

Research Article

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Comparison of energy parameters of a centrifugal pump with a multi-piped impeller in cooperation either with an annular channel and a spiral channel

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Abstract: The article presents results of numerical analyzes, which raise a subject of influence of the cooperation the multi-piped impeller with a rationalized flow geometry of annular casing and volute casing for liquid flow through centrifugal pump and their operating parameters in the extremely low specific speed $n_q < 10$. The multi-piped impeller (patented by authors) is a major alternative to classic vane impellers. The stator type is responsible for the conversion of the kinetic energy of the liquid by the impeller outlet into potential energy, which determines the overall efficiency of the pump. Also, the article presents qualitative and quantitative verification of results obtained by computer modeling and an attempt to estimate their accuracy. The article focuses mainly on the comparison of the performance parameters of the pump with a multi-piped impeller in cooperation with two stator types with a rationalized flow geometry. Both outlet elements were tested in various configurations of constructional features. The complexity of the construction of the stator can significantly affect the manufacturing costs of pump unit. Knowledge concerning construction of hydraulic elements of centrifugal pumps working in the range of parameters corresponding specific speed ($n_q < 10$) is insufficient. As shown in the paper, the annular type casing model pump cooperating with a multi-piped impeller, designed in accordance with literature, reached far poorer operating parameters than the rational annular construction in a configuration with the same impeller.

Keywords: Centrifugal pump, multi-piped impeller, annular casing, volute casing, CFD

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Nomenclature

β_{cw}	start angle of a spiral volute tongue [deg]
ϵ	convergence criterion
η_c	total efficiency
η_h	hydraulic efficiency
η_m	mechanical efficiency
η_v	volumetric efficiency
ω	angular velocity [rad/s]
ρ	density [kg/m ³]
b_{3kk}	width of an annular casing [mm]
b_{3sp}	width of volute casing [mm]
b_3	width of a volute casing inlet [mm]
d_4	outer diameter of a stator [mm]
g	acceleration due to gravity [m/s ²]
H_u	total pump head [m]
M_t	total moment on the impeller rotating surfaces [Nm]
n	rotational speed [rpm]
n_q	kinematic specific speed ($n_q = n$) [rpm]
p	ambient pressure [Pa]
p_{cin}	total pressure in an impeller inlet section [Pa]
p_{cout}	total pressure in a pump outlet section [Pa]
P_h	hydraulic power [W]
P_w	power on a pump shaft [W]
Q	flow rate [m ³ /h]
Re	Reynolds number
t_s	time step [s]
u_x	velocity in direction X [m/s]
v_a	average fluid velocity in stator [m/s]

1 Introduction

In order to improve the design of stators of centrifugal pumps, a better understanding of the flow of such machines is required. This paper deals with the experimental and theoretical study of the flow in the two types of

stators (annular casing and volute casing) of a low specific speed centrifugal pump. Similar research have been performed in article [1] but for classical blade impellers. The role of the outlet stator becomes particularly important when considering innovational and untypical constructions of the centrifugal impeller. An example of such a construction is a multi-piped impeller whose name (proposed by the authors) and conception of working has been developed and patented [2] during development with hole impeller (Figure 1a) – hole impeller have been known, researched and used for a long time [3, 4]. The multi-piped impeller (Figure 1b) is completely new idea of design centrifugal pump rotors. This construction works in a range of ultra low specific speed $n_q < 10$ (def. n_q according [3, 4]). It uses the classical centrifugal liquid flow through the internal channels of the impeller as well as the additional external flow associated with the phenomenon of flow around the pipes to transfer energy.

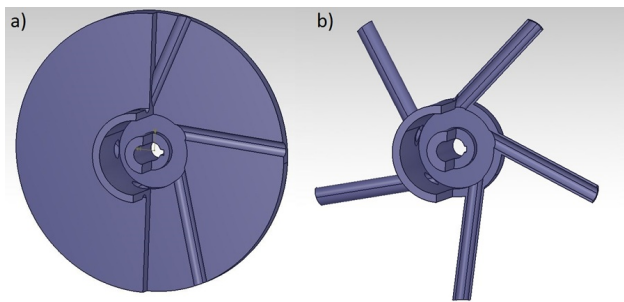


Figure 1: Comparison of geometry of rotors of special centrifugal pumps: a) hole impeller, b) multi-piped impeller

The centrifugal pump from a hydraulic point of view consist of two main elements: an impeller responsible for changing mechanical energy of the motor to hydraulic energy and the stator which the following functions:

- it converts kinetic energy of the liquid after the rotor outlet into potential energy. The efficiency of this alteration largely determines performance of the whole pump.
- It collects liquid flowing out of the impeller and carries it to the outlet of the pump or to the inlet of the next stage rotor in multistage pumps.
- Flow area of that element determines the BEP (Best Efficiency Point) location on the pump characteristic.

Centrifugal pump with multi-piped impeller cooperating with a proper choice and design of the stator is an interesting alternative to classical blade impellers both from

operating parameters and costs of manufacturing (especially working in ultra low specific speed $n_q < 10$). This pumps could be used in chemical industry (pumping corrosive liquids), petrochemical industry (pumping gasoline or diesel), automation systems (micro-pumps for hydraulic cylinders) or firefighting.

In the literature [3] the author claims that for pumps with low and extremely low specific speed it is better to apply a channel of a constant and simple cross-section than a different stator type, since together with the decrease of n_q the difference in efficiency between an annular channel and volute casing diminishes, so that at specific speed $n_q < 12$ the annular channel could represent higher efficiency. It is important, that, to make such a channel with the highest surface quality which guarantees losses reduction at the process of momentum exchange. This claim was verified by authors later in the article.

In order to evaluate the concept of using a multi-piped impeller in centrifugal pumps, comparative experimental investigations of hole impeller and multi-piped rotors were conducted [5]. In addition, preliminary CFD analysis were conducted to identify the flow phenomena associated with the flow around the pipes in the rotor. Based on many research performed by authors – both experimental research prepared at the laboratory rig and a numerical analysis – which raised issues of hole impellers and multi-piped impellers, could be conclude that second rotor generates 30% total head pump H_u more than hole rotor (the same amount and width b_2 of flow channels was maintained in both construction). As a result, it is possible to optimize the geometry of the impeller as for example by reduction in outer diameter d_2 of the impeller for the same energy parameters as in the hole rotor. (total head pump H_u and pump capacity Q).

The essence of the multi-piped impeller work is related to phenomena occurred during the external liquid flow around outer surface of flow channels of the impeller. No information was found in the literature, apparently, this topic has not been tested so far. At the very beginning, authors of article thought of two different theories (both based on the liquid circulation around the profile – in this case cylindrical channel). The first is related to the generated resistance force in the concept of the aerodynamic flow of the airfoil. It is more true for propeller pumps. The second idea – more probably – is based on the theory of vortex pumps with lateral channel accordance with literature [6]. The fluid flow around the impeller pipes (flow channels) generates strong vortex of liquid. It is visible through vortex paths behind the flow channels – similar to Karman vortex streets presented in Figure 2 (for average

fluid velocity $v_a = 6 \text{ m/s}$ in stator of a base model pump, Re was about $59 \cdot 10^3$).

This study aims at modelling a flow in a pump with an annular channel and a spiral channel (in cooperate with multi-piped impeller) using CFD and verifying a numerical model against experimental data. The verified numerical model will be used for identifying the flow phenomena in such a construction and for further research aimed at determining the impact of geometrical features of such a stator on the operating parameters and efficiency of the process of transferring liquid energy.

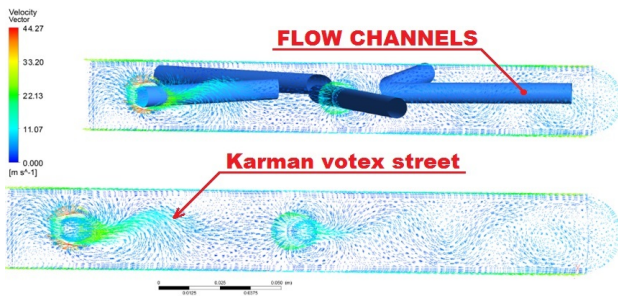


Figure 2: Vortex paths associated with the phenomenon of external flow around the pipes of impeller

2 Test rig and object of research

A basic object of the research is a stator of model pump in cooperation with multi-piped impeller with rectilinear pipes (flow channels) inclined at an angle of 60° to the rotor axis. The geometry of impeller was presented in Figure 1b (dimensions were presented in article [5]). Base type of stator used in construction of model pump of the test rig is annular casing whose dimensions was presented in Figure 3.

In order to verify the results of whole numerical calculations experimental tests on a test rig (Figure 4a) were scheduled and conducted. Measuring instruments applied to measure proper physical qualities on the test rig were included in Table 1 together with the range and accuracy class. More details concerning the test rig as well methodology of measurements can be found in the publication of the authors [5]. The main element of the test rig was a module pump (Figure 4b) designed in a way which would allow a fast exchange of flow elements (impellers, stators). The measurements at the test rig were totally automated, in compliance with the standard [7], with the use of a computer and a dedicated control software. The measurement

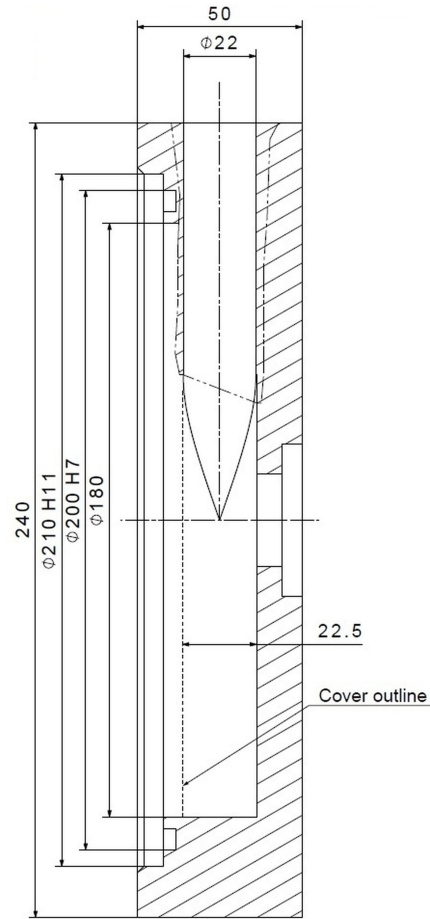


Figure 3: Dimensions of base annular casing of model pump

was conducted from a complete opening of the control valve to it is closing, and then from closing to the fully open.

Table 1: Measuring instruments.

Measuring instrument	Range	Accuracy class
Electromagnetic flowmeter	0.18-17.67 m^3/h	0.2%
Arkon MAGS1-ST DN25 PN40	(0.1-10 m/s)	
Pressure gauge (suction) FUJI FPK 01	-0.7 to 0.5 bar	0.1%
Pressure gauge (discharge) FUJI FPK 03	0-30 bar	0.1%
Active power transducer METROL PP73	0-3000 W	0.3%
Temperature transducer FLEXTOP	0-50°C	$\pm 0.9^\circ\text{C}$

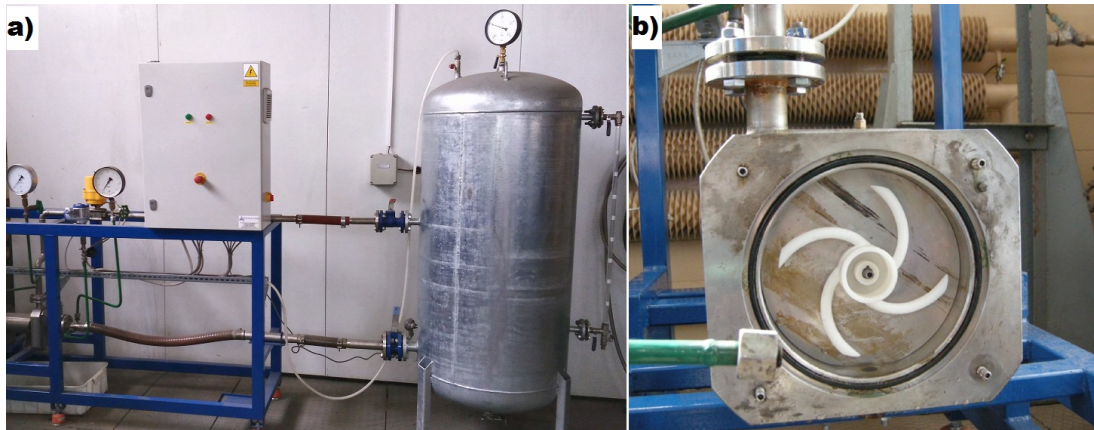


Figure 4: Presentation of test rig – (a) view of test rig, (b) the test rig model pump without the front panel with elliptical type of multi-piped impeller.

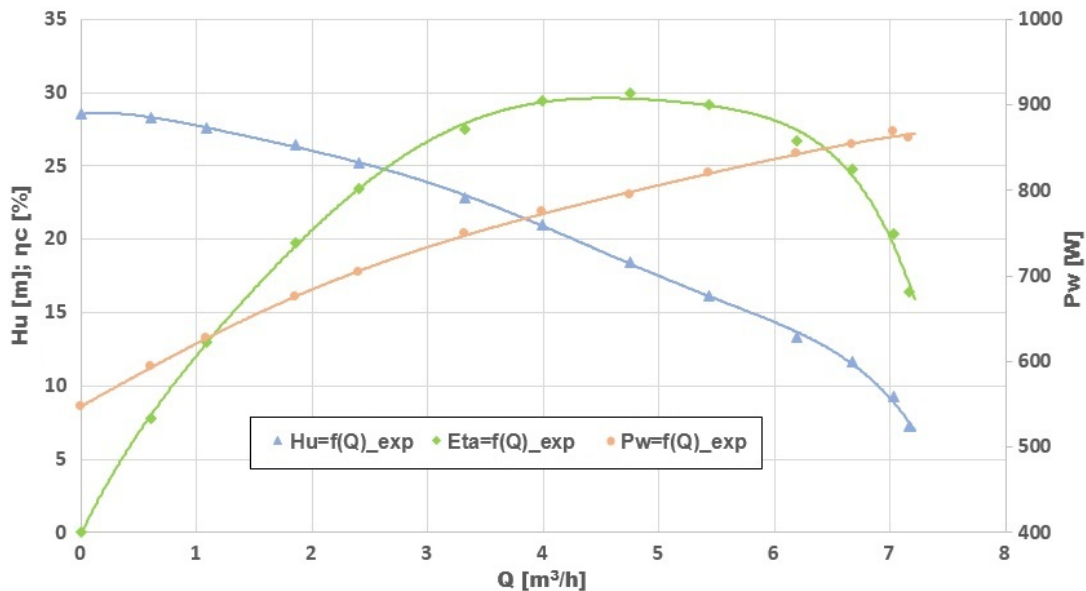


Figure 5: Characteristics of the model pump with an annular casing and a multi-piped impeller.

The results of measurements of energetic characteristics of the model pump in the base configuration were shown in Figure 5.

As show energetic characteristics of the model pump in Figure 5 the Best Efficiency Point (BEP) of researched pump is characterized by the following operating parameters: pump capacity $Q = 4.8 \text{ m}^3/\text{h}$ ($v_a = 6 \text{ m/s}$, Re was about $59 \cdot 10^3$), total pump head $H_u = 18.4 \text{ m}$, total efficiency $\eta_c = 29.9\%$. This value will be used to build a numerical model of pump with annular casing.

3 Numerical simulations

In order to identify flow phenomena occurring during the liquid flow in the stator type and to determine the rational flow geometry (which has optimal operating parameters), numerical flow analyzes were made using CFD (Computational Fluid Dynamics). As a base liquid model of pump – geometry of an annular casing and a multi-piped impeller implemented in the test rig pump – was created as a 3D model in Catia software. Further, geometry of the impeller remained unchanged. However, the type and construction of stators cooperating with the impeller were altered. Geometry of basic annular casing was calculated and designed according to theory included in [3, 4].

In order to perform the calculations Ansys Fluent from Ansys Workbench 18.2 package was used. The geometric model of the pump consisted of the following volumes: inlet, impeller, annular-type casing (and volute casing in late calculations), outlet. The simplified geometric model of the pump used for discretization was presented in Figure 6.

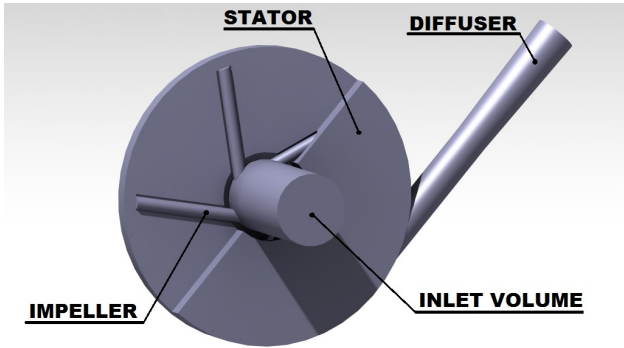


Figure 6: Simplified model of flow geometry of a multi-piped pump with an annular casing.

To determine an optimal size of a grid from accuracy and speed of calculation point of view the GIT (Grid Independence Test) was performed. The calculations were performed for six variants of grids, which differed in size of the element (about 30% each). In each case the grid was built from the tetrahedral elements and concentrated in the areas of walls of the impeller and stator (used function Inflation in Ansys Fluent). For further calculations, the smallest size of the calculation grid was assumed, for which the discrepancies in the results of the comparison parameters (in this case total head pump H_u and total moment on the impeller rotating surfaces M_t) with the next gradation of mesh were in the range: 2.8% for H_u and 0.9% for M_t . In chosen grid the minimum size of element was 0.2 mm and total quantity of tetrahedral elements was 29 million. The $y+$ parameter on rotating surfaces does not exceed 1.

The all numerical calculations were performed as transient flow (PISO algorithm, second-order upwind for all equations, double precision Solver, convergence criterion for each equation was $\epsilon = 10^{-6}$) in Ansys Fluent software. Rotational speed of the multi-piped impeller was constant and was $n = 2870$ rpm. For one rotation of an impeller 120 time steps were assumed, the value of one time step determined in accordance with [8] was $t_s = 5.2 \cdot 10^{-4}$ s. The calculations were performed by means of a turbulence model $k-\omega$ SST, which one was choose as optimal turbulence model by procedure described accordance

with [5, 8]. Other – necessary for calculations – boundary conditions were defined compliant with Figure 5, as:

- Inlet model – velocity of the liquid at the inlet corresponding the assumed efficiency and intensity of turbulence $T_i = 4\%$.
- Walls – velocity of the liquid in a perpendicular direction to the wall $u_x = 0$, zero pressure gradient $dp/dn = 0$.
- Outlet model (diffuser) – the assumed pressure at the outlet $p = 400$ kPa, intensity of reverse flow turbulence $T_{ibf} = 2\%$, constant liquid viscosity, constant mass flow.

To evaluate correctness of the assumptions for the numerical model the validation of numerical results was performed by comparing them with the experimental test results in the whole range of a pump characteristic. In the whole area of a pump with a multi-piped impeller and annular casing the difference between the experimental results and numerical ones does not exceed 3%. Numerical characteristics coincided with the experimental characteristics of model pump (Figure 5). The verified numerical model was applied in the tests on the influence of the type and construction of the stator cooperating with a multi-piped impeller on the pump's energetic parameters.

Main operating parameters of the tested centrifugal pump were determined in compliance with the following equations:

$$H = (p_{cout} - p_{cin}) / \rho g \quad (1)$$

$$P_w = M_t \omega \quad (2)$$

$$\eta_h = P_h / P_w = \rho g Q H / (M_t \omega) \quad (3)$$

$$\eta = \eta_h \eta_v \eta_m \quad (4)$$

The total efficiency of the pump (4) was determined assuming values of mechanical efficiency $\eta_m = 0.90$ and volumetric efficiency $\eta_v = 0.92$. Mechanical efficiency can be treated as a constant value, because it depends on the losses in bearings and sealing. Volumetric efficiency mainly depends on the pressure difference in an impeller gap sealing what it is unchangeable in our tests. Due to this fact the volumetric efficiency can be treated as constant as well. The hydraulics efficiency is the key factor especially for pumps working in ultra-low kinematic specific speed – it mainly affects the total pump efficiency.

The cooperation of the multi-piped impeller with two types of stators was analyzed in this paper: an annular casing and volute casing – with different configurations of

Table 2: Research changes of geometrical parameters of stator type.

Type of stator	Parameter	Range	Base value	Rational value
Annular casing	b_{3kk}	14 mm ÷ 27 mm	22.5 mm	18.5 mm
	d_4	160 mm ÷ 186 mm	180 mm	164 mm
	cross-section shape	rectangular profile	rectangular profile	rectangular profile
		semi-circular profile trapezoidal profile	semi-circular profile trapezoidal profile	rectangular profile
Volute casing	B_{cw}	0 – 30°	0°	15°
	b_3	constant value	18.5 mm	18.5 mm
	b_{3sp}	10 mm ÷ 19 mm	18.5 mm	14 mm
	cross-section shape	rectangular profile	rectangular profile	rectangular profile
		semi-circular profile trapezoidal profile	semi-circular profile trapezoidal profile	rectangular profile

their geometric features. Outlet elements were designed in accordance with commonly used theoretical models based on one-dimensional flow theory of centrifugal pump (according to the constant and averaged velocity of liquid in the stator after impeller outlet).

The algorithm of numerical simulation of flow geometry rationalization was prepared to analyze the cooperation of a multi-piped impeller with an annular casing at various configurations of construction features. The following geometrical parameters of stator were the researched (Figure 7a):

- In first step – impact of the width b_{3kk} of the cross-section – basic value of width of model pump was 22.5 mm.
- After finding a rational value of width, the next step was to research the outer diameter d_4 of the channel – basic value of outer diameter of model pump was 180 mm.
- After finding a rational value of outer diameter, the last step was to research the cross-section shape – basic was rectangular profile.

Then the algorithm of numerical simulation of flow geometry rationalization was prepared to analyze the cooperation of a multi-piped impeller with a volute casing at various configurations of its geometric features. The following parameters were tested (Figure 7b):

- In first step – impact of the angle B_{cw} of the beginning of the volute tongue – basic value angle of the theoretical spiral casing was 0°.
- After finding a rational value of angle, the next step was to research the width b_{3sp} of spiral part of stator – basic value of width was 18.5 mm.

- After finding a rational value of width, the last step was to research the cross-section shape – basic was rectangular profile.

The important information – the width of non-spiral part of stator b_3 was constant in all numerical calculation and was equaled rational value of width b_{3kk} of annular casing (orange dimension $b_3 = 18.5$ mm in Figure 7b).

The Table 2 shown research changes of geometrical parameters of stators. Range of changes of value, base value of parameters (initial parameters of simulations) and rational value of them was contained. Base value of geometrical parameters of annular casing was taken from model pump (from test rig). Initial value of geometrical parameters of volute casing was calculated.

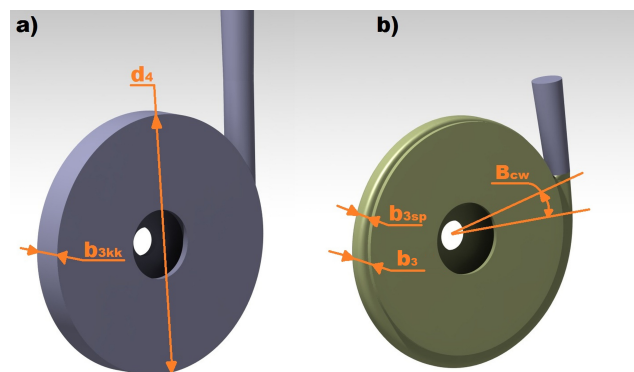


Figure 7: Analysed features of flow geometry for both types of stator: a) annular casing, b) volute casing.

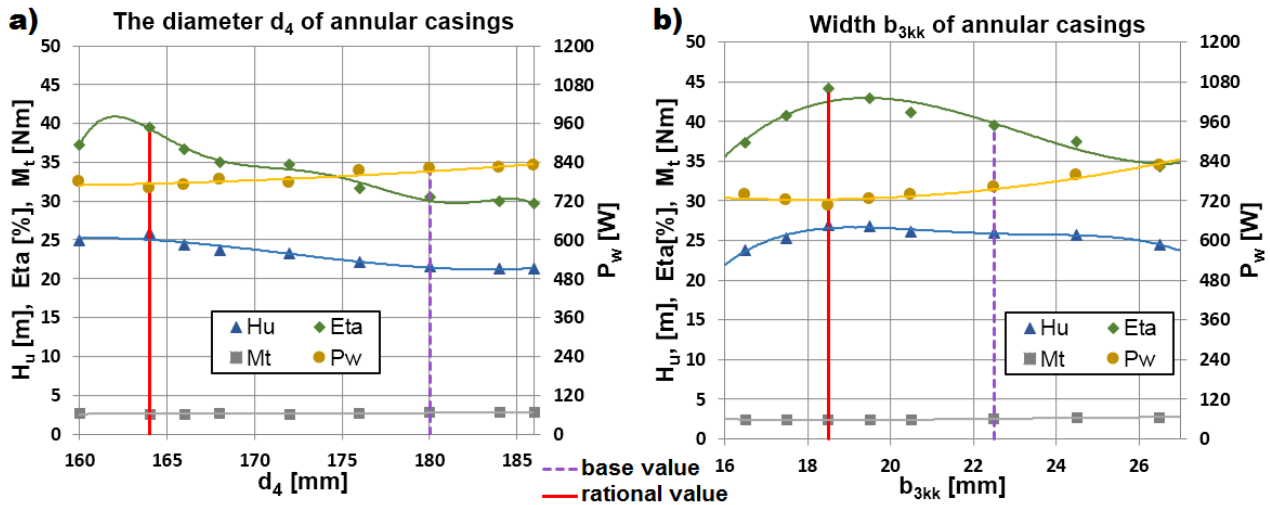


Figure 8: Influence of changes of the diameter d_4 (a) and width b_{3kk} (b) of the annular casing.

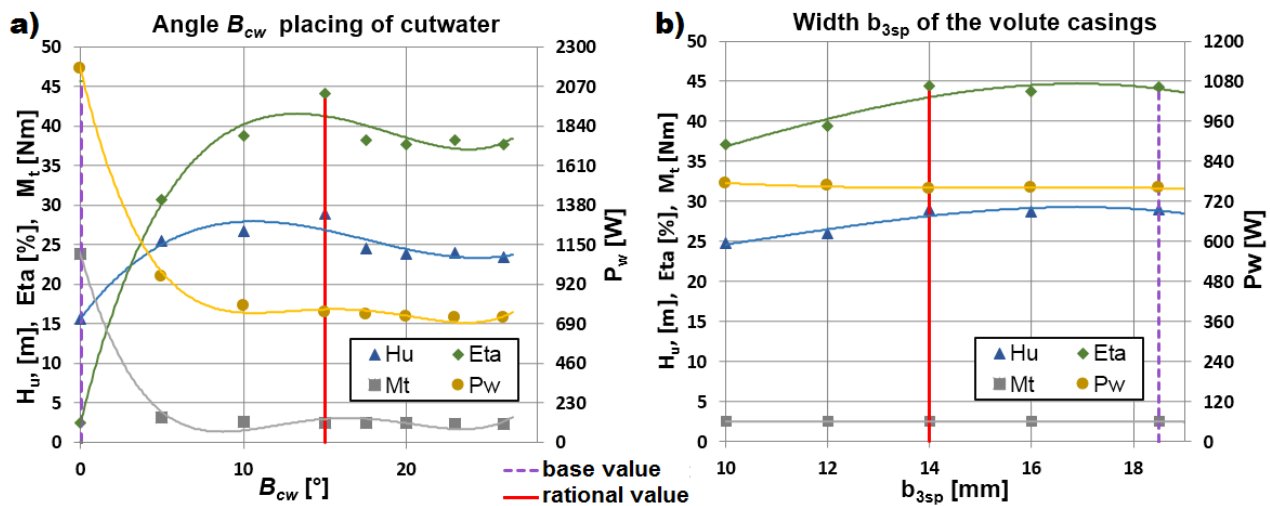


Figure 9: Influence of changes of the angle B_{cw} location of a volute tongue (a) and the width b_{3sp} (b) of the volute casing.

4 Results of numerical research

The results of the numerical calculations of change geometrical parameters show Figure 8 for annular casing and Figure 9 for volute casing. Rationalization of flow geometry of stator has improved the parameters of the pump in both construction. Table 3, on the other hand, shows the results obtained after an alteration of the shape of a channel's profile.

While analyzing the obtained numerical results of pump with both types of stators and multi-piped impeller it can be noticed that:

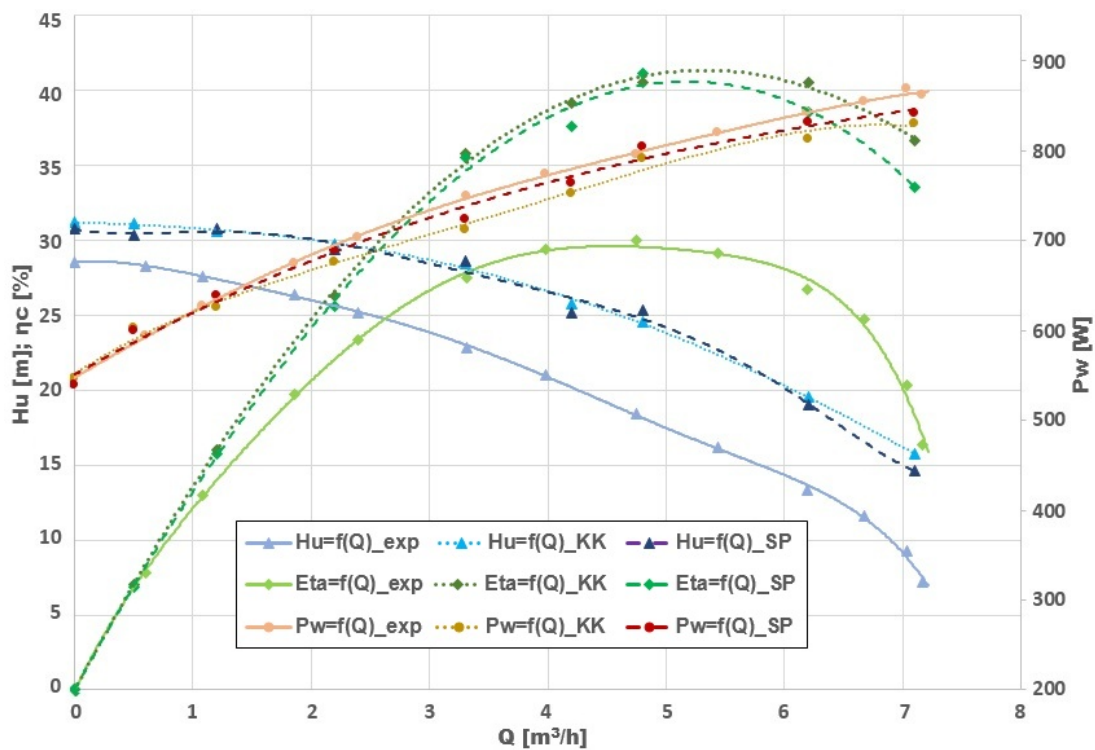
- As show Figure 8, reduction of annular casing geometry (represented by outer diameter d_4 and width b_{3kk} of channel) by about 26% caused a relative in-

crease in total efficiency by 12 percent point, total head pump of 34% and decrease in power consumption of almost 9%.

- Reduction of volute casing geometry (represented by width b_{3kk} of spiral part of channel) by about 20% caused a relative increase in total efficiency by 13 pp., total head pump of 30% and decrease in power consumption by the pump of almost 7% (show in Figure 9).
- The angle B_{cw} of the volute tongue – as show Figure 9a. – in its low values is strongly affecting the pump operating parameters. It determines the width of the gap between the impeller and the tongue. Reducing the gap caused an increase in local resistances of flow.

Table 3: Influence of changes in the shape of the cross-sectional profile in both types of stators.

Annular casing								
Lp.	Profile	Q	M _t	H	P _h	P _w	η _h	η _c
	-	m ³ /h	Nm	m	W	W	%	%
1	rectangular profile	4.8	2.631	25.57	387.5	790.5	49.02	40.57
2	semi-circular profile	4.8	3.023	25.22	355.4	908.5	41.32	34.21
3	trapezoidal profile	4.8	2.765	25.81	386.8	831.1	47.75	39.54
Volute casing								
Lp.	Profile	Q	M _t	H	P _h	P _w	η _h	η _c
	-	m ³ /h	Nm	m	W	W	%	%
1	rectangular profile	4.8	2.687	25.17	389.3	807.4	48.23	39.93
2	semi-circular profile	4.8	2.935	26.77	375.7	882.1	43.73	36.21
3	trapezoidal profile	4.8	2.811	26.71	374.9	844.8	45.56	37.72

**Figure 10:** Characteristics of the base model pump (exp) and pump with rational geometry of both types of stator: annular casing (KK) and volute casing (SP).

- The shape of the cross-section of the both stator type does not have a positive effect on the energy parameters tested pump. As show table 3, the base rectangular shape of the channel is characterized by the highest efficiency and total head pump.
- A change size of the flow area had a significant impact on the improvement of flow parameters. The size of the flow area determines pressure and velocity distribution of the liquid throughout the whole

width of the stator (presented in Figure 11 and Figure 12).

The characteristics of the centrifugal pump with a multi-piped impeller cooperating with the basic construction of annular casing used in model pump of test rig (index EXP), rational geometry of the annular casing (KK) and with the optimal volute casing (SP) obtained in numerical calculations was presented in Figure 10.

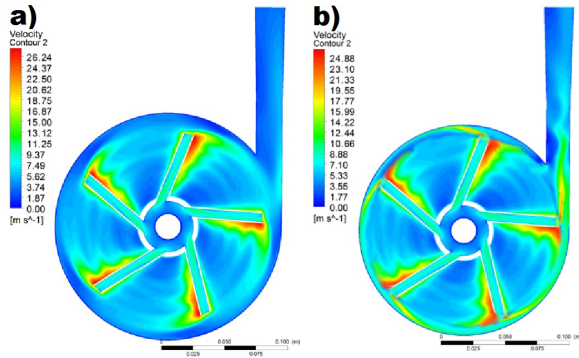


Figure 11: Distribution of liquid velocity on central plane (SPAN50) for: a) base model pump, b) pump with rational flow geometry of annular casing.

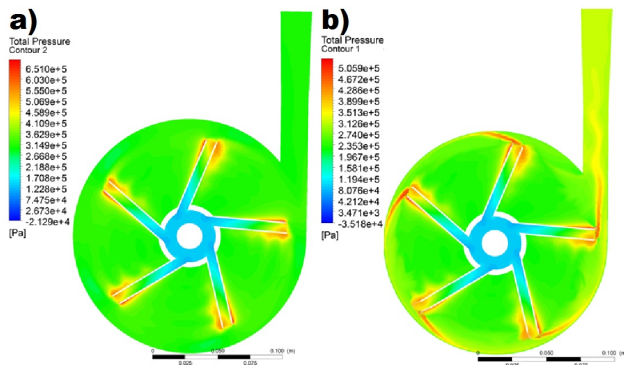


Figure 12: Distribution of total pressure on central plane (SPAN50) for: a) base model pump, b) pump with rational flow geometry of annular casing.

In the pictures the distribution of velocity vectors (Figure 11) and the distribution of total pressure (Figure 12) were presented. The results of numerical calculations for the model pump and pump with rational geometry of the stator – annular casing – were compared with each other on the central plane of the pump (SPAN50), across impeller, annular casing and diffuser. Reducing the stator geometry (outer diameter d_4 and width b_{3kk} for annular casing, width b_{3sp} for volute casing, cross-section shape for both stators) caused the slight decrease of the liquid velocity after impeller outlet while uniforming its distribution along the whole perimeter. Consequently hydraulic losses are lower – lack of recirculation and turbulence areas. Furthermore, decreasing the stator geometry (both for annular casing and volute casing) resulted in a considerable enhancement of the uniformity of static and total pressure distribution. Working conditions of an outlet diffuser at rational geometry of annular casing were improved, it is used in a much higher degree, however, still liquid does not flow into it with the whole width of the cross-section.

5 Conclusion

As shown in paper, the annular casing of model pump (from test rig shows in Figure 3 and Figure 4; represented by index EXP in Figure 10) cooperating with multi-piped impeller – designed in accordance with [3, 4] – reached far poorer operating parameters than the rational construction of stator type (in a comparison with the same multi-piped impeller).

A proper choice of the construction and type of stator cooperating with a multi-piped impeller can attain a relative increase of efficiency of nearly 12 percent point, the growth of total head pump over 25% and decrease in power consumption by the pump of almost 9% comparison with the one based on literature. This surplus gives such of opportunities for further rationalization of multi-piped impeller geometry (for example reducing the outer diameter of impeller).

While analyzing the cooperation results of a multi-piped impeller with the volute casing, it can be noticed that the results obtained for the cooperation with the annular type casing are virtually comparable. Annular channel is easier and cheaper to produce compared to a spiral channel. This also confirms the thesis put forward in the literature [3], the author believes that for pumps with extremely low specific speed it is better to use a stator with a constant cross-section than another stator type, because difference in efficiency are negligible. It appears that, due to the ease of construction, the annular type casing is the best choice for cooperation with a hole impeller in the range of extremely low specific speed $n_q < 10$.

Knowledge concerning construction of hydraulic elements – especially in type of stators which was researched in this article – of centrifugal pumps working in the range of parameters corresponding ultra low specific speed ($n_q < 10$) is insufficient.

For efficiency corresponding nominal best efficiency point (BEP) calculation error [9] did not exceed 1.9% – it suggest high level of confidence of used analytics and numerical models.

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