

## Research Article

Ulrich Heber\*, Andreas Irrgang, and Johannes Schaffenroth

# Spectral energy distributions and colours of hot subluminous stars

<https://doi.org/10.1515/astro-2018-0008>

Received Nov 22, 2017; accepted Nov 30, 2017

**Abstract:** Photometric surveys at optical, ultraviolet, and infrared wavelengths provide ever-growing datasets as major surveys proceed. Colour-colour diagrams are useful tools to identify classes of star and provide large samples. However, combining all photometric measurements of a star into a spectral energy distribution will allow quantitative analyses to be carried out. We demonstrate how to construct and exploit spectral energy distributions and colours for subluminous B (sdB) stars. The aim is to identify cool companions to hot subdwarfs and to determine atmospheric parameters of apparently single sdB stars as well as composite spectrum sdB binaries. We analyse two sdB stars with high-quality photometric data which serve as our benchmarks, the apparently single sdB HD 205805 and the sdB + K5 binary PG 0749+658, briefly present preliminary results for the sample of 142 sdB binaries with known orbits, and discuss future prospects from ongoing all-sky optical space- (Gaia) and ground-based (e.g. SkyMapper) as well as NIR surveys.

**Keywords:** stars: early type -subdwarfs - Techniques: photometric

## 1 Introduction

Optical photometry and spectroscopy provide the observational basis for astronomy. Ongoing large photometric surveys provide a huge amount of photometric measurements in several optical passbands, which can be used to identify candidate hot subluminous stars, though spectroscopy is needed for proper spectral typing. However, optical photometry is much more than a mere target selection tool. Time-series photometry (light curves) are a crucial ingredient for asteroseismology of pulsating stars and to identify compact binaries from eclipses, reflection effects, and ellipsoidal variations. Single-epoch observations, however, provide crucial information as well. Spectroscopic distances rely on at least one measured apparent magnitude. Ultraviolet and infrared surveys, when combined with optical photometry, allow us to construct broad spectral energy distributions (SED), which can be used *e.g.*, to determine the effective temperature of a star, to identify an infrared excess hinting at the presence of a cool

companion, and to quantify interstellar absorption from UV flux depression.

Here we shall not address light variation but restrict ourselves to colour-metric properties of hot subdwarf B (sdB) stars. Several investigations of hot subdwarf stars have made use of single-epoch photometry. With the advent of the International Ultraviolet Explorer (IUE) satellite, crucial information to study hot stars arose. Early attempts to analyse SEDs of sdB stars were carried out by Heber et al. (1984); Heber (1986), and Aznar Cuadrado & Jeffery (2001) by combining low resolution UV spectra from IUE with optical photometry. Colour-colour diagrams combining infrared and optical magnitudes are important tools to identify composite objects, such as sdB stars with F/G/K companions (e.g. Stark & Wade 2003; Green et al. 2008).

Subdwarf B stars are core helium burning stars of half a solar mass and in the Hertzsprung Russell diagram they form the extreme horizontal branch. Because radial velocity surveys have shown that the fraction of close binaries amongst single-lined (SB1) sdB stars is as high as 50 %, common envelope evolution plays an important role in the formation of sdB stars. About 30% of the sdB stars show composite colours, that is they have companions of spectral types F, G, or K. In many cases the companions to SB1 systems have been found to be white dwarfs, but low mass main-sequence stars (spectral type M) and brown dwarfs have been found as well (see Heber 2009, 2016, for reviews). Because it is often very difficult to clarify the nature

**Corresponding Author:** **Ulrich Heber:** Dr. Remeis-Sternwarte & ECAP, University of Erlangen-Nürnberg, Germany; Email: [ulrich.heber@fau.de](mailto:ulrich.heber@fau.de)

**Andreas Irrgang:** Dr. Remeis-Sternwarte & ECAP, University of Erlangen-Nürnberg, Germany; Email: [andreas.irrgang@fau.de](mailto:andreas.irrgang@fau.de)

**Johannes Schaffenroth:** Dr. Remeis-Sternwarte & ECAP, University of Erlangen-Nürnberg, Germany; Email: [johannes.schaffenroth@fau.de](mailto:johannes.schaffenroth@fau.de)

of the companions from optical data alone, broad SEDs are the method of choice to constrain the companions' properties and constrain their nature.

We describe a method to construct broad SEDs by combining measurements in various photometric systems from the ultraviolet to the infrared in Sect. 2. Synthetic photometry for various photometric systems are calculated from grids of appropriate model atmospheres (Sect. 3). An objective method to derive various parameters from observed SEDs is presented in Sect. 4 and preliminary results are discussed in Sect. 5. We conclude with an outlook.

## 2 Constructing observational SEDs

The SEDs of the program stars were constructed from photometric measurements, ranging from the ultraviolet to the infrared, collected from literature. To eliminate the steep slope of the SED we plot the flux density times the wavelength to the power of three ( $F_\lambda \lambda^3$ ) as a function of wavelength throughout this paper.

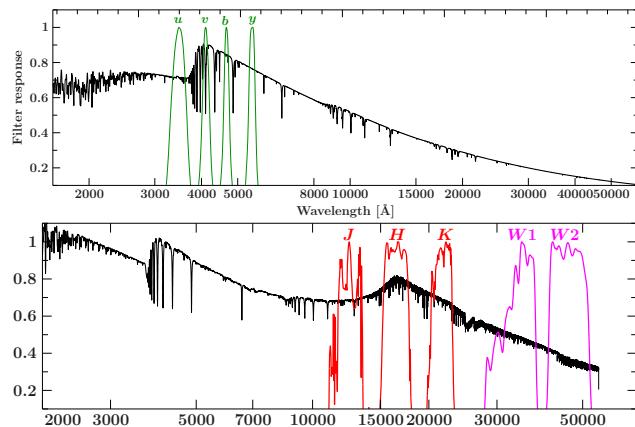
### 2.1 Photometric data

The visual range is covered by SDSS (Alam *et al.* 2015) and APASS (Henden *et al.* 2016) data as well as magnitudes and colours in the Johnson-Cousins, Strömgren (see Figure 1), and Geneva systems, which are collected using Vizier as well as the Subdwarf Database<sup>1</sup> by Østensen (2006).

Ultraviolet fluxes are important to constrain the atmospheric parameters of a hot subdwarf and were extracted from observations by the International Ultraviolet Explorer (IUE), available in the MAST<sup>2</sup> archive.

Infrared photometry is of particular importance for binary systems that contain a cool companion because an IR excess is expected. Available infrared data were taken from ALLWISE (Wright *et al.* 2010; Cutri *et al.* 2013), 2MASS (Skrutskie *et al.* 2006), and UKIDSS (Lawrence *et al.* 2007, see Figure 1).

The photometric datasets are inhomogeneous, both with respect to bandwidth as well as to accuracy. Ultraviolet spectra from IUE cover the wavelength range from 1150 Å to 3150 Å at a spectral resolution of 6 Å. The optical spectral range is covered by several filters, both narrow band (e.g. Strömgren) and wide-band (e.g. Sloan or John-



**Figure 1.** Response function for optical (Strömgren, top) and infrared (2MASS and WISE, bottom) photometric systems. Synthetic SEDs are plotted as  $F_\lambda \lambda^3$ . In the top panel a single SED is plotted, while for the bottom panel a composite SED is used. Both are scaled for comparison to the transmission functions.

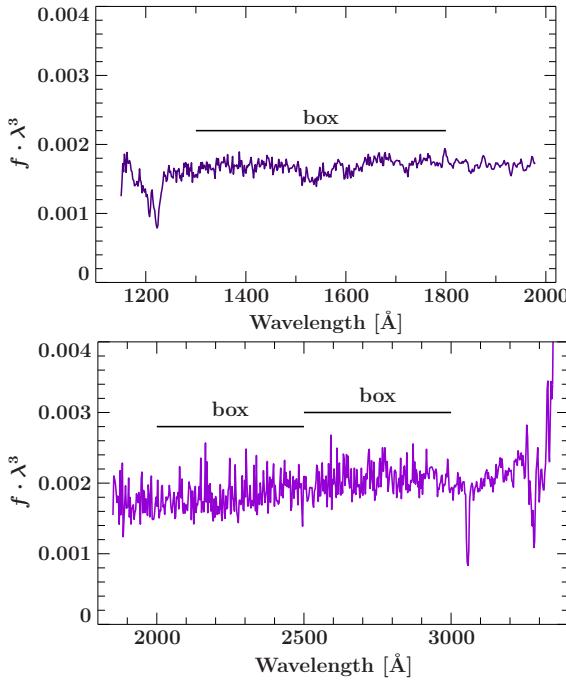
son), while the infrared is usually represented by five wide-band filters (J, H, K, W1, and W2).

### 2.2 Ultraviolet fluxes from IUE spectra

The IUE satellite provided UV spectra for two wavelength ranges; the short (SW, 1150–1975 Å) and long (1910–3150 Å) wavelength range. Each spectrograph offered both high and low resolution modes, with spectral resolutions of 0.2 and 6 Å respectively, as well as two entrance apertures each, a small circular aperture with a 3 arcsec diameter and a large rectangular aperture of 10 by 20 arcsecs. We discarded spectra at high-resolution as well as those taken through a small aperture, because the flux calibration is less accurate than that for the large-aperture, low-resolution spectra. Because we have to combine them with broad and intermediate band optical and infrared photometry, we defined a suitable set of filters to derive UV-magnitudes from IUE spectra (see Figure 2). Three box filters, which cover the spectral ranges 1300–1800 Å, 2000–2500 Å, and 2500–3000 Å, are defined to extract magnitudes from the IUE spectra. The box filters were designed in order to avoid the boundaries of the SW and LW wavelength ranges because of the increasing noise level, and the region around the Lyman-alpha line because of the contribution by interstellar gas absorption. The mid-UV filter was designed to include the UV absorption bump at  $\approx$  2200 Å of interstellar absorption (see Figure 3), which is important to determine the interstellar reddening parameter  $E(B-V)$ .

<sup>1</sup> <http://catserver.ing.iac.es/sddb/>

<sup>2</sup> <http://archive.stsci.edu/>



**Figure 2.** Box filters to convert IUE low resolution spectra to UV magnitudes. One box is placed in the wavelength range covered by the short wavelength camera (SWP, upper panel) and two in the regime covered by the long wavelength cameras (LWR/LWP, lower panel).

### 3 Synthetic SEDs and colours

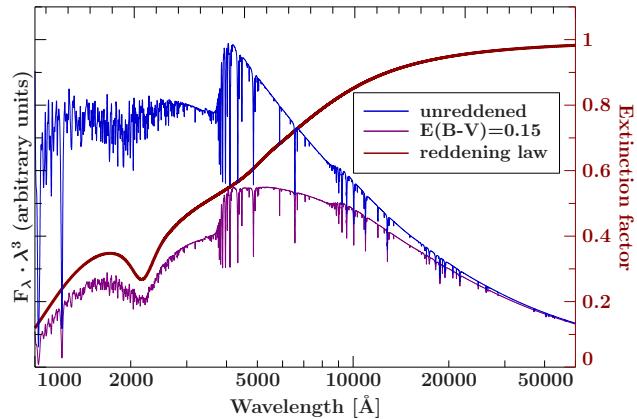
The magnitude  $\text{mag}_x$  of an arbitrary photometric passband  $x$  is defined as

$$\text{mag}_x = -2.5 \log \left( \frac{\int_0^{\infty} r_x(\lambda) f(\lambda) \lambda d\lambda}{\int_0^{\infty} r_x(\lambda) f^{\text{ref}}(\lambda) \lambda d\lambda} \right) + \text{mag}_x^{\text{ref}} \quad (1)$$

where  $r_x(\lambda)$  is the response function of the filter (see Figure 1 for examples) and  $f(\lambda)$  the flux at the photon-counting detector. The flux of a reference star (usually Vega)  $f^{\text{ref}}$  is needed to set the zero point of the filter to a predefined magnitude  $\text{mag}_x^{\text{ref}}$ .

The stellar flux at Earth  $f(\lambda)$  can be calculated from the model flux at the stellar surface  $F(\lambda)$  and the angular diameter of the star  $\Theta (= 2R_*/d)$ , which is two times the stellar radius  $R_*$  divided by the distance, from which we obtain  $f(\lambda) = \Theta^2 F(\lambda)/4$ .

To account for interstellar extinction, the synthetic flux is multiplied by a reddening factor  $10^{-0.4A(\lambda)}$ . The extinction in magnitude at wavelength  $\lambda$ ,  $A(\lambda)$ , as a function of the colour excess  $E(B - V)$  and the extinction parameter  $R_V = A(V)/E(B - V)$  (defaulted to 3.1) is taken from



**Figure 3.** The impact of interstellar reddening on SEDs of a B star for moderate interstellar reddening by  $E(B-V)=0.15$  mag. The reddening law is from Fitzpatrick (1999).

Fitzpatrick (1999, see Figure 3). The final expression to calculate a synthetic magnitude, therefore, reads as

$$\text{mag}_x = -2.5 \log \left( \frac{\Theta^2 \int_0^{\infty} r_x(\lambda) 10^{-0.4A(\lambda)} F(\lambda) \lambda d\lambda}{4 \int_0^{\infty} r_x(\lambda) f^{\text{ref}}(\lambda) \lambda d\lambda} \right) + \text{mag}_x^{\text{ref}}. \quad (2)$$

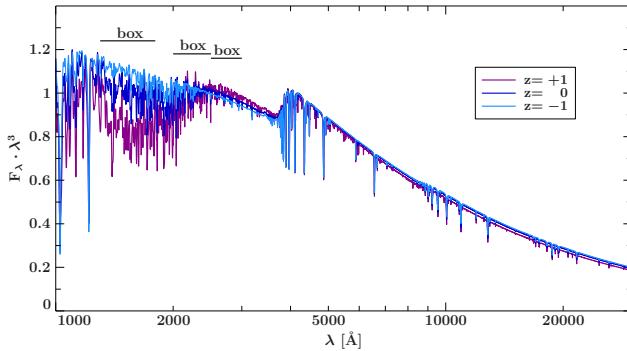
### 3.1 Grids of synthetic SEDs and colours

We aim to model the observed SEDs and colours of single sdB stars or SB1 binaries, as well as composite spectrum systems consisting of a hot subdwarf and a late-type main-sequence star.

#### 3.1.1 SEDs of hot subdwarf stars

Subluminous B stars are known to show peculiar chemical abundance patterns (Heber 2009, 2016) characterized in general by depletions of light metals (C to Ca) and enrichment of heavy metals by very large factors with respect to solar composition. However, star-to-star scatter is large. Naslim et al. (2013) suggested an average abundance pattern, which we adopted for the model calculations. For the elements not listed in Naslim et al. (2013) the reference abundance is solar (Asplund et al. 2009).

In order to synthesize the SED of a hot subdwarf star a grid of model atmospheres was calculated using the ATLAS12 code (Kurucz 1996) with effective temperatures ranging from 15000 K to 55000 K and surface gravities from 4.6 to 6.2. The helium abundance was fixed to a low



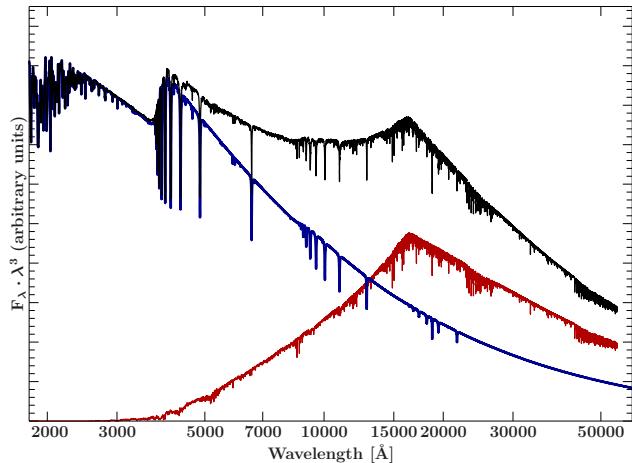
**Figure 4.** Model SED for different metallicities (scaled typical sdB pattern from Naslim *et al.* 2013). The UV box filters are marked by horizontal lines. Note that the flux depression is strongest in the shortest wavelength UV box filter.

value of one hundredth the solar abundance and the logarithmic "metallicities"  $z$  are scale factors with respect to the abundance pattern of Naslim *et al.* (2013). The synthetic spectra cover the wavelength range from 300 Å to 100 000 Å (far UV to mid infrared). The logarithmic metallicity  $z$  is allowed to vary between  $-1$  and  $+1$  (a tenth or ten times the typical composition of a subdwarf B star). Please note that iron and nickel are the dominant absorbers and have the greatest influence on the metallicity  $z$  because they have many absorption lines in the FUV and their absolute abundance is high. As demonstrated in Figure 4, the metallicity essentially effects the UV spectral range, most significantly the short wavelength UV box filter. Hence it might be possible to derive the metallicity of the sdB if such UV measurements were available.

Recently, several improvements have been implemented in the ATLAS12 code (Irrgang, in prep.), the most important of which is the treatment of high series members of the hydrogen and ionized helium line series, following Hubeny *et al.* (1994). This is of particular importance to model the Balmer jump.

### 3.1.2 SEDs of cool stars

For cool stars a grid of PHOENIX models calculated by Husser *et al.* (2013) is used <sup>3</sup>. The synthetic SEDs cover the wavelength range from 500–55 000 Å. The parameter range is confined to effective temperatures between 2300 K and 12 000 K, surface gravities between 2 and 5 dex, and the helium content is set at the solar value.



**Figure 5.** Synthetic SED for a composite-spectrum sdB binary. The sdB model (blue) is computed with ATLAS12 for  $T_{\text{eff}}=30000$  K. The flux distribution of the cool companion (red) is taken from the PHOENIX grid for a  $T_{\text{eff}}=5000$  K (Husser *et al.* 2013).

### 3.1.3 Combining SEDs of sdB and cool stars

In order to combine the spectra of the two components, the surface ratio  $S$  needs to be determined. This adds another parameter, from which the angular diameter of the companion  $\Theta^c$  can be derived.

## 4 Photometric analysis methodology

To facilitate objective and efficient photometric analyses, we have developed a grid-based fitting routine. It is based on  $\chi^2$  minimization tools provided by the Interactive Spectral Interpretation System (Houck & Denicola 2000) to find the global best-fit in the multi-parameter space.

The six parameters considered to model SEDs and colours of the sdB stars are

- the angular diameter,  $\Theta$
- the effective temperature,  $T_{\text{eff}}^{\text{sdB}}$
- the surface gravity,  $\log g^{\text{sdB}}$
- Helium abundance,  $\log(n(\text{He})/n(\text{all}))$
- "Metallicity"  $z$  (scaled typical abundance pattern (Naslim *et al.* 2013))
- the interstellar reddening parameter,  $E(B-V)$

Adopting the canonical mass for the sdB star, we also derive the stellar distance.

<sup>3</sup> <http://phoenix.astro.physik.uni-goettingen.de/>

## 4.1 Composite spectra

In the case of binary stars we may observe a composite spectrum, which increases the parameter space by the parameters describing the companion as well as the surface ratio S of both stars.

- Effective temperature,  $T_{\text{eff}}^c$
- Surface gravity,  $\log g^c$
- Metallicity, [Fe/H]

However, usually the surface gravity and metallicity of the cool star is unconstrained. Therefore, they were kept fixed to  $\log g=4.5$  and 1/10 solar metallicity.

## 4.2 Determination of uncertainties

Uncertainties are derived from the  $\chi^2$  statistics. The parameter under consideration is increased/decreased – while all remaining parameters are fitted to account for possible correlations – until a certain increment  $\Delta\chi^2$  from the minimum  $\chi^2$  is reached. The value chosen for  $\Delta\chi^2$  determines the confidence level of the resulting interval. For instance,  $\Delta\chi^2 = 1$  yields single-parameter  $1\sigma$  uncertainties.

The photometric data were compiled from various sources and, thus, are quite inhomogeneous, in particular with respect to the stated uncertainties. The following strategy was employed to cope with this: (i) Data flagged in catalogs as uncertain and obvious outliers are omitted. (ii) Magnitudes and colours without given errors are assigned typical uncertainties of 0.05 and 0.025 mag, respectively. (iii) To account for systematic shortcomings (e.g. in the system response curves, synthetic SEDs, or calibration of the data), a generic error of 0.015 mag is added in quadrature to all observed values. (iv) Eventually, all uncertainties are rescaled by a common factor to ensure a reduced  $\chi^2$  of 1 at the best fit.

## 5 Results

We present preliminary results for two sdB stars, the apparently single HD 205805 and the composite spectrum sdB binary PG 0749+658. These stars were chosen because extensive, high-quality photometric observations in all relevant wavelength regimes are available.

## 5.1 HD 205805 – a benchmark single sdB star

HD 205805 is one of the brightest sdB stars and, therefore, ample photometric measurements are available for the optical regime including Strömgren indices, in particular the  $H\beta$  index. Ultraviolet spectra have also been observed by IUE as well as infrared fluxes. HD 205805 is one of a handful of sdB stars that have such good photometric data coverage and, therefore, provides our benchmark for SED and colour fitting.

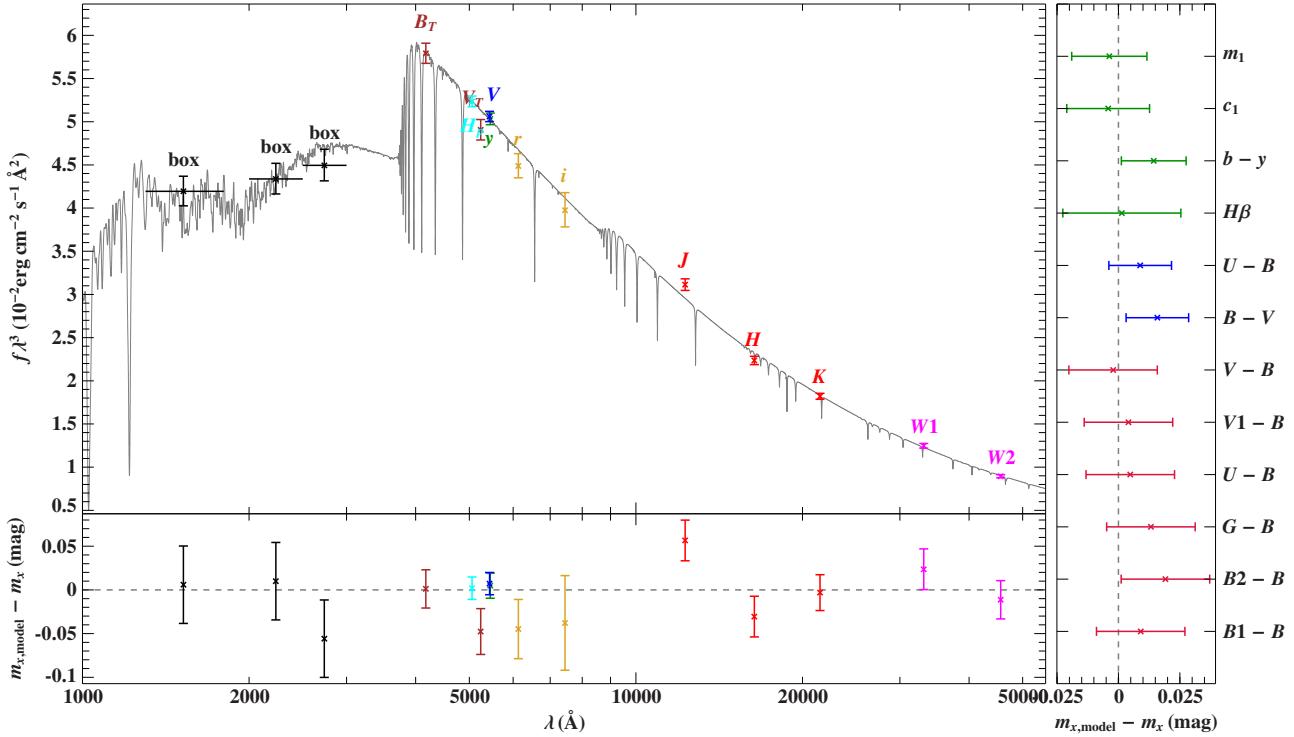
High resolution optical spectra taken with the FEROS spectrograph at the ESO 2.2m telescope also became available through the ESO archive. We analysed five FEROS spectra using an updated version of the grid of synthetic hydrogen and helium spectra calculated from metal-line blanketed LTE models described by Heber *et al.* (2000). The resulting atmospheric parameters are  $T_{\text{eff}}=25114\pm214$  K,  $\log g=4.96\pm0.09$ , and a helium to hydrogen ratio of  $\log(n_{\text{He}}/n_{\text{H}})=-1.93\pm0.03$  by number.

The SED fit and the corresponding confidence map for the error estimation of  $T_{\text{eff}}$  are shown in Figures 6 and 8, respectively. The resulting parameters ( $T_{\text{eff}}=25338^{+463}_{-423}$  K,  $\log g=5.21\pm0.21$ ) are in perfect agreement with those derived from spectroscopy. The metal abundance parameter ( $z=0.09^{+0.17}_{-0.28}$ ) points to a normal sdB composition for HD 205805 consistent with the metal abundances derived by Geier (2013).

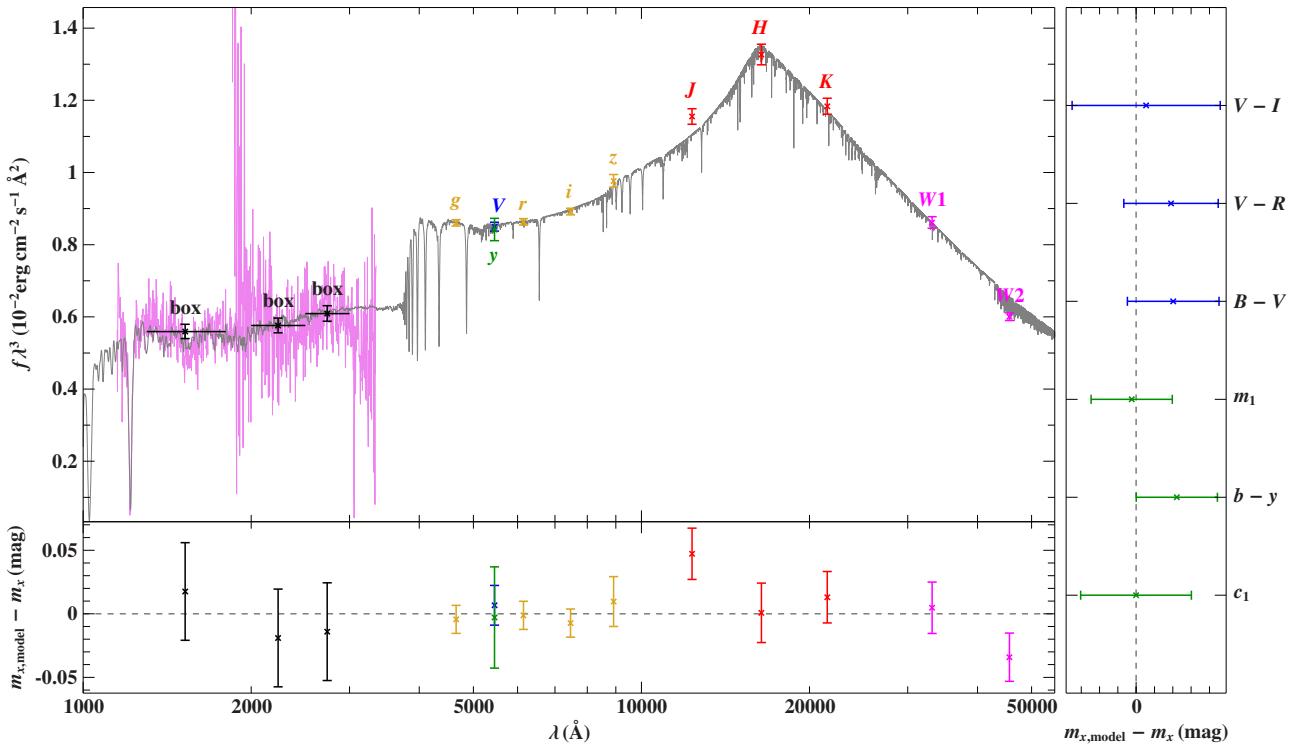
## 5.2 The composite spectrum sdB binary PG 0749+658

The sdB star PG 0749+658 was classified as sdB-O by Green *et al.* (1986). A spectral analysis of the optical spectrum resulted in an effective temperature  $T_{\text{eff}}=24600$  K and surface gravity  $\log g=5.54$  (Saffer *et al.* 1994). Its composite nature was realised by Allard *et al.* (1994) from BVRI photometry and the faint companion was classified as spectral type K5.5, but no significant radial velocity variations were found (Maxted *et al.* 2001; Aznar Cuadrado & Jeffery 2002).

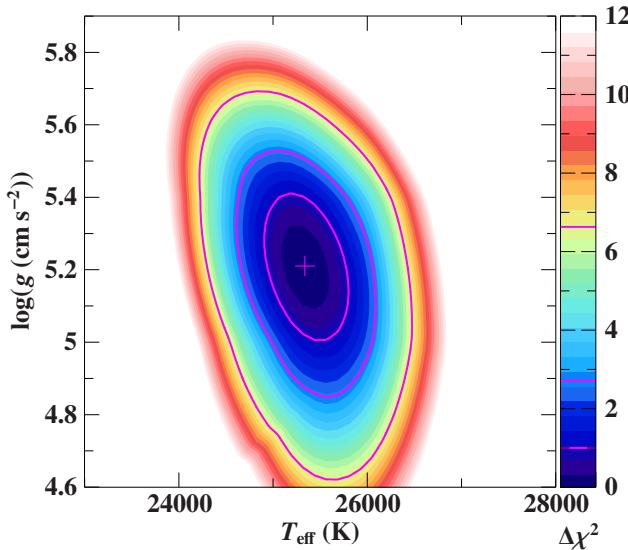
Aznar Cuadrado & Jeffery (2001) determined the effective temperatures for both components from the SED to be  $T_{\text{eff}}=25050\pm675$  K and  $T_{\text{eff}}^c=5600\pm300$  K, while Aznar Cuadrado & Jeffery (2002) analysed the composite spectrum of PG 0749+658 and derived similar temperatures  $T_{\text{eff}}=25400\pm500$  K and  $T_{\text{eff}}^c=5000\pm500$  K. The corresponding gravities were found to be  $5.7\pm0.11$  and  $4.58\pm0.24$  for the sdB and the late-type companion, respectively. Heber *et al.* (2002) derived a considerably lower effective temperature of  $T_{\text{eff}}=22000$  K for the sdB component from the opti-



**Figure 6.** HD 205805: Fit of the SED (top panel) simultaneously with available colours. Residuals are shown in the right hand (colours) and lower (fluxes) panels as magnitudes.



**Figure 7.** Same as Figure 6 but for the composite spectrum of PG 0749+658. The bump in the H band is caused by the onset of H^- absorption.



**Figure 8.** HD 205805: Confidence map for the fit shown in Figure 6. The contour lines refer to single parameter uncertainties of 68%, 90% and 99%, respectively. Single parameter  $1\sigma$  uncertainties are  $\Delta T_{\text{eff}}=400$  K,  $\Delta \log g=0.2$  dex.

**Table 1.** Results of the analyses of the SED (see Figure 7) of PG 0749+658.

	$T_{\text{eff}}$ [K]	$\log g$	$z$	$\theta/10^{-11}$
sdB	$23250^{+555}_{-391}$	$5.290^{+0.19}_{-0.23}$	$-0.16^{+0.29}_{-0.57}$	$2.53 \pm 0.07$
comp.	$4805 \pm 59$	$4.5^*$	$-1^*$	$10.7 \pm 0.4$

\* fixed value

cal SED and attempted to resolve the binary spatially using the Wide Field and Planetary Camera 2 on-board the Hubble Space Telescope, but found it to be unresolved to a limiting angular separation  $<0.2''$  which, at a distance of 580 pc, translates into a separation  $<116$  AU. Ohl *et al.* (2000) determined metal abundances from FUV spectra obtained with FUSE and showed that the sdB is somewhat metal poor in comparison to the typical sdB abundance pattern.

The fit of the observed SED of PG 0749+658 is shown in Figure 7 and the resulting parameters are listed in Table 1. The resulting temperatures of both stars are lower than those derived from spectroscopy. The resulting gravity of the sdB is consistent with the spectroscopic one derived by Saffer *et al.* (1994) to within error limits, but lower than that of Aznar Cuadrado & Jeffery (2002).

## 6 Outlook

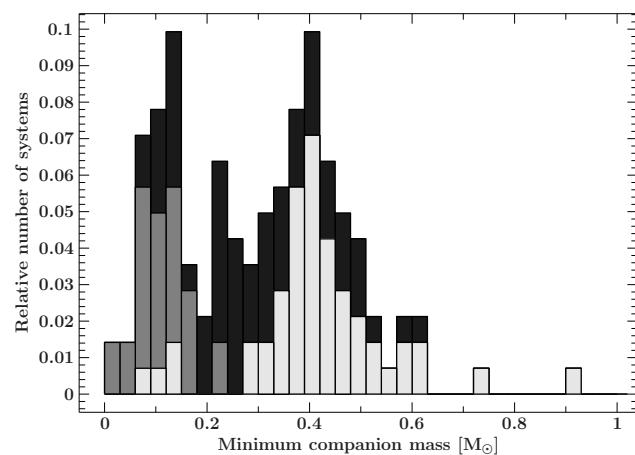
HD 205805 and PG 0749+658 are amongst the best cases, both in terms of available data quality and wavelength coverage. For most of the other known sdB stars, available

datasets are less complete. Hence we can not expect to achieve similar accuracy for the parameters derived from SED fitting, in particular the surface gravity  $\log g^{\text{sdB}}$  will likely be unconstrained as well as the metal abundance parameter  $z$  when no IUE data are available. Because of their large systematic uncertainties, FUV and NUV fluxes from the GALEX mission are not sufficient to replace UV magnitudes from IUE (Kawka *et al.* 2015).

Using mock dataset we shall investigate the quality requirements for observed photometric datasets to derive atmospheric parameters to be conclusive.

### 6.1 The sample of sdB binaries with known orbits

Kupfer *et al.* (2015) and Kawka *et al.* (2015) compiled a list of close binary sdB stars with known orbits and studied their properties (see Figure 9).



**Figure 9.** Companion mass histogram of the sample of sdB binaries with known orbits (Kupfer *et al.* 2015). Systems with white dwarf companions are depicted in light grey, those with M-dwarf companions in grey, and systems for which the nature of the companion is unclear are marked in black. Adapted from Kupfer *et al.* (2015).

We restrict ourselves to the single-lined spectroscopic binaries. Because the companions are unseen, they could be white dwarfs, low mass main sequence stars, or sub-stellar objects. From light variations (reflection effect or ellipsoidal variations) and the mass function, the nature of the companions could be inferred only for about half of the sample (Kupfer *et al.* 2015).

Hence, we embarked on an analysis of their SEDs in order to better constrain the nature of the companions. We compiled available photometric data from the data archives and constructed the SEDs as described in Sect. 2.

The sample contains 142 stars. Twenty-six are reflection effect systems, hence the companions are normal stars, but were excluded from the study because of their light variability. Kupfer *et al.* (2015) suggested that 52 stars host a white dwarf companion. We could model the SEDs of 50 of them by a single synthetic SED, confirming the white dwarf nature of the companion. However, two binaries showed infrared excess and were modelled with a composite SED. The companions are most likely main-sequence stars. For the sixty stars for which the nature of the companion was unclear, we were able to reproduce their observed SED with a single synthetic sdB one, but ten binaries require a composite SED, indicating that the companion is likely a late-type main-sequence star. In the case of the former binaries, additional modelling is required to possibly clarify the nature of their companions. Details will be reported in a subsequent publication.

## 6.2 Gaia, SkyMapper, and other photometric surveys

Because subdwarf O and B stars are hot, the Balmer jump is an important diagnostic tool, which requires measurements of optical, UV (e.g.  $u$ ,  $u'$  or  $U$ ) or NUV magnitudes. Several ongoing surveys will provide such photometric data, in particular SkyMapper, which measures the Strömgren  $u$ -band, and the Gaia space mission, which will measure spectrophotometry in 30 bands with fine sampling of the Balmer jump. All-sky NIR surveys will be important to study composite spectrum sdB binaries and constrain the properties of both components.

This will put us into an excellent position to constrain the properties of the known ( $> 5000$ ) hot subdwarfs (Geier *et al.* 2017), out of which we expect 50% to be close binaries as well as to enlarge the sample enormously from new discoveries, in particular from Gaia.

**Acknowledgment:** Some of the data presented in this paper were obtained from the Mikulski Archive for Space Telescopes (MAST). STScI is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS5-26555. Support for MAST for non-HST data provided by the NASA Office of Space Science via grant NNX09AF08G and by other grants and contracts. This publication makes use of data products from the AAVSO Photometric All Sky Survey (APASS). Funded by the Robert Martin Ayers Sciences Fund and the National Science Foundation. This work is based in part on data obtained as part of the UKIRT Infrared Deep Sky Survey. This publication makes use of data products from the Wide-

field Infrared Survey Explorer, which is a joint project of the University of California, Los Angeles, and the Jet Propulsion Laboratory/California Institute of Technology, funded by the National Aeronautics and Space Administration. This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation. This research has made use of the NASA/ IPAC Infrared Science Archive, which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

## References

Alam, S., Albareti, F. D., Allende Prieto, C., Anders, F., Anderson, S. F., Anderton, T. *et al.* 2015, *ApJS*, 219, 12.

Allard, F., Wesemael, F., Fontaine, G., Bergeron, P., & Lamontagne, R. 1994, *AJ*, 107, 1565–1576.

Asplund, M., Grevesse, N., Sauval, A. J., & Scott, P. 2009, *ARA&A*, 47, 481–522.

Aznar Cuadrado, R. & Jeffery, C. S. 2001, *A&A*, 368, 994–1005.

Aznar Cuadrado, R. & Jeffery, C. S. 2002, *A&A*, 385, 131–142.

Cutri, R. M. *et al.* 2013, *VizieR Online Data Catalog*, 2328.

Fitzpatrick, E. L. 1999, *PASP*, 111, 63–75.

Geier, S. 2013, *A&A*, 549, A110.

Geier, S., Kupfer, T., Heber, U., Schaffenroth, V., Barlow, B. N., Østensen, R. H., *et al.* 2017, *A&A*, 602, C2.

Green, E. M., Fontaine, G., Hyde, E. A., For, B.-Q., & Chayer, P. 2008, In: U. Heber, C. S. Jeffery, & R. Napiwotzki (Eds.), *Hot Subdwarf Stars and Related Objects* (23–27 July 2007, Bamberg, Germany), *ASP Conf. Ser.*, 392, 75–82.

Green, R. F., Schmidt, M., & Liebert, J. 1986, *ApJS*, 61, 305–352.

Heber, U. 1986, *A&A*, 155, 33–45.

Heber, U. 2009, *ARA&A*, 47, 211–251.

Heber, U. 2016, *PASP*, 128, 082001.

Heber, U., Hunger, K., Jonas, G., & Kudritzki, R. P. 1984, *A&A*, 130, 119–130.

Heber, U., Moehler, S., Napiwotzki, R., Thejll, P., & Green, E. M. 2002, *A&A*, 383, 938–951.

Heber, U., Reid, I. N., & Werner, K. 2000, *A&A*, 363, 198–207.

Henden, A. A., Templeton, M., Terrell, D., *et al.* 2016, *VizieR Online Data Catalog*, 2336.

Houck, J. C. & Denicola, L. A. 2000, In: N. Manset, C. Veillet, & D. Crabtree (Eds.), *Astronomical Data Analysis Software and Systems IX*, *ASP Conf. Ser.*, 216, 591–594.

Hubeny, I., Hummer, D. G., & Lanz, T. 1994, *A&A*, 282, 151–167.

Husser, T.-O., Wende-von Berg, S., Dreizler, S., Homeier, D., Reiners, A., Barman, T., *et al.* 2013, *A&A*, 553, A6.

Kawka, A., Vennes, S., O'Toole, S., Németh, P., Burton, D., Kotze, E., *et al.* 2015, *MNRAS*, 450, 3514–3548.

Kupfer, T., Geier, S., Heber, U., Østensen, R. H., Barlow, B. N., Maxterd, P. F. L., *et al.* 2015, *A&A*, 576, A44.

Kurucz, R. L. 1996, In: S. J. Adelman, F. Kupka, & W. W. Weiss (Eds.), *Model Atmospheres and Spectrum Synthesis*, ASP Conf. Ser., 108, 160–164.

Lawrence, A., Warren, S. J., Almaini, O., Edge, A. C., Hambly, N. C., Jameson, R. F. et al. 2007, *MNRAS*, 379, 1599–1617.

Maxted, P. F. L., Heber, U., Marsh, T. R., & North, R. C. 2001, *MNRAS*, 326, 1391–1402.

Naslim, N., Jeffery, C. S., Hibbert, A., & Behara, N. T. 2013, *MNRAS*, 434, 1920–1929.

Ohl, R. G., Chayer, P., & Moos, H. W. 2000, *ApJ*, 538, L95

Østensen, R. H. 2006, *Baltic Astronomy*, 15, 85–90.

Saffer, R. A., Bergeron, P., Koester, D., & Liebert, J. 1994, *ApJ*, 432, 351–366.

Skrutskie, M. F., Cutri, R. M., Stiening, R., Weinberg, M. D., Schneider, S., Carpenter, J. M. et al. 2006, *AJ*, 131, 1163–1183.

Stark, M. A. & Wade, R. A. 2003, *AJ*, 126, 1455–1471.

Wright, E. L., Eisenhardt, P. R. M., Mainzer, A. K., Mainzer, A. K., Ressler, M. E., Cutri, R. M. et al. 2010, *AJ*, 140, 1868–1881.