterfly adjusting rate $BAR_0 = 1.0$, the butterfly adjusting rate BAR is equal to the initial butterfly adjusting rate BAR_0 . The butterfly adjusting rate BAR will not change during the whole optimization process. Essentially, this description fits a basic MBO algorithm.

**Figure 4:** Results obtained by EMBO with different BAR_0 .

6.4.2 Influence of the probability p for EMBO

In EMBO, there is another probability p that decides the number of NP_1 and NP_2 . In other words, there are NP_1 and NP_2 butterflies that implement the migration operator and butterfly adjusting operator, respectively. Here, we studied the probability p . The other parameters were set as follows: population size $N_p = 50$, the initial butterfly adjusting rate $BAR_0 = (\sqrt{5}-1)/2$, elitism number $Keep = 2$, and maximum generation $t_{max} = 100$. The final times achieved by EMBO with different p are shown in Table 13 and Fig. 5. From Table 13, when probability p was equal to 0.7, 0.8 or 0.9, we see that EMBO could find the optimal scheduling scheme with the least time. Examining Fig. 5 carefully, we can observe that the performance of EMBO improved significantly with the increment of p . However, EMBO had a similar performance when p was between 0.5 and 1.0. Considered overall, the probability p was set to $5/12$ in this paper.

It should be mentioned that the probability p was between 0.1 and 0.9. For MBO, when probability $p = 0$, all the individuals will be updated only by the butterfly adjusting operator. When probability $p = 1.0$, all the individuals will be updated only by the migration operator.

Table 12: The least time used by the proposed EMBO algorithm for the EmVRP with relief materials in sudden disasters with different BAR_0 .

	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
Best	135.36	135.39	134.07	135.52	109.44	109.34	108.58	109.02	108.85	110.42	110.46
Mean	138.17	138.09	138.10	137.63	133.57	114.28	109.51	109.51	109.47	110.91	110.91
Worst	140.69	140.84	140.55	139.91	140.86	137.88	110.14	109.94	109.94	111.03	111.03
Std	1.5266	1.3504	1.3326	0.8532	9.7697	10.3059	0.3526	0.2779	0.3323	0.1675	0.1856

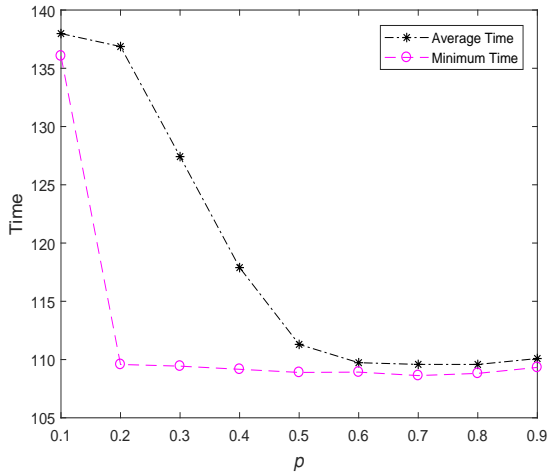


Figure 5: Results obtained by EMBO with different p .

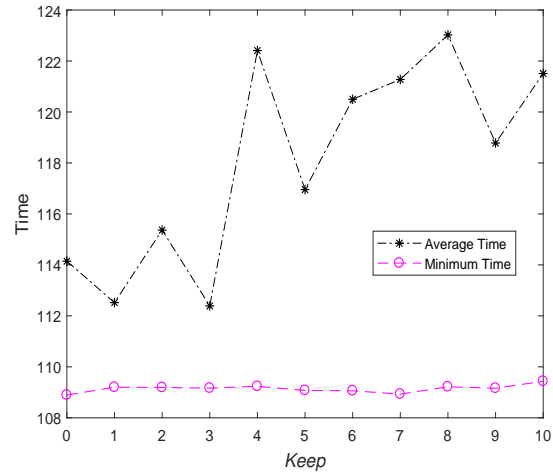


Figure 6: Results obtained by EMBO with different $Keep$.

No special attention was paid to these two extreme cases of $p = 0$ and $p = 1.0$.

6.4.3 Influence of the elitism $Keep$ for EMBO

As we can see, most intelligent algorithms involve an elitism strategy that has a great influence on the performance. Here, the elitism $Keep$ was studied in the range of $[0, 10]$. The other parameters were set as follows: probability $p = 5/12$, initial butterfly adjusting rate $BAR_0 = (\sqrt{5}-1)/2$, population size $N_p = 50$, and maximum generation $t_{max} = 100$. The final times attained by EMBO with different $Keep$ values are shown in Table 14 and Fig. 6. From Table 14, when the parameter $Keep$ was equal to 0, 3 or 8, EMBO could find the optimal scheduling scheme with the least time. Looking carefully at Fig. 6, though the trend of EMBO is less obvious, generally speaking the performance of EMBO improved with the increment of $Keep$. However, on average, EMBO had a similar performance when $Keep$ was equal to 1 and 3. Therefore, we set the elitism $Keep$ to 2 for this research.

6.4.4 Influence of the population size N_p for EMBO

Subsequently, we studied the population size N_p in the range of $[10, 100]$ with interval 10. The other parameters were set as follows: the initial butterfly adjusting rate $BAR_0 = (\sqrt{5}-1)/2$, probability $p = 5/12$, elitism number $Keep = 2$, and maximum generation $t_{max} = 100$. The final times obtained by EMBO with different N_p were recorded as shown in Table 15 and Fig. 7. From Table 15, when population size N_p was equal to 90, 100, 20, and 10, EMBO could find the optimal scheduling scheme with the least time. Examining Fig. 7, we can observe that the performance of EMBO decreased and then improved with the increment of N_p . Furthermore, overall the proposed EMBO algorithm was capable of obtaining satisfactory solutions within a reasonable time when the population size $N_p = 10$. Under this condition, fewer computational resources were required, indicating that EMBO could solve the EmVRP while consuming only limited computational resources. Considered altogether, we set the population size N_p to 50 in our present work.

Table 13: The least time used by the proposed EMBO algorithm for the emergency VRP with relief materials in sudden disasters with different p .

	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Best	136.05	109.57	109.43	109.16	108.89	108.92	108.62	108.81	109.33
Mean	137.97	136.86	127.41	117.89	111.30	109.73	109.58	108.58	110.08
Worst	140.56	141.69	139.68	139.36	138.08	116.14	110.47	110.54	110.67
Std	1.0755	7.4311	13.6690	12.6734	6.4444	1.2843	0.3514	0.4003	0.3664

Table 14: The least time used by the proposed EMBO algorithm for the emergency VRP with relief materials in sudden disasters with different $Keep$.

	0	1	2	3	4	5	6	7	8	9	10
Best	108.89	109.19	109.19	109.16	109.23	109.07	109.06	108.92	109.21	109.15	109.43
Mean	114.14	112.52	115.36	112.39	112.40	126.95	120.49	121.27	123.02	118.78	121.51
Worst	137.74	137.92	139.75	137.83	138.34	138.35	138.55	138.79	137.49	137.94	139.17
Std	10.2456	8.4974	11.5944	8.4129	13.8968	12.2843	13.5096	13.5515	13.6949	13.0870	13.5949

Table 15: The least time used by the proposed EMBO algorithm for the emergency VRP with relief materials in sudden disasters with different N_p .

	10	20	30	40	50	60	70	80	90	100
Best	110.25	109.63	109.16	109.19	109.20	109.16	109.16	108.89	108.85	108.85
Mean	111.38	111.37	111.95	112.60	114.34	118.55	119.17	115.55	115.27	117.76
Worst	116.17	139.58	139.23	137.49	139.86	138.85	137.51	136.82	135.96	135.97
Std	1.8294	5.4166	7.2907	8.3299	10.4997	12.9187	13.0635	11.3207	10.9097	12.2106

Table 16: The least time used by the proposed EMBO algorithm for the emergency VRP with relief materials in sudden disasters with different t_{max} .

	20	40	60	80	100	120	140	160	180	200
Best	110.09	109.65	109.39	108.59	109.06	109.20	108.89	109.12	109.12	108.85
Mean	110.68	110.32	109.85	114.43	112.41	116.01	116.56	117.99	122.81	120.91
Worst	111.03	114.64	110.30	141.23	139.51	137.50	138.50	136.32	135.83	136.52
Std	0.2450	0.8589	0.2236	10.8763	8.7851	11.6742	11.7442	12.2216	12.6813	12.3809

6.4.5 Influence of the maximum generation t_{max} for EMBO

Last, we studied the maximum generation t_{max} in the range of [20, 200] with interval 20. The other parameters were set as follows: the initial butterfly adjusting rate $BAR_0 = (\sqrt{5}-1)/2$, elitism number $Keep = 2$, probability $p = 5/12$, and population size $N_p = 50$. The final times used by EMBO with different t_{max} are shown in Table 16 and Fig. 8. From Table 16, when the maximum generation t_{max} was equal to 80, 60, and 60, EMBO was able to get the optimal scheduling scheme with the least time. Looking

carefully at Fig. 8, generally the performance of EMBO was significantly reduced with the increment of t_{max} . However, when t_{max} was equal to 20, 40, and 60, EMBO provided better performance than at the other t_{max} values. This finding goes against common expectations. For most intelligent algorithms, their performance will exceed, or at least be equal to, the performance given before the increment of generations. We propose the reason for this finding is that maximum generation t_{max} has an influence on the value of the butterfly adjusting rate BAR , which, in turn, has a big impact on MBO's performance. Under this condition, the situation becomes complicated. Considered as a whole, we

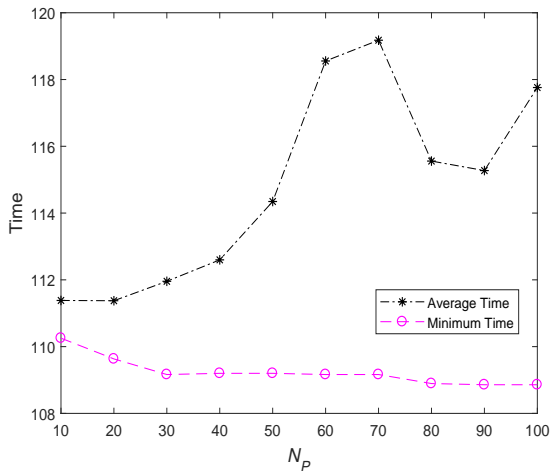


Figure 7: Results obtained by EMBO with different N_P .

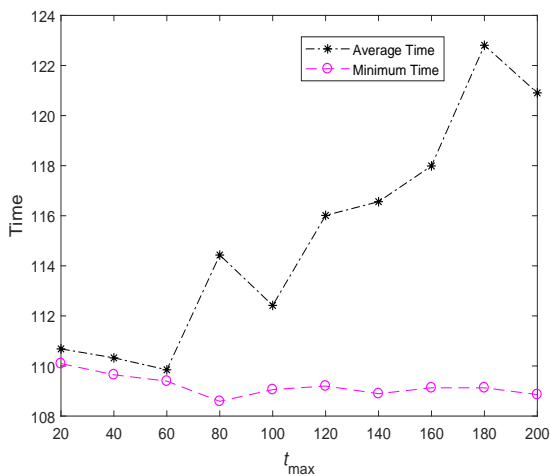


Figure 8: Results obtained by EMBO with different t_{max} .

set the maximum generation t_{max} to 100 in our present work.

7 Conclusions

In this paper, we constructed a model of the EmVRP (emergency vehicle routing problem) with relief materials in sudden disasters, and then solved the problem using the intelligent EMBO algorithm. For EMBO, we incorporated two modifications into the basic MBO algorithm: a self-adaptive strategy and a crossover operator. Our experiments using two examples EmVRP with relief materials in a sudden-onset disaster proved the suitability of EMBO. In addition, an array of comparative studies showed that the proposed EMBO algorithm can achieve satisfactory solu-

tions in less time than the basic MBO algorithm and seven other intelligent algorithms.

Consistent with our interest in the EmVRP with relief materials in sudden disasters, we look toward the following future work. First, more efficient optimization strategies, such as a self-adaptive strategy, should be incorporated into our original approach, thereby allowing the method to solve the EmVRP more efficiently and accurately. Second, new methods should be designed to solve the EmVRP with relief materials in sudden disasters. Third, the performance of EMBO should be studied and analyzed further for cases where the probability p is equal to 0 and 1.00. Fourthly, the performance of the basic MBO algorithm should be studied and analyzed more extensively with regard to the probability p and other parameters. Fifthly, in the current work, though the crossover rate is changed during the search process, it does not take into account the state of the search process. In our future research, the state of the search process should be taken into account and a more intelligent crossover operator should be developed. Sixthly, in our current work, the emergency VRP is just solved by our proposed MBO algorithm. That is to say, in this version of the paper there is no an equilibrium between methods and decision making processes. In our future work, we will build the equilibrium between methods and decision making processes. Seventhly, in our current work, all the parameters fall into the small range, therefore, try-and-error method can well solve it. In our future work, if there are more complicated parameters to be adjusted, irace and other parametric techniques will be used. At last, in our current work, we just use our proposed MBO algorithm to solve the relatively idealized mathematical model. So, other factors is canceled in our current work. In our future work, we will reconsider these factors to our mathematical model (such as congestion or unreliable road network [28, 40, 45]), which is much closer to real world problems. Eighth, for other road network, like grid of streets [31, 66], we will study them in our future studies. Ninth, we will learn from other models (like [1]) to improve the model used in our current work. These studies will contribute to the best implementation of MBO and EMBO.

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