

SUPPLIER SELECTION MODELS USING FUZZY HYBRID METHODS IN THE CLOTHING TEXTILE INDUSTRY

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Abstract:

Application of models for supplier assessment and selection in the clothing industry remains relatively underexplored. To fill this gap, this research study introduces the following fuzzy hybrid models for evaluating and selecting suppliers for clothing manufacturing firms: fuzzy set theory, Analytic Hierarchy Process method–fuzzy–Technique for Order of Preference by Similarity to Ideal Solution (AHP–fuzzy–TOPSIS), AHP–fuzzy–Weighted Sum Model (WSM), and AHP–fuzzy–Weighted Product Mean (WPM). Criteria weights were established utilizing these models, which were applied to identify the optimal supplier. A practical study was conducted within a clothing firm to evaluate the effectiveness of these fuzzy hybrid models. The main results reveal that the AHP–fuzzy–TOPSIS model outperforms the AHP–fuzzy–WSM and AHP–fuzzy–WPM models in selecting the optimal alternative. Indeed, this approach has the potential to be adapted to different industrial sectors, considering the specific criteria and conditions that govern their supplying processes.

Keywords:

AHP–fuzzy–TOPSIS, AHP–fuzzy–WPM, AHP–fuzzy–WSM, supplier selection, supply chain

1. Introduction

Selecting supplier processes is an essential issue in the supply chain, affecting a company's competitiveness and performance. In the literature, a multitude of studies have addressed this topic across numerous fields, with particular emphasis on the clothing industry [1–3]. One of them focused on utilizing the Analytic Hierarchy Process (AHP) to select suppliers in the apparel industry. In this article, flexibility, cost, and delivery were used as criteria. As a result, the used model would be much easier and more efficient for buyers [4]. Amindoust and Saghafinia applied the fuzzy inference method in the textile industry. The study involved three decision-makers in evaluating five potential suppliers. Consequently, the utilized method was able to rank suppliers according to their performance assessments and assign critical criteria in the ranking process [5]. Burney and Ali used the AHP-fuzzy method to select Pakistan's textile industry suppliers. The selection criteria were identified by the purchasing manager of a textile manufacturing enterprise. As criteria, they have used quality, price, services, cost, delivery time, and payment terms [6]. Some researchers used the DEcision-MAking Trial and Evaluation Laboratory (DEMATEL) approach and the Analytical Network Process (ANP) method as alternative evaluation methods in the textile field. The DEMATEL approach was employed to evaluate the interrelationships between criteria, and the ANP technique was employed to calculate the weighting of criteria [7,8]. Some researchers combined the AHP method with different methods such as electro-sorting, preventive objective programming (PGP), and the method of order of preference in the textile field. Weighting of criteria was established by using the

AHP technique, and various techniques were employed to classify alternatives [9–13]. Lahdhiri et al. applied both fuzzy logic and AHP methods to determine the optimal subcontractor in the clothing industry. Their research concluded that the AHP approach outperforms the fuzzy logic technique in subcontractor selection [14]. Moreover, numerous scientific studies have addressed this problem in the manufacturing field. We highlight a selection of them to present the extensive range of applications in this part. Kull and Talluri used the AHP method and the goal programming (GP) model to choose the optimal supplier in the automotive field. The AHP approach was employed to establish criteria assessment, and suppliers were selected using the GP model [11]. Some researchers applied the ANP approach in Taiwanese TV and electronic companies to choose the best supplier [15,16]. ArabsheYbani et al. used the fuzzy-Multi-Objective Optimization by Ratio Analysis (MOORA) method to identify the optimal supplier within the household appliance sector. In their study, suppliers' risks were assessed using failure mode and effect analysis, and the fuzzy-MOORA method was used to choose the optimal supplier. In conclusion, the proposed method chose the optimal supplier and can be implemented across various industries, including the manufacturing, electrical, chemical, and automotive industries [17]. Some researchers used the fuzzy-ANP approach in the electronics sector in India to choose the optimal supplier [18]. Masoud et al. applied the Balanced ScoreCard (BSC)–fuzzy-AHP technique to select optimal alternatives within the automobile sector. Their study proposed the BSC method for suppliers' performance measurement, and the fuzzy-AHP approach was employed for supplier assessment. Consequently, the method proposed in this research can be integrated with other Multiple



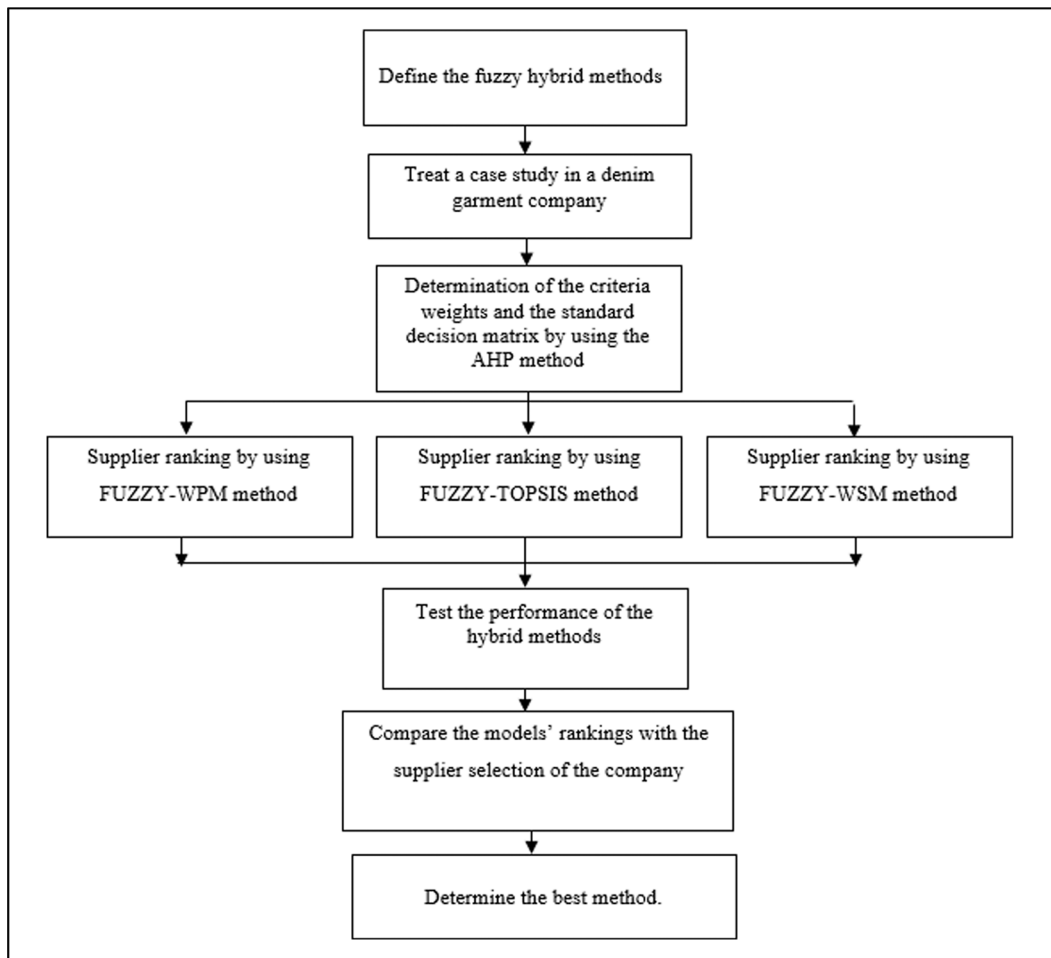


Figure 1. Our study's methodology.

Criteria Decision-Making (MCDM) tools [19]. Following an extensive review of the literature, numerous applications of MCDM methods for assessment and selection of suppliers have been identified; however, research studies in the garment and textile field remain relatively scarce. Hence, in this article, the AHP–fuzzy-Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS), AHP–fuzzy-Weighted Sum Model (WSM), and AHP–fuzzy-Weighted Product Method (WPM) models were established to classify and select suitable suppliers within a clothing supply chain. This study endeavored to evaluate selected suppliers by employing the AHP–fuzzy-TOPSIS, AHP–fuzzy-WSM, and AHP–fuzzy-WPM models, considering several criteria: price, quality, compliance of quantity, and compliance of delay. Moreover, this study aimed to utilize the AHP technique to compute the weightings of the criteria. Further, supplier rankings were established by employing hybrid MCDM methods (AHP–fuzzy-TOPSIS, AHP–fuzzy-WSM, and AHP–fuzzy-WPM).

Indeed, the use of hybrid MCDM models for supplier assessment and selection in the clothing industry was justified based on several factors:

- Complexity of decision-making.
- Handling subjectivity and uncertainty.
- Robustness and flexibility.

- Improved decision quality.

2. Modeling methods

2.1. Research methodology

The objective of our research was to introduce hybrid MCDM models, integrating the AHP method, fuzzy set theory, TOPSIS method, WSM, and WPM. These techniques were employed to identify the most suitable supplier for the clothing industry, aiming to address the existing gap in the literature. This research comprised several stages, as summarized in Figure 1. In the first step, the proposed models were presented. In the second step, a case study of a company specializing in denim apparel was conducted. In this case study, the AHP technique was employed to establish the criteria weightings and the decision matrix. Hybrid MCDM models, including AHP–fuzzy-WSM, AHP–fuzzy-TOPSIS, and AHP–fuzzy-WPM, were applied to choose the optimal supplier. In the concluding phase, the hybrid methods underwent evaluation and comparison. The methodology applied in this work is depicted in Figure 1.

The approach used in this study is introduced in the following sections.

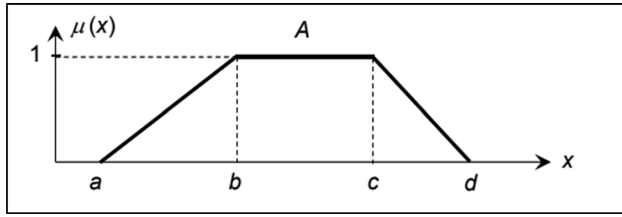


Figure 2. Membership functions of the trapezoidal fuzzy numbers.

2.2. Fuzzy set

Definition 1. (Fuzzy set)

A fuzzy set “ \tilde{A} ” of a universal set X can be described by its membership function $\mu_{\tilde{A}}(x)$ as $\tilde{A} = \{(x, \mu_{\tilde{A}}(x)) | x \in X\}$, where $x \in X$ refers to the elements belonging to the universal set and $\mu_{\tilde{A}}(x): X \rightarrow [0, 1]$. In the pair $(x, \mu_{\tilde{A}}(x))$, the first component $x \in A$, where A is the classical set, and the next element $\mu_{\tilde{A}}(x) \in [0, 1]$ is called the membership function [20].

Definition 2. (Trapezoidal fuzzy numbers)

The trapezoidal fuzzy number \tilde{A} is specified by quadruples $\tilde{A} = (a, b, c, d)$ such that $a \leq b \leq c \leq d$ and is defined by the membership function as expressed by equation (1) [21]:

$$\mu_{\tilde{A}}(x) = \begin{cases} 0, & x < a \\ \frac{x-a}{b-a}, & a \leq x \leq b \\ 1, & b \leq x \leq c \\ \frac{d-x}{d-c}, & c \leq x \leq d \\ 0, & x > d. \end{cases} \quad (1)$$

Figure 2 presents the membership functions corresponding to the trapezoidal fuzzy numbers.

Definition 3. (Operations on Trapezoidal fuzzy numbers)

Let $\tilde{X} = (a_1, b_1, c_1, d_1)$ and $\tilde{Y} = (a_2, b_2, c_2, d_2)$ denote two trapezoidal fuzzy numbers non-negative and $\alpha \in \mathbb{R}^+$. The arithmetic formulas are presented as follows:

$$\tilde{X} + \tilde{Y} = (a_1 + a_2, b_1 + b_2, c_1 + c_2, d_1 + d_2), \quad (2)$$

$$\tilde{X} - \tilde{Y} = (a_1 - a_2, b_1 - b_2, c_1 - c_2, d_1 - d_2), \quad (3)$$

$$\tilde{X} \times \tilde{Y} = (a_1 \times a_2, b_1 \times b_2, c_1 \times c_2, d_1 \times d_2), \quad (4)$$

$$\tilde{X} / \tilde{Y} = (a_1/d_2, b_1/c_2, c_1/b_2, d_1/a_2). \quad (5)$$

2.3. AHP–fuzzy-TOPSIS

The AHP model is one of the widely used MCDM models, and it was created by Saaty. It offers a structured approach to solving complex decisions [22]. The AHP method begins with the identification of the problem at hand, along with defining the criteria and available alternatives. Subsequently, pairwise comparisons are conducted between the criteria and alternatives to evaluate their respective importance. Once these comparisons are made, the process moves towards determining the alternatives’ rank based on the established criteria. Hwang et al. introduced the fuzzy-TOPSIS model as an MCDM approach [23]. It was based on negative and positive ideal solutions. In the integrated AHP–fuzzy-TOPSIS method, AHP was employed to calculate the weightings of the criteria, while the fuzzy-TOPSIS model was employed to classify the alternatives. The following steps are involved in utilizing the AHP–fuzzy-TOPSIS method.

AHP–fuzzy-TOPSIS steps:

Step 1: Establish linguistic variables and terms

Linguistic variables are variables within a system that use words from natural language instead of numerical values to represent inputs or outputs.

Step 2: Construct the membership functions

Membership functions are employed to quantify linguistic terms within a system. Various types exist, including triangular, trapezoidal, piecewise linear, Gaussian, and singleton functions.

Step 3: Assignment rating to the alternatives to create a fuzzy decision matrix

We suggest establishing a decision group consisting of F members. Each member of this decision-making group will utilize linguistic terms to assess every alternative for each criterion. The decision-maker matrix is presented in Table 1.

Table 1. Decision-maker matrix

Alternatives	Criteria					
		C_1	C_2	C_3	...	C_n
A_1		TS_{11}	TS_{12}	TS_{13}	...	TS_{1n}
A_2		TS_{21}	TS_{22}	TS_{23}	...	TS_{2n}
A_3		TS_{31}	TS_{32}	TS_{33}	...	TS_{3n}
..	
A_n		TS_{n1}	TS_{n2}	TS_{n3}	...	TS_{nn}

Table 2. Pairwise comparison matrix for criteria

Criteria	C_1	C_2	C_3	...	C_n
C_1	1	W_1/W_2	W_1/W_3	...	W_1/W_n
C_2	W_2/W_1	1	W_2/W_3	W_2/W_n
C_3	W_3/W_1	W_3/W_2	1	W_3/W_n
..	1	...
C_n	W_n/W_1	W_n/W_2	W_n/W_3	$W_n/W_{..}$	1

With Ts_{ij} equal to fuzzy sets for each linguistic variable, it could be low, medium, or high.

$$\tilde{r}_{ij} = \left(\frac{a_{ij}}{d_j^*}, \frac{b_{ij}}{d_j^*}, \frac{c_{ij}}{d_j^*}, \frac{d_{ij}}{d_j^*} \right), \quad (11)$$

Step 4: Transform the linguistic term into a fuzzy number

with $d_{ij}^* = \max(c_{ij})$.

Every linguistic term is transformed into a fuzzy number $\tilde{x}_{ij} = (a_{ij}, b_{ij}, c_{ij}, d_{ij})$.

For non-benefit criteria:

$$\tilde{r}_{ij} = \left(\frac{a_{ij}^-}{d_{ij}^-}, \frac{a_{ij}^-}{c_{ij}^-}, \frac{a_{ij}^-}{b_{ij}^-}, \frac{a_{ij}^-}{a_{ij}^-} \right), \quad (12)$$

Step 5: Aggregate the alternative fuzzy decision matrix

with $a_{ij} = \min(a_{ij})$.

The aggregated fuzzy rating $\tilde{y}_{ij} = (a_{ij}, b_{ij}, c_{ij}, d_{ij})$ of alternative A_i under criterion C_j is defined as follows:

$$a_{ij} = \min(a_{ijk}), \quad (6)$$

$$b_{ij} = 1/k \sum_{k=1}^k b_{ijk}, \quad (7)$$

$$c_{ij} = 1/k \sum_{k=1}^k c_{ijk}, \quad (8)$$

$$d_{ij} = \max(d_{ijk}). \quad (9)$$

Step 6: Normalize the fuzzy decision matrix

Step 7: Aggregate the alternative fuzzy decision matrix

An $n \times n$ pairwise comparison matrix is created to compare related criteria, as presented in Table 2. Criteria weights are determined by conducting pairwise comparisons using Saaty's scale [24]. Table 3 illustrates Saaty's scale.

The matrix is transformed into a normalized form, which is shown in Table 4.

To determine a vector of weights, the average of the lines "W" of the normalized pairwise matrix is computed.

The fuzzy decision matrix is normalized using the following equations:

$$\tilde{R}^k = [r_{ij}]mn, \quad (10)$$

with i from 1 to m and j from 1 to n .

For benefit criteria:

$$W = \begin{bmatrix} W_1 \\ W_2 \\ W_3 \\ \vdots \\ W_j \end{bmatrix} = \begin{bmatrix} \frac{\sum_{j=1}^n X_{1j}}{n} \\ \frac{\sum_{j=1}^n X_{2j}}{n} \\ \frac{\sum_{j=1}^n X_{3j}}{n} \\ \vdots \\ \frac{\sum_{j=1}^n X_{nj}}{n} \end{bmatrix}.$$

Step 8: Compute the weighting of the normalized matrix

Table 3. Saaty's 1–9 scale

Numerical scale	Verbal judgment of preference
1	Equal significance
3	Slight preference of one over another
5	Critical or significant importance
7	Clearly demonstrated importance
9	Utmost importance
2, 4, 6, and 8	Values that are intermediate between the two adjacent judgments

Table 4. Normalization matrix

Criteria	C_1	C_2	C_3	...	C_n
C_1	X_{11}	X_{12}	X_{13}	...	X_{1n}
C_2	X_{21}	X_{22}	X_{23}	...	X_{2n}
C_3	X_{31}	X_{32}	X_{33}	...	X_{3n}
..
C_n	X_{n1}	X_{n2}	X_{n3}	...	X_{nn}

Table 5. Categorization of variables

	Categorization		
	Low	Medium	High
Price/piece (euro)	0–0.8	0.8–4	4–7
Quality	0–1.2	1.2–4	4–6
Compliance of quantity (%)	0–0.3	0.3–0.8	0.8–1
Compliance of delay (%)	0–0.3	0.3–0.8	0.8–1

Matrix multiplication between the weighted criteria matrix and the normalized aggregated fuzzy decision matrix for alternatives is conducted, as expressed in equation (13):

$$\tilde{V}_{ij} = \tilde{r}_{ij} * W_j. \quad (13)$$

Step 9: Calculate the fuzzy positive and negative ideal solution (FPIS and FNIS) as expressed in equations (14) and (15).

$$A^* = (\tilde{V}_1^*, \tilde{V}_2^*, \tilde{V}_n^*) = (\max_j V_{ij} | i \in X), (\min_j V_{ij} | i \in Y), \quad (14)$$

with i from 1 to m and j from 1 to n ;

$$A^- = (\tilde{V}_1^-, \tilde{V}_2^-, \tilde{V}_n^-) = (\min_j V_{ij} | i \in X), (\max_j V_{ij} | i \in Y), \quad (15)$$

with i from 1 to m and j from 1 to n .

Here, “ X ” corresponds to the set of values for benefit criteria and “ Y ” defines the set of values for non-benefit criteria.

Step 10: Compute the weighted normalized fuzzy decision matrix

Equations (16) and (19) present the determination of the distance for each alternative from d_i^* and d_i^- :

$$d(\tilde{V}_{ij}, \tilde{V}_j^*) = \sqrt{\frac{1}{4} \times ((a_1 - a_2)^2 + (b_1 - b_2)^2 + (c_1 - c_2)^2 + (d_1 - d_2)^2)}, \quad (16)$$

$$d_i^* = \sum_{j=1}^n d(\tilde{V}_{ij}, \tilde{V}_j^*), \quad (17)$$

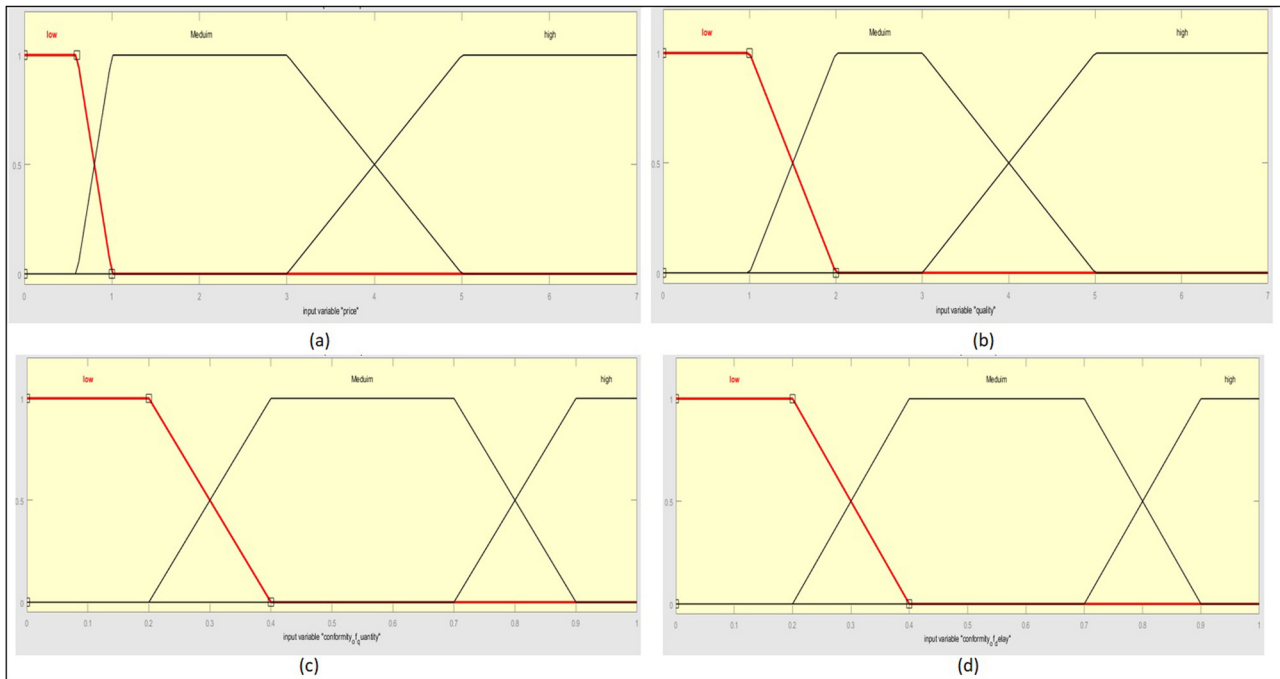

Figure 3. Membership function for each criterion: price (a), quality (b), conformity of quantity (c) and conformity of delay (d).

Table 6. Decision makers' evaluation

	Price	Quality	Compliance of quantity	Compliance of delay
Decision maker 1	S1	L	M	H
	S2	L	M	H
	S3	L	L	H
Decision maker 2	S1	M	H	M
	S2	H	M	M
	S3	L	L	M

Table 7. Fuzzy number of decision makers

	Suppliers	Price					Quality					Compliance of quantity					Compliance of delay				
		0	0	0	0.6	1	1	2	3	5		0.7	0.9	0.9	0.9	0.9	0.7	0.9	0.9	0.9	0.9
Decision maker 1	S1		0	0	0.6	1	1	2	3	5		0.7	0.9	0.9	0.9	0.9	0.7	0.9	0.9	0.9	0.9
	S2		0	0	0.6	1	1	2	3	5		0.7	0.9	0.9	0.9	0.9	0.7	0.9	0.9	0.9	0.9
	S3		0	0	0.6	1	0	0	1	2		0.7	0.9	0.9	0.9	0.9	0.7	0.9	0.9	0.9	0.9
Decision maker 2	S1	0.6	1	3	5	5	3	5	5	5		0.2	0.4	0.7	0.9	0.9	0.2	0.4	0.7	0.9	0.9
	S2	3	5	5	5	1	1	2	3	5		0.2	0.4	0.7	0.9	0.9	0	0	0.2	0.4	0.4
	S3	0	0	0.6	1	0	0	0	1	2		0.2	0.4	0.7	0.9	0.9	0.7	0.9	0.9	0.9	0.9

Table 8. Combined fuzzy decision matrix

Suppliers	Price				Quality				Compliance of quantity					Compliance of delay				
	0	0.5	1.8	5	1	3.5	4	5	0.2	0.7	0.8	0.9	0.2	0.7	0.8	0.9		
S1	0	0.5	1.8	5	1	3.5	4	5	0.2	0.7	0.8	0.9	0.2	0.7	0.8	0.9		
S2	0	2.5	2.8	5	1	2	3	5	0.2	0.7	0.8	0.9	0	0.5	0.6	0.9		
S3	0	0	0.6	1	0	0	1	2	0.2	0.7	0.8	0.9	0.7	0.9	0.9	0.9		

Table 9. Normalized fuzzy decision matrix

Suppliers	Price				Quality				Compliance of quantity				Compliance of delay			
S1	0	0	0	0	0.2	0.7	0.8	1	0.2	0.7	0.9	1	0.2	0.7	0.9	1
S2	0	0.4	0	0	0.2	0.4	0.6	1	0.2	0.7	0.9	1	0	0.5	0.6	1
S3	0	1.7	0	0	0	0	0.2	0.4	0.2	0.7	0.9	1	0.8	1	1	1

$$d(\tilde{V}_{ij}, \tilde{V}_j^-) = \sqrt{\frac{1}{4} \times ((a_1 - a_2)^2 + (b_1 - b_2)^2 + (c_1 - c_2)^2 + (d_1 - d_2)^2)}, \quad (18)$$

$$d_i^- = \sum_{j=1}^n d(\tilde{V}_{ij}, \tilde{V}_j^-). \quad (19)$$

Step 11: Determine the proximity coefficient for each alternative

This coefficient is utilized to establish the sequence of rankings for all alternatives after calculating the d_i^* and d_i^- values for each alternative A_i (where i ranges from 1 to m). Equation (20) represents this coefficient:

$$C_{ci} = \frac{d_i^-}{d_i^- + d_i^*}. \quad (20)$$

The ranking of all alternatives can be established by using this coefficient.

2.4. AHP–fuzzy-WPM

Fuzzy-WPM is a technique for MCDM [25]. We must select the best alternative between several options based on multiple criteria. An AHP–fuzzy-WPM method is an integrated approach that allows for calculating the criteria weights based on the AHP approach in the first step and then using the fuzzy-WPM approach to rank alternatives.

AHP–fuzzy-WPM steps:

Steps 1 through 7 of the AHP–fuzzy-WPM method share the same steps with those of the AHP–fuzzy-TOPSIS method.

Step 8: Determine the weighted normalized fuzzy decision matrix.

The weighted normalized fuzzy numbers of the alternatives are calculated using Equation (21):

$$\tilde{f}_i = \prod_{j=1}^n \tilde{r}_{ij} W_j, \quad (21)$$

with i from 1 to m and j from 1 to n .

Here, \tilde{f}_i represents the overall performance value of each alternative A_i , while \tilde{r}_{ij} denotes a fuzzy trapezoidal number. These values are utilized to establish the final fuzzy rating matrix:

$$\tilde{F}_{WSM} = \begin{bmatrix} \tilde{f}_1 \\ \tilde{f}_2 \\ \vdots \\ \tilde{f}_n \end{bmatrix}.$$

Step 9: Calculate the crisp value.

The crisp value is calculated according to equation (22):

$$d(\tilde{f}_i) = 1/4 * (a_i + b_i + c_i + d_i), \quad (22)$$

where $d(\tilde{f}_i)$ denotes the defuzzified or crisp value of the overall fuzzy score of alternative A_i .

2.5. AHP–fuzzy-WSM

Fuzzy-WSM is a technique for MCDM [25,26]. We must choose the best alternative among several options based on multiple criteria. The AHP–fuzzy-WSM method combines the AHP and fuzzy-WSM methods. The AHP method was employed to determine the weightings of the criteria, while the fuzzy-WSM method was employed to classify the alternatives.

AHP–fuzzy-WSM steps:

Steps 1 through 7 of the AHP–fuzzy-WSM method share the same steps as those of the AHP–fuzzy-TOPSIS method.

Step 8: Calculate the weighted normalized fuzzy decision matrix

The weighted normalized fuzzy numbers of the alternatives are calculated using equation (23):

Table 10. Matrix normalization

Criteria	Price/ piece	Quality	Compliance of quantity	Compliance of delay	Average vector: W
Price/piece	0.06	0.05	0.03	0.09	0.07
Quality	0.19	0.16	0.07	0.20	0.15
Compliance of quantity	0.31	0.32	0.15	0.12	0.22
Compliance of delay	0.44	0.47	0.75	0.60	0.56

Table 11. Weighted normalized fuzzy decision matrix

Suppliers	Price			Quality				Compliance of quantity					Compliance of delay			
	0	0	0	0	0.03	0.11	0.12	0.15	0.05	0.16	0.20	0.22	0.1	0.4	0.5	0.6
S1	0	0	0	0	0.03											
S2	0	0.02	0	0	0.03	0.06	0.09	0.15	0.05	0.16	0.20	0.22	0	0.3	0.3	0.6
S3	0	0.10	0	0	0	0	0.03	0.06	0.05	0.16	0.20	0.22	0.4	0.6	0.6	0.6

Table 12. FPIS and FNIS

Suppliers	Price				Quality				Compliance of quantity				Compliance of delay			
S1	0	0	0	0	0.03	0.11	0.12	0.15	0.05	0.16	0.20	0.22	0.1	0.4	0.5	0.6
S2	0	0.02	0	0	0.03	0.06	0.09	0.15	0.05	0.16	0.20	0.22	0	0.3	0.3	0.6
S3	0	0.10	0	0	0	0	0.03	0.06	0.05	0.16	0.20	0.22	0.4	0.6	0.6	0.6
A ⁺	0	0	0	0	0.03	0.11	0.12	0.15	0.05	0.16	0.20	0.22	0.44	0.56	0.56	0.56
A ⁻	0	0.1	0	0	0.00	0.00	0.03	0.06	0.05	0.16	0.20	0.22	0.00	0.28	0.34	0.56

Table 13. Closeness coefficient for each alternative

Suppliers	d_i^*	xxx	C_{ci}	Rank
S1	0.177	0.251	0.59	1
S2	0.486	0.103	0.17	3
S3	0.917	0.281	0.23	2

$$\tilde{f}_{ij} = \sum_{n=1}^i \tilde{r}_{ij} * w_j, \tag{23}$$

with i from 1 to m and j from 1 to n ,

where \tilde{f}_i represents the overall performance value of each alternative A_i , while \tilde{r}_{ij} denotes a fuzzy trapezoidal number. These values are utilized to establish the final fuzzy rating matrix:

$$\tilde{F}_{WPM} = \begin{bmatrix} \tilde{f}_1 \\ \tilde{f}_2 \\ \vdots \\ \tilde{f}_n \end{bmatrix}.$$

Step 9: Compute the crisp value, identical to AHP–fuzzy-WPM.

3. Practical application in a denim clothing manufacturing firm

3.1. Data set

This research was conducted in a denim manufacturing firm with a workforce of 450 employees. The company achieves a yearly production output of 800,000 products and works both as a principal for numerous subcontractors and as a producer of several products such as skirts, pants, and jackets. These products are manufactured for various international labels, requiring high-quality levels and fast delivery. This company procures numerous and various materials, including textile accessories, fabric, and other necessary items. When it comes to fabric purchases, the ordering customers specify their preferred suppliers to the company. Our focus was primarily on purchasing textile accessories, which constitute a crucial aspect due to their diversity and cost implications. Furthermore, while this company maintains a detailed database of these items, it lacks systematic supplier selection and evaluation methods. Historically, purchasing activities and operations have depended solely upon the expertise and experience of the procurement manager. In this practical application, to implement the proposed methods, we organized and compiled successful procurement actions, which formed the database for the current supplier selection analysis. Consequently, the sorted and filtered database comprised 20 distinct textile accessories, 46 suppliers, and 20 purchase orders.

3.2. Assessment and selection of suppliers using the proposed models

Within this section, the hybrid proposed models were used to identify the most suitable suppliers for procuring textile supplies and accessories from three suppliers (S1, S2, and S3). The overarching objective in this scenario revolves around procuring buttons with reference 002. In this example, two

Table 14. Weighted normalized fuzzy decision matrix

Suppliers	Price					Quality					Compliance of quantity					Compliance of delay					\tilde{f}_i				
	0.00	0	0	0	0	0.79	0.95	0.97	1	0.72	0.93	0.97	1.00	0.43	0.83	0.94	1.00	0	0	0	0	0	0	0	0
	0.00	0.94	0	0	0	0.79	0.87	0.93	1	0.72	0.93	0.97	1.00	0.00	0.68	0.76	1.00	0	0	1	0	0	0	0	0
	0.00	1.03	0	0	0	0	0	0.79	0.87	0.72	0.93	0.97	1.00	0.87	1.00	1.00	1.00	0	0	0	0	0	0	0	0

Table 15. Crisp value

	$d(\tilde{f}_i)$	Rank
S1	0	2
S2	0.1	1
S3	0	3

decision-makers were used. As criteria, price, quality, compliance of quantity, and compliance of delay were used.

AHP–fuzzy-TOPSIS model

Step 1: Establish linguistic variables and terms

In our case, criteria represent variables:

- Price per piece
- Quality
- Compliance of quantity
- Compliance of delay

Fuzzy set for each variable:

Three classes are chosen for each criterion:

- Low
- Medium
- High

Step 2: Construct membership functions

The categories for each variable were established with the contribution of a purchasing expert, which are presented in Table 5 and illustrated in Figure 3.

Step 3: Assignment rating to the alternatives to create a fuzzy decision matrix, as presented in Table 6.

We propose establishing a decision group comprising two members. This group of decision-makers will employ linguistic terms to assess each alternative for every criterion. The decisions of each decision-maker are presented in Table 6.

Step 4: Transform the linguistic term into a fuzzy number, as presented in Table 7.

Step 5: Aggregate the alternative fuzzy decision matrix

All fuzzy decision matrices are combined into one matrix, as presented in Table 8.

Step 6: Normalize the fuzzy decision matrix, as mentioned in Table 9.

Table 16. Weighted normalized fuzzy decision matrix

Suppliers	Price			Quality				Compliance of quantity				Compliance of delay				F				
	0	0.00	0	0	0.03	0.11	0.12	0.15	0.05	0.16	0.20	0.22	0.12	0.40	0.50	0.56	0.20	0.67	0.81	0.93
S1	0	0.00	0	0	0.03	0.11	0.12	0.15	0.05	0.16	0.20	0.22	0.12	0.40	0.50	0.56	0.20	0.67	0.81	0.93
S2	0	0.02	0	0	0.03	0.06	0.09	0.15	0.05	0.16	0.20	0.22	0.00	0.28	0.34	0.56	0.08	0.52	0.63	0.93
S3	0	0.10	0	0	0.00	0.00	0.03	0.06	0.05	0.16	0.20	0.22	0.44	0.56	0.56	0.56	0.48	0.82	0.79	0.84

Table 17. Crisp value

	$d(\tilde{r}_i)$	Rank
S1	0.65	2
S2	0.54	3
S3	0.73	1

Price was considered as a non-benefit criterion, and quality, compliance of quantity, and compliance of delay were considered as benefit criteria.

Step 7: Determine each criterion weight, as presented in Table 10.

Step 8: Compute the weighting of the normalized matrix, as presented in Table 11.

Step 9: Compute the fuzzy positive ideal solution (FPIS) and the fuzzy negative ideal solution (FNIS), as presented in Table 12.

Steps 10 and 11: Determine the distance from each alternative to the FPIS/NIS and calculate the closeness coefficient of each alternative, as presented in Table 13.

According to Table 13, supplier S1 is the best choice.

AHP–fuzzy-WPM model

The results obtained from steps 1 to 7 in the AHP–fuzzy-WPM method align closely with those obtained in the AHP–fuzzy-TOPSIS approach, as presented in the description of the AHP–fuzzy-WPM model.

Step 8: Compute the weighted normalized fuzzy decision matrix, as presented in Table 14.

Step 9: Compute a crisp value, as presented in Table 15.

As observed from Table 15, supplier S2 is the best choice.

AHP–fuzzy-WSM model

The results from steps 1 to 7 in the AHP–fuzzy-WSM method align closely with those obtained in the AHP–fuzzy-TOPSIS approach, as presented in the description of the AHP–fuzzy-WSM model.

Step 8: Compute the weighted normalized fuzzy decision matrix, as presented in Table 16.

Step 9: Compute a crisp value, as presented in Table 17.

Table 17 shows that supplier S3 is the best choice.

Table 18. Evaluation test

No. purchase order	Article	Selected supplier by the company	Supplier chosen by AHP–fuzzy-TOPSIS	Rank of the supplier	Supplier chosen by AHP–fuzzy-WSM	Rank of the supplier	Supplier chosen by AHP–fuzzy-WPM	Rank of the supplier
1	Ar1	FX	FX	1	FZ	2	FY	2
2	Ar2	AY	AY	1	AY	1	AY	1
3	Ar3	FR	FR	1	FA	2	FA	2
4	Ar4	XA	XA	1	XR	2	XS	2
5	Ar5	ZD	ZA	3	ZD	1	ZC	2
6	Ar6	Y1	Y1	1	Y2	2	Y2	2
7	Ar7	A2	A1	2	A2	1	A2	1
8	Ar8	BR	BR	1	BR	1	BR	1
9	Ar9	FH	FH	1	FH	1	FH	1
10	Ar10	XR	XR	1	XB	3	XB	2
11	Ar11	XY	XY	1	XZ	2	XZ	2
12	Ar12	CR	CF	2	CR	1	CR	1
13	Ar13	G1	G1	1	G2	2	G2	2
14	Ar14	FR	FR	1	FS	2	FS	2
15	Ar15	BT	BG	2	BT	1	BT	1
16	Ar16	FT	FT	1	FT	2	FT	2
17	Ar17	GH	GT	2	GH	1	GH	1
18	Ar18	VH	VZ	2	VH	1	VH	1
19	Ar19	SML	SML	1	SML	1	SML	1
20	Ar20	SF	SF	1	SF	1	SF	1

Table 19. Statistical analysis comparing each pair of methods

Hybrid method	σ_{xy}	σ_x	σ_y	R_{xy}	Standard deviation
AHP–fuzzy-TOPSIS and AHP–fuzzy-WSM	0.0068	0.11	0.10	0.6	0.09
AHP–fuzzy-TOPSIS and AHP–fuzzy-WPM	0.0117	0.11	0.15	0.71	0.07
AHP–fuzzy-WSM and AHP–fuzzy-WPM	0.0124	0.10	0.15	0.78	0.06

Table 20. ANOVA for the three MCDM methods

Source of variation	SS	Df	MS	F	p-value	F criteria
Between groups	0.11186333	2	0.05593167	3.49983533	0.03684409	3.15884272
Within groups	0.91093	57	0.01598123			
Total	1.02279333	59				

4. Results and discussion

4.1. Assessment tests

To assess the effectiveness of the AHP–fuzzy-TOPSIS, AHP–fuzzy-WSM, and AHP–fuzzy-WPM methods in the assessment and selection of optimal suppliers, a set of data comprising 20 orders was utilized. Subsequently, this dataset was validated in a real case. It is important to note that the purchase orders assigned to specific suppliers were chosen from those who had previously been successful in the supplier evaluation, selection, and procurement processes. These purchase requisitions were chosen based on criteria, including high quality, reasonable pricing, time delivery, and meeting the specified quantity. In this study, two decision-makers were used, and these two decision-makers have professional careers in textile purchasing. As criteria, we used price, quality, compliance of quantity, and compliance of delay. Table 18 illustrates the enterprise's supplier rank in the supplier list identified by the AHP–fuzzy-TOPSIS, AHP–fuzzy-WSM, and AHP–fuzzy-WPM methods.

4.2. Result analysis

Statistical analysis was performed between the two methods based on these results. We utilized the results of the top-ranked supplier from each method, and analysis of variance (ANOVA) was established to ascertain whether the differences between the means of the groups were statistically meaningful or not. The analysis of the results is illustrated in Tables 19 and 20.

Table 19 displays the correlation coefficients calculated to establish the dependence between the supplier rankings obtained

from the AHP–fuzzy-TOPSIS, AHP–fuzzy-WSM, and AHP–fuzzy-WPM methods. Consequently, a significant correlation was observed among the different pairs of MCDM methods with correlation coefficient values (R_{xy}) exceeding 0,5.

According to the results presented in Table 20, the p -value is below 0.05. Hence, the null hypothesis is not accepted, meaning that not all population means are identical. In conclusion, we found statistically meaningful differences between the means of the groups. Another study was done to determine if the distribution of the value of the first rank for each model obeyed the normal distribution or not. The results are illustrated in Table 21 and Figure 4.

Figure 4 and Table 21 show that 68% of values are in the interval $[\mu - \sigma, \mu + \sigma]$, 95% are in the interval $[\mu - 2\sigma, \mu + 2\sigma]$, and 99.7% are in the interval $[\mu - 3\sigma, \mu + 3\sigma]$. According to these results, we can conclude that the distribution of the value of the 1st rank for each method obeys the normal distribution. Besides, based on Table 18, we calculated the coincidence ratio of supplier scores between the methods used and the selections made by the purchasing manager for all successful purchase orders in the database. The coincidence ratio results are presented in Figure 5.

Figure 5 indicates that the AHP–fuzzy-TOPSIS model exhibits the highest proportion of coincidence in supplier scores with the decisions made by the purchasing manager compared with other models. This percentage is equal to 70%. In our case study, the results demonstrate that the AHP–fuzzy-TOPSIS method excels in choosing the best and optimal supplier.

Table 21. Normal distribution parameters

Methods	μ : mean	σ : standard deviation	Percentage between $\mu - \sigma$ and $\mu + \sigma$	Percentage between $\mu - 2\sigma$ and $\mu + 2\sigma$	Percentage between $\mu - 3\sigma$ and $\mu + 3\sigma$
AHP-Fuzzy-TOPSIS	0.619	0.11	67.9%	95%	99.7%
AHP-Fuzzy-WSM	0.682	0.10	68%	94.9%	99.9%
AHP-Fuzzy-WPM	0.5775	0.15	68%	95%	99.6%

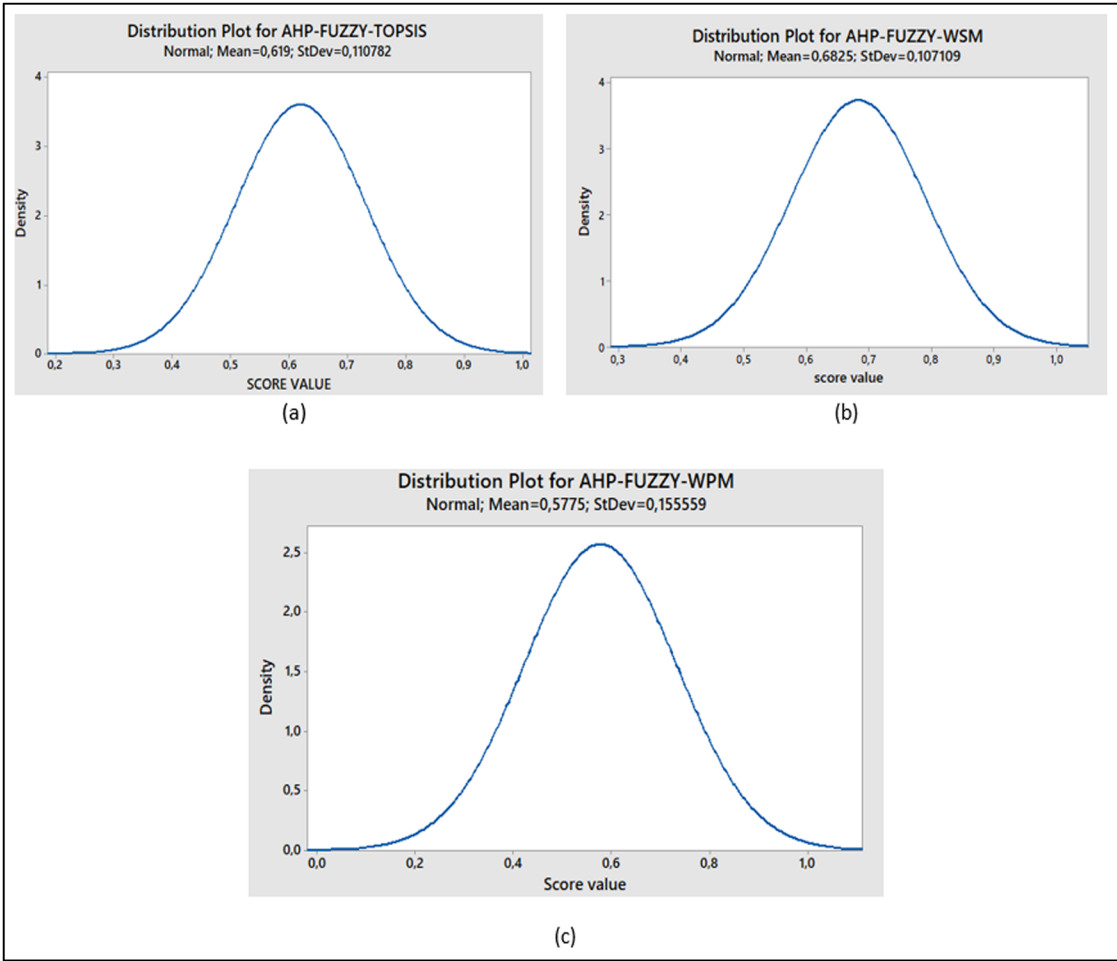


Figure 4. Distribution plot for the hybrid MCDM models: AHP–fuzzy-TOPSIS (a), AHP–fuzzy-WSM (b), and AHP–fuzzy-WPM (c).

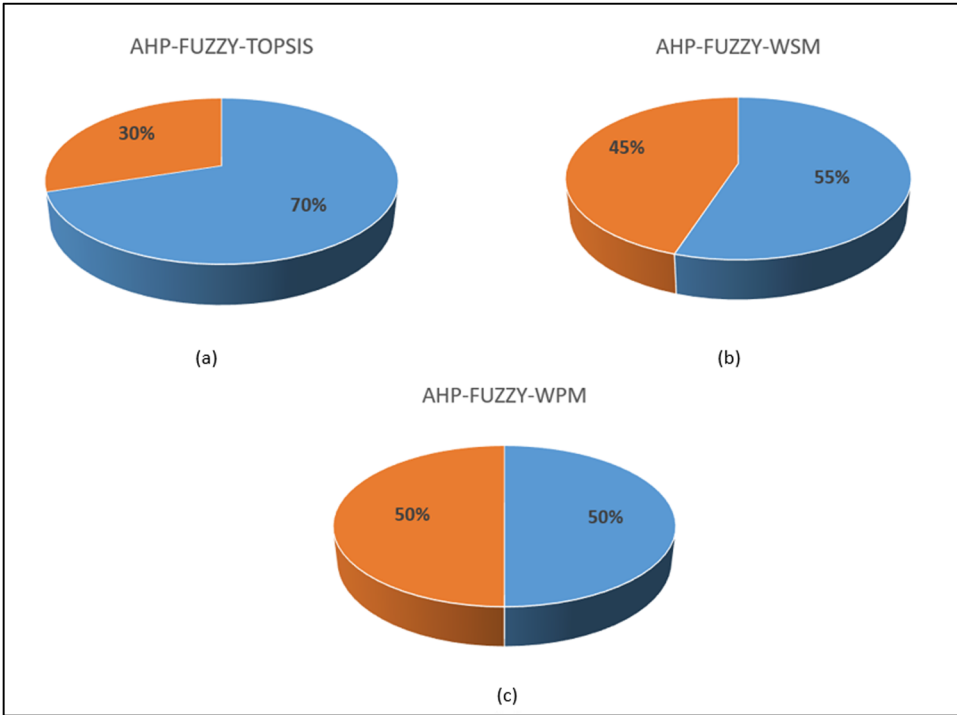


Figure 5. Ratio of coincidence of supplier rankings between the AHP–fuzzy-TOPSIS (a), AHP–fuzzy-WSM (b), and AHP–fuzzy-WPM (c) models and the decision made by the supply chain manager.

The screenshot displays the MCMCD software interface for industrial application in supplier selection. The interface is divided into several sections:

- Method Selection:** A dropdown menu for 'Method' is set to 'AHP-FUZZY-TOPSIS'. Other fields include 'decision number' (2), 'Purchase Order' (123), 'Client' (CA), and 'Article' (stopper).
- Decision Maker 1 and 2:** Two tables for 'decision maker 1' and 'decision maker 2' showing criteria (supplier, article, costM1) and values for suppliers F1, F2, and F3.
- STEP2:** A button labeled 'combined fuzzy decision matrix'.
- STEP3:** A button labeled 'Normalize the fuzzy decision matrix'.
- STEP4:** A button labeled 'compute the weighted normalized fuzzy decision matrix'.
- STEP5:** A button labeled 'compute the fuzzy positive ideal solution (FPIS) and the'.
- Calculate rank:** A section with a 'score' input field and a table showing the final ranking of suppliers.

supplier	article	costM1	costM2	costM3	rank
F1	stopper	0	0	0	1
F2	stopper	0	0,02	0	3
F3	stopper	0	0,1	0	2

Figure 6. Interface for industrial application in supplier selection.

4.3. Industrial applications

During this stage, we developed an application to facilitate swift and effective supplier evaluation and selection decisions. This application was based on the AHP–fuzzy-TOPSIS method. In this industrial application, Visual Basic .NET (2015 version) was employed as a development program. Microsoft Access (2016 version) as a database. Figure 6 shows the interface of our industrial application.

In the apparel industry, we deployed a digital decision support application utilizing the database discussed in Section 4.1. We then compared the outcomes derived from the application with the decisions made by the company, presenting the results in Figure 7.

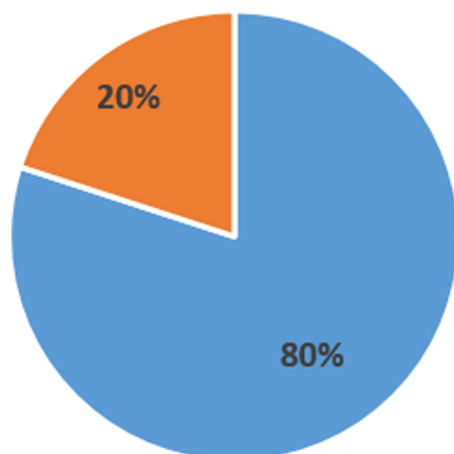


Figure 7. Industrial application result.

As shown in Figure 7, the percentage of similarity in supplier scores between our software's results and the decisions made by the supply chain manager was 80%. This result is deemed highly satisfactory. In future studies, the database will be further expanded to encompass all the company's real cases to improve the performance of decision support applications.

5. Conclusions

In this research, three fuzzy hybrid methods were developed to select suppliers for a company specializing in the fabrication of denim. The methods used are crucial for making decisions or evaluating multiple options in situations where no option is ideal. In our article, three integrated approaches combining the AHP with the fuzzy-TOPSIS, fuzzy-WSM, and fuzzy-WPM models were employed. Subsequently, we used these methods within a clothing company. Consequently, we found that the AHP–fuzzy-TOPSIS method is better and more practical compared to the AHP–fuzzy-WSM and the AHP–fuzzy-WPM methods in assessment and choosing the best supplier. The coincidence ratio between the obtained solutions using the AHP–fuzzy-TOPSIS model with those corresponding to the firm's preferred choice is equal to 70%. Based on this percentage, we can infer that the AHP–fuzzy-TOPSIS method is well-suited for forecasting, identifying, and selecting the optimal suppliers within the clothing company's procurement process. Moreover, this approach can be used in other industrial sectors. Indeed, The AHP–fuzzy-TOPSIS method is thus more effective than the other models in managing subjectivity, uncertainty, and complexity. Providing a structured framework for decision-making, this model integrates qualitative and quantitative approaches with a solid ranking methodology, thus allowing

decision-makers to make more effective and reliable decisions in complex decision environments. In future perspectives, other models can be implemented such as the ANP, the neural network, and heuristic methods. Then, we will integrate the most efficient models in this application to play the role of a good decision tool in the selection and assessment of suppliers and subcontractors.

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Conflict of interest: The authors state no conflict of interest.

Data availability statement: The datasets generated during and/or analysed during the current study are available from the corresponding author on reasonable request.

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