

A.2 Appendix

1. Structural vector autoregression model

The structural form of the vector autoregression model is given by

$$\mathbf{A}_0 X_t = \sum_{i=1}^p \mathbf{A}_i X_{t-i} + \mathbf{B}_0 Z_t + \epsilon_t, \quad (1)$$

where X_t is a $N \times 1$ vector of endogenous variables, Z_t is a $M \times 1$ vector of exogenous variables including the constant term, and $\epsilon_t \sim WN(0, I)$ is a $N \times 1$ vector of structural shocks. In our benchmark specification we have $N = 5$, $M = 3$, $p = 1$, and $T = 59$.

The coefficient matrices are as follows. $\mathbf{A}_0$ is the $N \times N$ matrix used to identify contemporaneous relations among variables, $\mathbf{A}_i$ are the $N \times N$ coefficient matrices of lagged variables, and $\mathbf{B}_0$ is the $N \times M$ matrix of coefficients on the exogenous variables and the constant term.

We set $p = 1$ and multiply both sides of (1) by $\mathbf{A}_0^{-1}$ to obtain the reduced form VAR

$$X_t = \mathbf{C}X_{t-1} + \mathbf{D}Z_t + \mathbf{u}_t \quad (2)$$

where $\mathbf{C} = \mathbf{A}_0^{-1}\mathbf{A}_1$, $\mathbf{D} = \mathbf{A}_0^{-1}\mathbf{B}_0$, and $\mathbf{u}_t \sim N(0, \Sigma)$.

A compact representation of (2) can be obtained

$$\mathbf{Y} = \mathbf{E}\mathbf{W} + \mathbf{U},$$

where

$$\begin{aligned} \mathbf{Y}_{NxT} &= (X_1, \dots, X_T) \\ \mathbf{E}_{Nx(N+M)} &= (\mathbf{C}, \mathbf{D}) \\ \mathbf{W}_{(N+M) \times T} &= \begin{pmatrix} \mathbf{Y}_0, \dots, \mathbf{Y}_{T-1} \\ \mathbf{Z}_1, \dots, \mathbf{Z}_T \end{pmatrix} \\ \mathbf{U}_{NxT} &= (\mathbf{u}_1, \dots, \mathbf{u}_T), \end{aligned}$$

and

$$\mathbf{u}_t = \mathbf{A}_0^{-1}\epsilon_t.$$

Estimation entails obtaining a matrix of estimated coefficients $\hat{\mathbf{E}}$, and the ensuing matrix of residuals from $\hat{\mathbf{U}} = \mathbf{Y} - \hat{\mathbf{E}}\mathbf{W}$.

For easier manipulation, and without loss of generality, let us consider the SVAR model in (1) without the exogenous block

$$X_t = \mathbf{C}X_{t-1} + \mathbf{u}_t, \quad (3)$$

which can be written as

$$(\mathbf{I} - \mathbf{C}(\mathbf{L}))X_t = \mathbf{u}_t, \quad (4)$$

In compact form

$$X_t = \mathbf{F}(\mathbf{L})\mathbf{A}_0^{-1}\epsilon_t, \quad (5)$$

where $\mathbf{F}(\mathbf{L}) = (\mathbf{I} - \mathbf{C}(\mathbf{L}))^{-1}$ can be obtained from estimating $\mathbf{C}$ and inverting $\mathbf{A}_0$ from (2). We use short-run recursive identification, which entails setting restrictions on $\mathbf{A}_0$.

The identification strategy is implemented as follows. Multiply both sides of (4) by a matrix of parameters $\mathbf{A}_{N \times N}$ and equate the resulting expression to a scaled version of the i.i.d vector ϵ_t using a scaling matrix $\mathbf{B}_{N \times N}$.

$$\mathbf{A}(\mathbf{I} - \mathbf{C}(\mathbf{L}))X_t = \mathbf{A}\mathbf{u}_t = \mathbf{B}\epsilon_t$$

The identification strategy is discussed in the paper and is implemented by setting $\mathbf{A}$ as a lower triangular matrix with ones on the diagonal, and $\mathbf{B}$ as a diagonal matrix.

Implementation is achieved by using the Cholesky decomposition of $\mathbf{\Sigma}$, the covariance matrix of $\mathbf{u}_t$, such that $\mathbf{\Sigma} = \mathbf{S}\mathbf{S}'$. In this case $\mathbf{S} = \mathbf{A}^{-1}\mathbf{B} = \mathbf{A}_0^{-1}$.

2. Parameter estimates

Here we report the coefficients from estimating the benchmark specification from **Figure 1** in the paper.

$$A = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0.04 & 1 & 0 & 0 & 0 \\ -0.05 & -0.02 & 1 & 0 & 0 \\ -0.12 & -0.16 & 0.72 & 1 & 0 \\ 0.01 & -0.13 & -0.03 & 0.05 & 1 \end{pmatrix}$$

$$B = \begin{pmatrix} 0.79 & 0 & 0 & 0 & 0 \\ 0 & 0.71 & 0 & 0 & 0 \\ 0 & 0 & 0.26 & 0 & 0 \\ 0 & 0 & 0 & 0.48 & 0 \\ 0 & 0 & 0 & 0 & 0.36 \end{pmatrix},$$

and the resulting Cholesky factor $\mathbf{S} = \mathbf{A}^{-1}\mathbf{B}$ is

$$A = \begin{pmatrix} 0.79 & 0 & 0 & 0 & 0 \\ -0.03 & 0.71 & 0 & 0 & 0 \\ 0.04 & 0.01 & 0.26 & 0 & 0 \\ 0.06 & 0.10 & -0.18 & 0.48 & 0 \\ -0.01 & 0.09 & 0.02 & -0.02 & 0.36 \end{pmatrix}.$$