

# Temperature Dependence of The Raman Frequency Shifts Related to The Specific Heat and Thermal Expansion Close To I-II Phase Transition in S-Triazine.

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## ABSTRACT

A linear variation of the specific heat  $C_p$  with the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  is established for the Raman modes I-V at various temperatures ( $P=0$ ) close to I-II phase transition in s-triazine ( $T_c=198$  K).

As an extension of this work, the temperature dependence of the thermal expansion  $\alpha_p$  is predicted from the frequency shifts and by the  $\gamma_p$  values deduced for the Raman modes studied close to the I-II phase transition in s-triazine.

Our predicted  $\alpha_p$  can be examined by the thermodynamics measurements of the thermal expansion at various temperatures at zero pressure in both phases I and II of s-triazine.

**Keywords:** Raman modes. Frequency shifts. Phase transition. s-triazine.

## 1. INTRODUCTION

A structural phase change occurs in s-triazine at about 198 K /1/, as observed experimentally by x-ray diffraction and adiabatic calorimetry /2, 3/. This is the

I-II phase transition as the temperature decreases. The crystal structure of the high-temperature phase (I) of s-triazine belongs to the rhombohedral space group  $R\bar{3}c$  /4/. This transforms to a triply-twinned monoclinic phase (II) with decreasing temperature below  $T_c$ . It is a reversible temperature induced transformation to a lower symmetric phase accompanied by twinning /1/.

It has been reported that the low temperature structure (phase II) can be generated from the high-temperature hexagonal form (phase I) by shearing the crystal in the  $ac^*$  plane and rotating the molecules about the b-axis /2/. Thus, the shear and rotation angles have been measured as a function of temperature in the temperature range 110 to 198 K in phase II /2/. As observed by the measurements of coherent inelastic neutron scattering /5, 6/ and Brillouin scattering /7/, Rae /8/ has studied the I-II transition by proposing that it is accompanied with a soft acoustic mode.

Several experimental studies have been carried out to investigate the mechanism of the I-II phase transition in s-triazine. The measurements associated with the I-II phase transition in s-triazine at low pressures on the specific heat /3/ and nuclear quadrupole resonance /9/, have been reported.

Various theoretical studies regarding I-II transition in s-triazine have also been reported in the literature /8, 10-14/. Very recently, we have analyzed the temperature dependence of the observed specific heat

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/3/ close to the I-II phase transition in s-triazine according to power-law formula /15/. We have calculated the specific heat using the quasi-harmonic and mean field approximation for s-triazine /16/. In order to understand the dynamical properties of the I-II transition in s-triazine, we have also studied the temperature dependence of the damping constant /17/.

The Raman spectra of s-triazine have revealed the mechanism of I-II phase transition under various temperatures and pressures. The Raman measurements of s-triazine have been conducted by several workers /18-22/. The Raman modes of I-V have been observed at various temperatures at atmospheric pressure in the phases I and II of s-triazine /21/. They have also been observed as a function of pressure at room temperature in the pressure range of 0 to 5 kbar (phase I) and from 5.1 to 40.5 kbar (phase II) in s-triazine /22/. Among those Raman modes, bands I and II have been assigned as the low frequency  $E_g$  mode of the high-temperature phase (phase I), and also bands IV and V as the high frequency  $E_g$  mode of phase I /21/. Thus, the low frequency  $E_g$  mode of the high-temperature phase (I) splits into the Raman bands I and II in the low-temperature phase (phase II). Also, the high frequency  $E_g$  mode of phase I splits into the Raman bands IV and V in phase II, as pointed out previously /21/. The Raman band III which is unobservable above 170 K, corresponds to the molecular motions  $R_z$  and  $T_z$ , and it is Raman inactive in the high-temperature phase I /21/.

In this study, using the observed frequencies of the Raman modes I-V /21/ and the observed specific heat  $C_p$  data /3/, at various temperatures at zero pressure, we establish the spectroscopic modification of the Pippard relation close to the I-II phase transition in s-triazine. This gives a linear variation of  $C_p$  with the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  for the Raman modes studied here in

s-triazine. From linear plots of  $C_p$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ ,

values of the isobaric mode Grüneisen parameter  $\gamma_p$  are extracted for the Raman modes in both phases I and II, and the thermal expansion  $\alpha_p$  is calculated as a function of temperature close to the I-II phase transition in this molecular crystal.

Below, we give in section 2 our calculations for the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ ,  $\gamma_p$  and  $\alpha_p$  in phases I and II of s-triazine. In section 3 our discussion about the results is given. Finally, conclusions are given in section 4.

## 2. CALCULATIONS AND RESULTS

The specific heat  $C_p$  can be related to the thermal expansion  $\alpha_p$  close to the I-II transition in s-triazine according to the Pippard relation

$$C_p = T \left( \frac{dP}{dT_c} \right) \alpha_p V + T \left( \frac{dS}{dT} \right)_i \quad (1)$$

In Eq.(1) the slope  $dP/dT_c$  and the variation of entropy with the temperature,  $(dS/dT)_i$ , are taken at the transition temperature  $T_c$  (198 K) in s-triazine.  $V$  is the crystal volume. By the mode Grüneisen parameter  $\gamma$ , the crystal volume can be related to the vibrational frequency  $\omega$  according to

$$\gamma = -\frac{V}{\omega} \frac{d\omega}{dV} \quad (2)$$

or by defining isobaric mode Grüneisen parameter  $\gamma_p$  as

$$\gamma_p = -\frac{1}{\alpha_p} \cdot \frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p \quad (3)$$

where the thermal expansion  $\alpha_p \equiv \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_p$ . The Pippard relation given by Eq.(1) can be written as

$$C_p/R = -\frac{TV}{\gamma_p} \left( \frac{dP}{dT} \right)_c \cdot \frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p + T \left( \frac{dS}{dT} \right)_i \quad (4)$$

Here  $R$  is the gas constant. This relates the specific heat  $C_p$  to the variation of the vibrational frequency with the temperature (frequency shift),  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ . Thus, the

specific heat  $C_p$  measured thermodynamically can be plotted as a function of the frequency shifts,  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ , measured spectroscopically at various temperatures for a constant pressure ( $P=0$ ) close to the I-II phase transition in s-triazine according to Eq.(4). This linear plot gives the value of the mode Grüneisen parameter  $\gamma_p$  for the relevant phonon by knowing the values of the slope ( $dP/dT$ ) and the crystal volume at  $T=T_c$ .

In this study, we established the Pippard relation modified spectroscopically (Eq.(4)) using the observed specific heat  $C_p$  [3] and the observed Raman frequencies of the modes I, II, III, IV and V [21] at various temperatures (zero pressure) in phases I and II ( $T_c = 198$  K) in s-triazine. A linear relationship was established between  $C_p$  and the Raman frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  for the five Raman modes (I-V) close to the I-II phase transition in the phases I ( $T > T_c$ ) and II ( $T < T_c$ ) in s-triazine according to Eq.(4). From this linear

relationship, the values of the mode Grüneisen parameter  $\gamma_p$  were obtained for the Raman modes studied here. For this procedure, we first fitted with Eq.(5) to the temperature dependence of the measured Raman frequencies [3] for the modes I and IV in the phase I ( $T > T_c$ ), and then to the Raman frequencies for the modes I, II, III, IV and V in phase II ( $T < T_c$ ).

$$\omega = a + bT \quad (5)$$

Table 1 gives the fitted parameters  $a$  and  $b$  for all the modes studied here. We then determined  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  as a function of temperature for the Raman modes in phase I (modes I and IV) and in phase II (modes I-V). Thus, the observed specific heat  $C/R$  [3], was plotted against the Raman frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  for those modes according to Eq.(4) for the phases I and II in s-triazine.

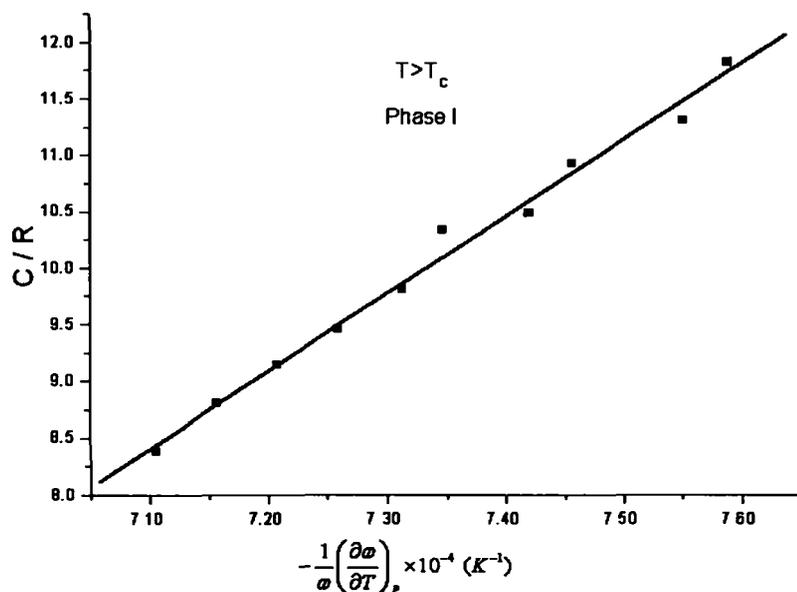
**Table 1**

Values of the parameters  $a$  and  $b$  according to Eq.(5) for the observed frequencies [21] of the Raman modes indicated at various temperatures in the phases I and II of s-triazine

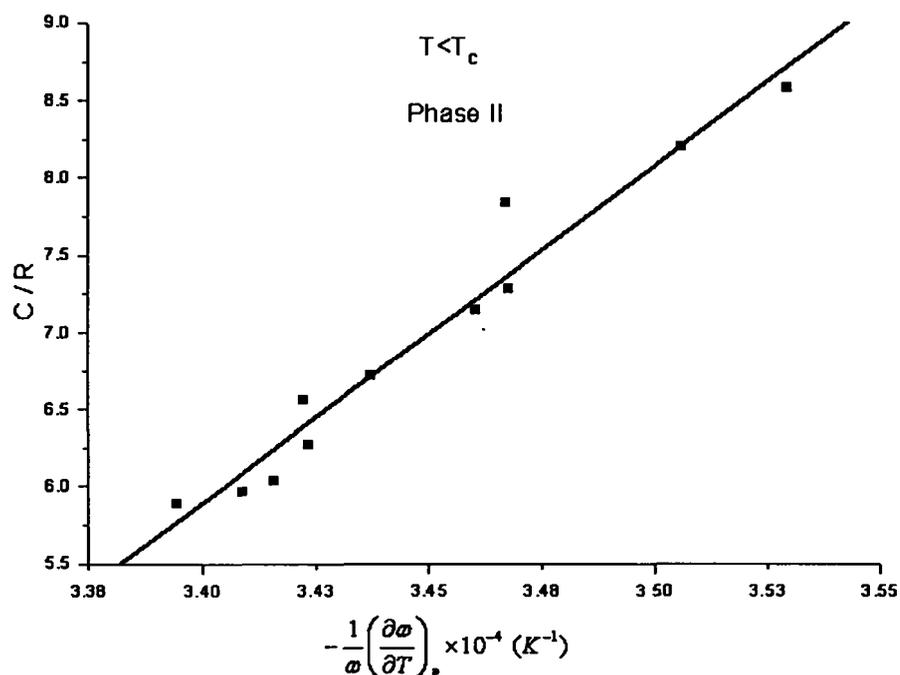
$T_c=198.07$ K	$T > T_c$ (Phase I)		$T < T_c$ (Phase II)	
Raman modes	$a \times 10^{-2}$ (m <sup>-1</sup> )	$-b \times 10^{-2}$ (m <sup>-1</sup> /K)	$a \times 10^{-2}$ (m <sup>-1</sup> )	$-b \times 10^{-2}$ (m <sup>-1</sup> /K)
I	82.80	0.052	81.43	0.027
II	-	-	97.89	0.125
III	-	-	92.05	0.049
IV	114.58	0.075	111.96	0.061
V	-	-	126.32	0.133

Figures 1 and 2 give  $C/R$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  of the Raman mode I for the phases I ( $T > T_c$ ) and II ( $T < T_c$ ) of s-triazine, respectively according to Eq.(4). Since mode II appears in the Raman spectra of s-triazine in phase II only [21], variation of  $C/R$  with the frequency shifts of this mode is plotted in Figure 3. Similarly, mode III appears only in phase II ( $T < T_c$ ) as the Raman mode II [21]. We plot  $C/R$  against the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  of the Raman

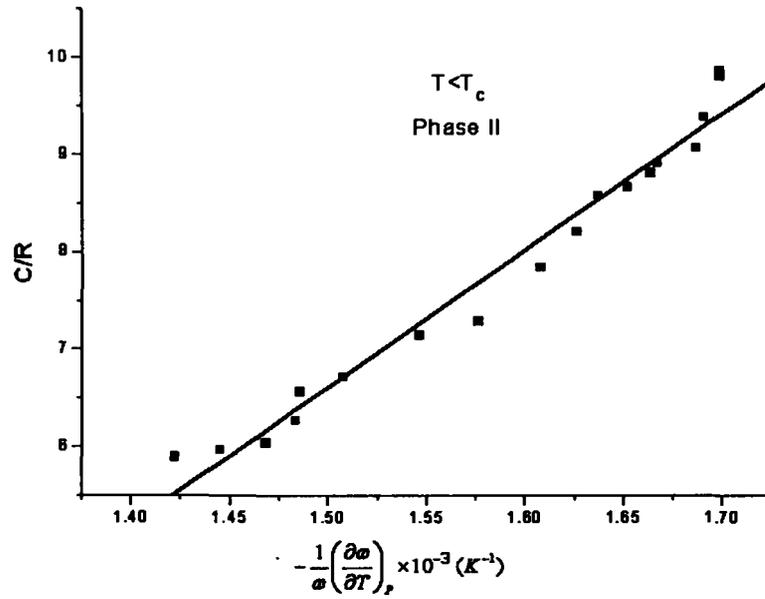
mode III for phase II ( $T < T_c$ ) in Figure 4. For the Raman mode IV, variation of  $C/R$  with the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  in phases I and II, is plotted in Figure 5 and Figure 6, respectively. Also, the Raman mode V exists in phase II ( $T < T_c$ ) only similar to the Raman modes II and III [21]. Figure 7 gives our plot of  $C/R$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  for the Raman mode V below  $T_c$  (phase II) in s-triazine.



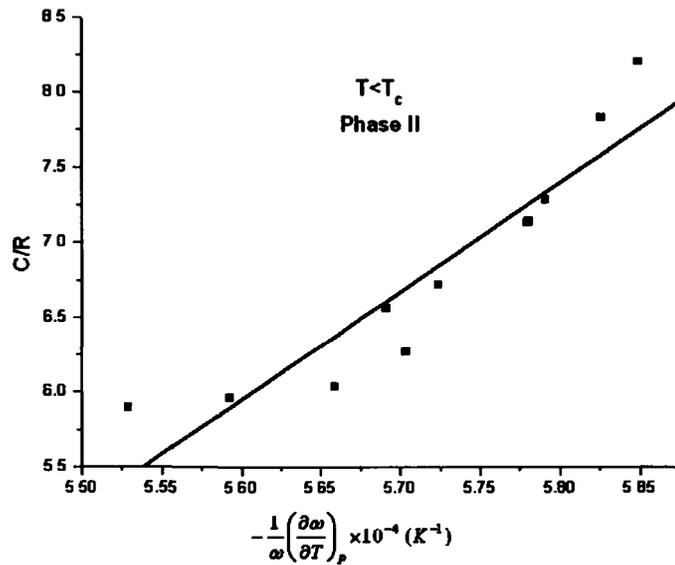
**Fig. 1:** Observed specific heat  $C/R$  ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  obtained from the observed Raman frequencies  $\omega$  at various temperatures ( $P=0$ ) for the Raman mode I according to Eq.(4) above the transition temperature ( $T_c=198.07$  K) in the phase I of s-triazine.



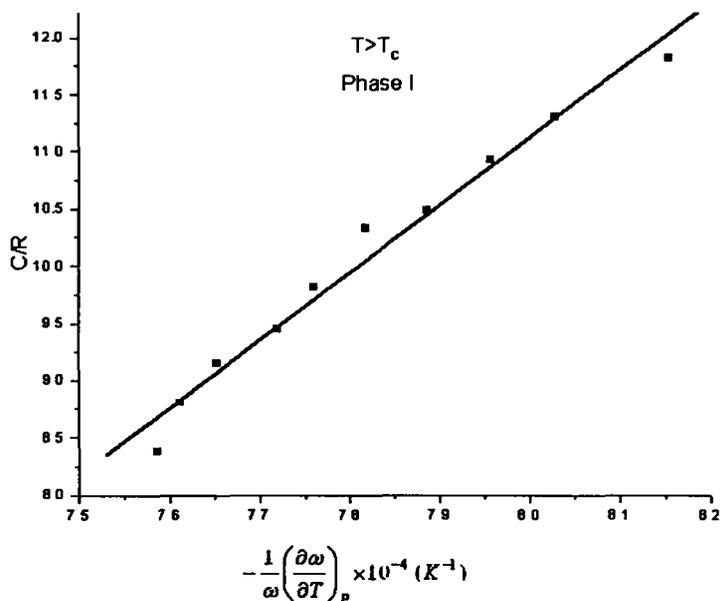
**Fig. 2:** Observed specific heat  $C/R$  ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  obtained from the observed Raman frequencies  $\omega$  at various temperature ( $P=0$ ) for the Raman mode I according to Eq.(4) below the transition temperature ( $T_c=198.07$  K) in the phase II of s-triazine.



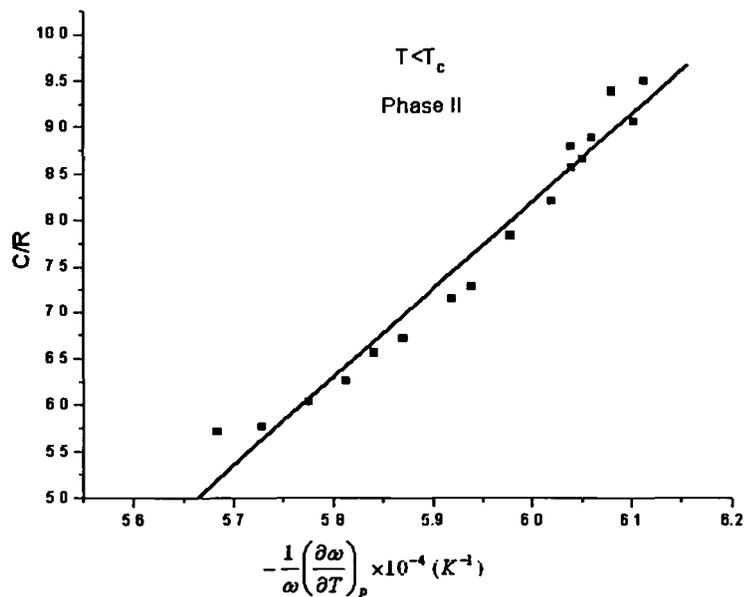
**Fig. 3:** Observed specific heat  $C/R$  ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  obtained from the observed Raman frequencies  $\omega$  at various temperatures ( $P=0$ ) for the Raman mode II according to Eq.(4) below the transition temperature ( $T_c=198.07$  K) in the phase II of s-triazine.



**Fig. 4:** Observed specific heat  $C/R$  ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  obtained from the observed Raman frequencies  $\omega$  at various temperatures ( $P=0$ ) for the Raman mode III according to Eq.(4) below the transition temperature ( $T_c=198.07$  K) in the phase II of s-triazine.



**Fig. 5:** Observed specific heat  $C/R$  /3/ ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_P$  obtained from the observed Raman frequencies /21/ at various temperatures ( $P=0$ ) for the Raman mode IV according to Eq.(4) above the transition temperature ( $T_c=198.07$  K) in the phase I of s-triazine.



**Fig. 6:** Observed specific heat  $C/R$  /3/ ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_P$  obtained from the observed Raman frequencies /21/ at various temperatures ( $P=0$ ) for the Raman mode IV according to Eq.(4) below the transition temperature ( $T_c=198.07$  K) in the phase II of s-triazine.

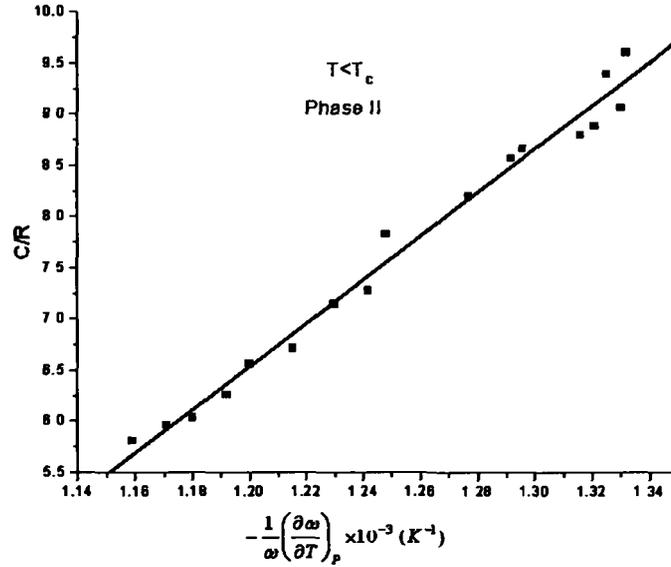


Fig. 7: Observed specific heat  $C/R$  ( $R$  is the gas constant) as a function of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  obtained from the observed Raman frequencies  $\omega$  at various temperatures ( $P=0$ ) for the Raman mode V according to Eq.(4) below the transition temperature ( $T_c=198.07$  K) in the phase II of s-triazine.

We extracted the values of the mode Grüneisen parameter  $\gamma_p$  for the Raman modes I-V studied here from our plots of the specific heat  $C/R$  against the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ , as given in Figures (1-7)

according to Eq.(4). The  $\gamma_p$  values of those modes were determined for both phases I ( $T > T_c$ ) and II ( $T < T_c$ ) in s-triazine. Since the modes II and V do not appear in the Raman spectra  $\omega$  in phase I ( $T > T_c$ ), we considered here that they were originated from the modes I and IV, respectively, in the phase I. So that, we took the same  $\gamma_p$  value for the Raman mode II as the mode I in phase I ( $T > T_c$ ). Also, we assumed the same  $\gamma_p$  values for the Raman mode V as the mode IV in phase I ( $T > T_c$ ). Due to the fact that the Raman mode III appears only in phase II ( $T < T_c$ ), as stated above, we were unable to extract its  $\gamma_p$  value in phase I ( $T > T_c$ ). Table 2 gives our values of the mode Grüneisen parameter  $\gamma_p$  for the Raman modes I-V in the phases I and II with the values of the intercept  $(dS/dT)_c$  at the transition temperature ( $T_c=198.07$  K) for the I-II transition in s-triazine. When

we determined the  $\gamma_p$  values from our plots of  $C/R$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  from Eq.(4), we used the slope value of the transition temperature according to the empirical relation

$$T_c = 198 + 18.7 P \quad (6)$$

which was obtained experimentally in the  $P$ - $T$  phase diagram [23, 24], as also given in the previous work [22]. In Eq.(6),  $T_c$  is in the units of Kelvin (K) and the pressure in kbars. So, the  $(dP/dT)_c=5.348$  MPa/K(=53.48 bar/K) was obtained from Eq.(6), which was used in Eq.(4). The volume  $V$  value was obtained from the density value of  $\rho=1376$  kg/m<sup>3</sup> [4] and the mass value of  $M=81 \times 10^{-3}$  kg/mol of s-triazine ( $C_3H_3N_3$ ), which gave  $V=58.866 \times 10^{-6}$  m<sup>3</sup>/mol. Using those values of  $T_c=198.07$  K,  $(dP/dT)_c$  and  $V$ , the  $\gamma_p$  values for the Raman modes (I-V) were extracted from Eq.(4), as given in Table 2.

**Table 2**

Values of the isobaric mode Grüneisen parameter  $\gamma_p$  for the Raman modes indicated and the values for the variation of the entropy with the temperature,  $(dS/dT)_i$  (normalized with the gas constant R because of the observed specific heat  $C/R$  /3/) at the transition temperature  $T_c$  in the phases I and II of s-triazine according to Eq.(4).

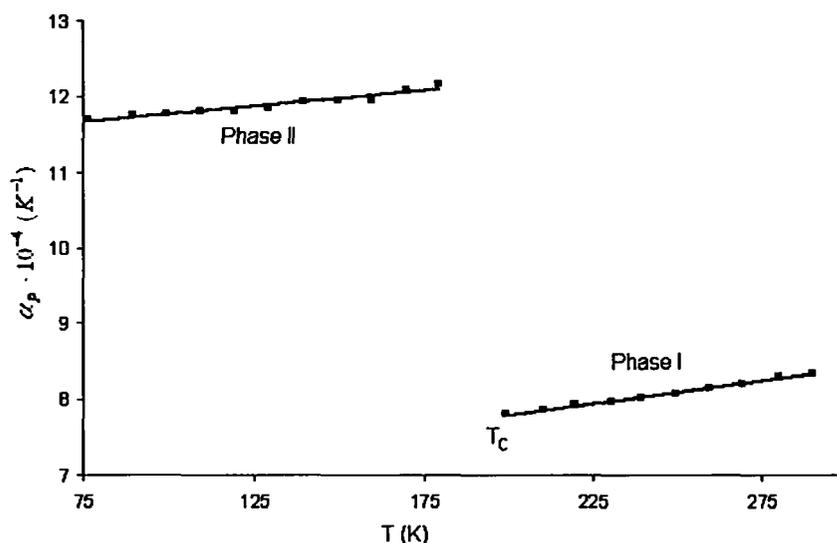
$T_c=198.07$ K	$T > T_c$ (Phase I)		$T < T_c$ (Phase II)	
Raman modes	$\gamma_p$	$-(dS/dT)_i$ (K <sup>-1</sup> )	$\gamma_p$	$-(dS/dT)_i$ (K <sup>-1</sup> )
I	0.91	0.20	0.29	0.34
II	0.91	0.20	4.44	0.07
III	-	-	0.86	0.18
IV	1.06	0.18	0.66	0.25
V	1.06	0.18	2.95	0.10

As an extension of this study, we also calculated here the temperature dependence of the thermal expansion  $\alpha_p$  by knowing the values of the mode Grüneisen parameter  $\gamma_p$  of the Raman modes considered (Table 2), according to Eq.(3). By using the temperature dependence of the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$ , the  $\alpha_p$

values were calculated as a function of temperature. Figures 8 and 9 give the temperature dependence of the thermal expansion  $\alpha_p$  calculated from the frequency

shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  of the Raman modes I and II, respectively. As shown in Figure 9, we had the same  $\alpha_p$  values calculated using the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$

Raman mode II as the Raman mode I (Figure 8) above  $T_c$  (phase I) with the same  $\gamma_p$  value (Table 1) since the modes I and II in phase II merge to give a single Raman mode in phase I ( $T > T_c$ ), as observed experimentally [21].



**Fig. 8:** Temperature dependence of the thermal expansion  $\alpha_p$  calculated from Eq.(3) using the observed Raman frequencies [21] of the mode I close to the I-II phase transition in s-triazine ( $T_c=198$  K).

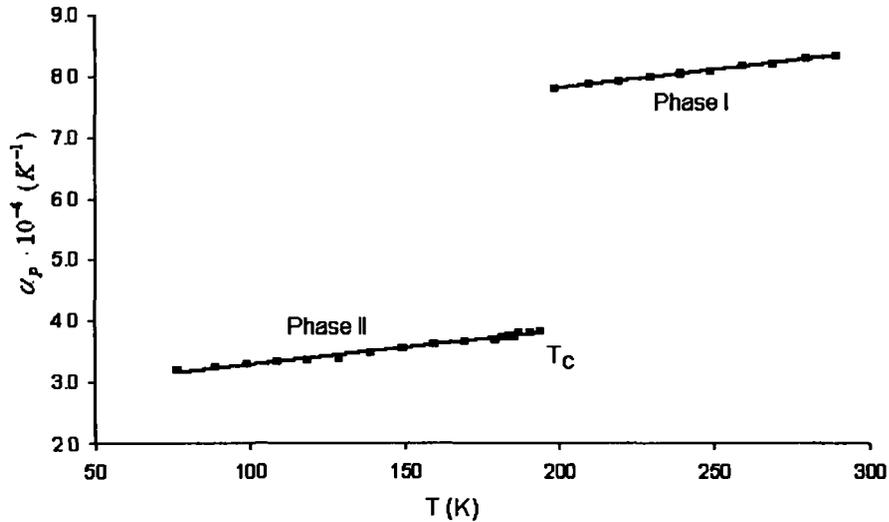


Fig. 9: Temperature dependence of the thermal expansion  $\alpha_p$  calculated from Eq.(3) using the observed Raman frequencies /21/ of the mode II close to the I-II phase transition in s-triazine ( $T_c=198$  K).

Figure 10 gives the thermal expansion  $\alpha_p$  as a function of temperature below  $T_c$  (phase II) in s-triazine, which was calculated using the Raman frequencies of the mode III according to Eq.(3). Since there was no observed frequency data for this mode above  $T_c$  /21/, we were not able to calculate the temperature dependence of  $\alpha_p$  in phase I. We also plot the thermal expansion  $\alpha_p$  calculated using the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  values of the Raman

modes IV and V as a function of temperature in Figure 11 and Figure 12, respectively. For the same reason as the Raman modes I and II, we considered that the modes IV and V in phase II ( $T < T_c$ ) merge to give a single mode in phase I ( $T > T_c$ ), as observed experimentally /21/. So that we obtained the same values of the thermal expansion  $\alpha_p$  above  $T_c$  for both modes IV (Figure 11) and V (Figure 12).

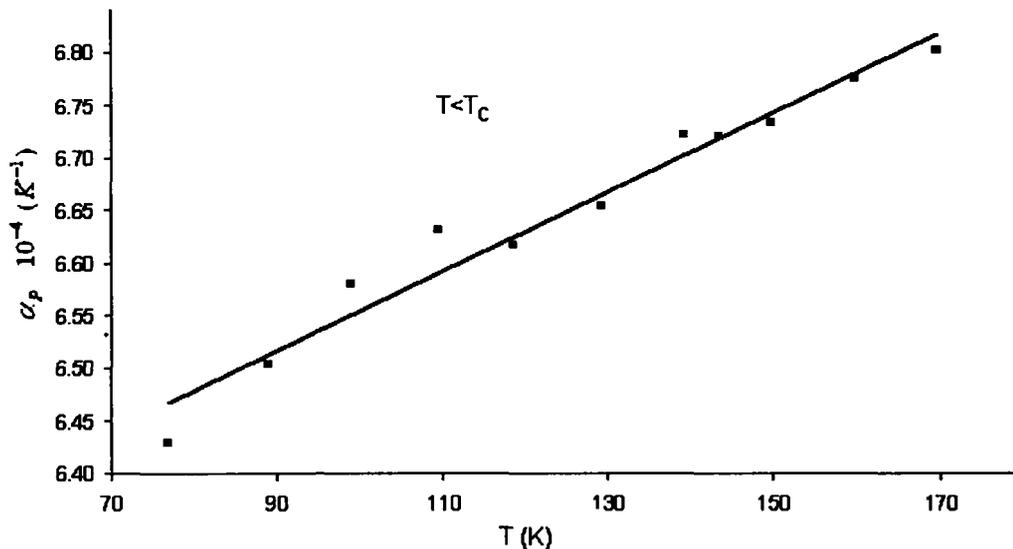


Fig. 10: Temperature dependence of the thermal expansion  $\alpha_p$  calculated from Eq.(3) using the observed Raman frequencies /21/ of the mode III in phase II of s-triazine ( $T_c=198$ K).

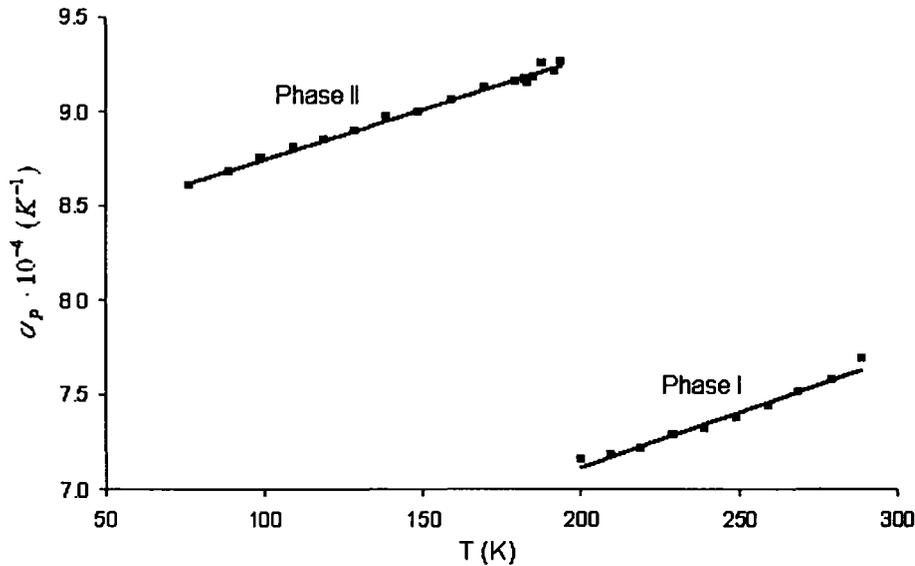


Fig. 11: Temperature dependence of the thermal expansion  $\alpha_p$  calculated from Eq.(3) using the observed Raman frequencies  $\omega/21$  of the mode IV close to the I-II phase transition in s-triazine ( $T_c=198$  K).

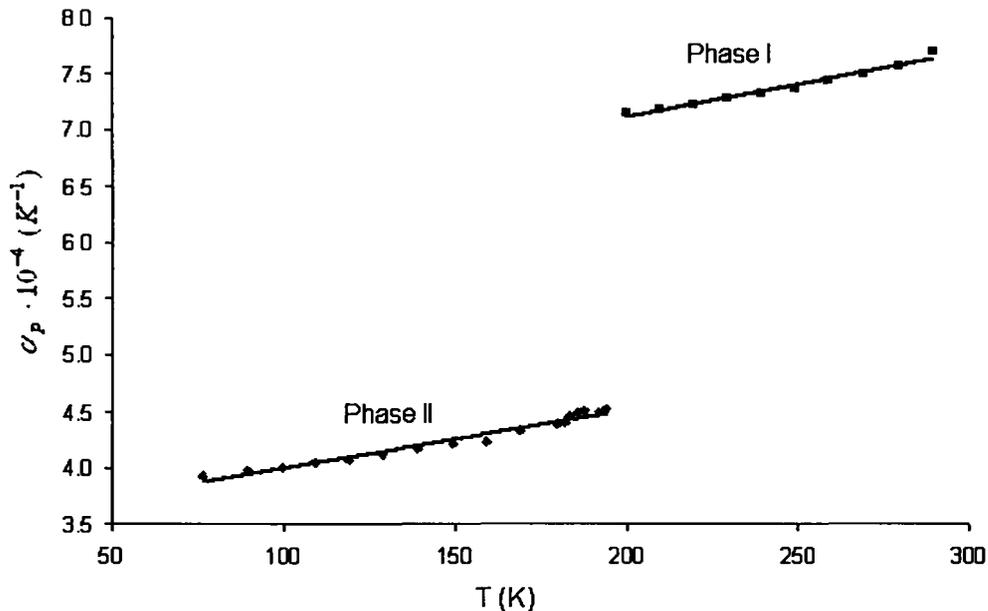


Fig. 12: Temperature dependence of the thermal expansion  $\alpha_p$  calculated from Eq.(3) using the observed Raman frequencies  $\omega/21$  of the mode V close to the I-II phase transition in s-triazine ( $T_c=198$  K).

### 3. DISCUSSION

A linear variation of the specific heat  $C/R$  with the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  was established at various temperatures in phases I ( $T > T_c$ ) and II ( $T < T_c$ ) of s-

triazine, as shown in Figures (1-7). This was obtained in both phases I and II using the frequencies of the Raman modes I and IV. Linear plots of  $C/R$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  were obtained for the Raman modes II, III and V in phase II ( $T < T_c$ ) only since there was no Raman data  $\omega/21$

in phase I ( $T > T_c$ ) for those modes considered. Thus, Figures (1-7) show that there is a linear relationship between the specific heat  $C/R$  and the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  close to the I-II transition in s-triazine according to the spectroscopic modification of the Pippard relation (Eq.4)

From the linear plots of  $C/R$  against  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$

(Figures 1-7), the values of the mode Grüneisen parameter  $\gamma_p$  were deduced for the Raman modes I to V in phase II ( $T < T_c$ ), as tabulated in Table 2. In phase I ( $T > T_c$ ) the  $\gamma_p$  values were determined for the Raman modes I to V except the Raman mode III since there were no observed frequencies  $|21|$  in this phase of s-triazine. In phase I ( $T > T_c$ ) the value of  $\gamma_p \approx 1$  was obtained for the Raman modes of I, II, IV and V, whereas the  $\gamma_p$  values varied from 0.3 to nearly 4 for all the modes I to IV in phase II ( $T < T_c$ ) in s-triazine (Table 2).

We also deduced the values of the  $(dS/dT)_i$  from Eq.(4) for the phases I ( $T > T_c$ ) and II ( $T < T_c$ ) of s-triazine, as given in Table 2. The  $(dS/dT)_i$  values obtained from the Raman frequencies of the modes I, II, IV and V, were the same as nearly 0.2 in phase I ( $T > T_c$ ) (Table 2). For the phase II ( $T < T_c$ ), the values of  $(dS/dT)_i$  varied from 0.1 to 0.3  $K^{-1}$  which were obtained from the Raman frequencies of all the modes (I to V) in s-triazine (Table 2)

Since we determined the values of the isobaric mode Grüneisen parameter  $\gamma_p$  for the Raman modes studied here in the phases I ( $T > T_c$ ) and II ( $T < T_c$ ), we were able to calculate the thermal expansion  $\alpha_p$  as a function of temperature according to Eq.(3), as given in Figures (8-12). The  $\alpha_p$  was calculated as a function of temperature, using the Raman frequencies of the mode III in phase II ( $T < T_c$ ) only, since we were able to determine its  $\gamma_p$  value in this phase (Table 2), as given in Figure 10. The temperature dependence of the thermal expansion  $\alpha_p$  exhibits similar critical behaviour due to the Raman modes I (Figure 8) and IV (Figure 11), which jumps considerably to the lower values with increasing temperature in s-triazine. On the other hand, the critical behavior of the thermal expansion  $\alpha_p$  is similar that was calculated from the Raman frequencies of the modes II (Figure 9) and V (Figure 12). The  $\alpha_p$  increases with increasing temperature by exhibiting a jump at  $T_c$ , as shown in Figures 9 and 12. We note that the  $\alpha_p$  has the same values in phase I ( $T > T_c$ ), which were obtained from the Raman frequencies of the modes I and II (Figures 8 and 9). Also, the  $\alpha_p$  values are the same in phase I ( $T > T_c$ ), which was obtained using the Raman frequencies of the modes IV and V, as given in Figures 11 and 12, respectively. By extending the  $\alpha_p$  to the transition temperature  $T_c = 198.07$  K from both phases I ( $T > T_c$ ) and II ( $T < T_c$ ), we calculated their values, as tabulated in Table 3.

**Table 3**

Values of the thermal expansion  $\alpha_p$  extended to the transition temperature ( $T_c = 198.07$  K) from both phases I ( $T > T_c$ ) and II ( $T < T_c$ ), which were calculated using the Raman frequencies of the modes indicated according to Eq.(3).

Difference in the  $\alpha_p$  values at  $T_c$ , (Eq. 7)  $\Delta\alpha_p = \alpha_p(T > T_c) - \alpha_p(T < T_c)$ , is also given here.

$T_c = 198.07$ K	$T > T_c$ (Phase I)	$T < T_c$ (Phase II)	$T = T_c$ (K)
Raman Modes	$\alpha_p \times 10^{-4}$ ( $K^{-1}$ )	$\alpha_p \times 10^{-4}$ ( $K^{-1}$ )	$\Delta\alpha_p \times 10^{-4}$ ( $K^{-1}$ )
I	7.80	12.20	-4.40
II	7.80	3.84	3.96
III	-	6.94	-
IV	7.11	9.27	-2.16
V	7.11	4.52	2.59

They were calculated using the Raman frequencies of the modes I, II, III (phase II only), IV and V according to Eq.(3) by using the values of the mode Grüneisen parameter  $\gamma_p$  (Table 2). We also give the values of the difference (jump) in  $\alpha_p$  which we defined as

$$\Delta\alpha_p = \alpha_p(T > T_c) - \alpha_p(T < T_c) \quad (7)$$

due to the Raman modes studied in s-triazine. For the Raman modes I and II, the difference in  $\alpha_p$  is about the same with the decreasing (-) and increasing (+) values, as the temperature decreases from phase I ( $T > T_c$ ) to phase II ( $T < T_c$ ). Also, the  $\Delta\alpha_p$  value is nearly the same for the Raman modes IV and V with the decreasing (-) and increasing (+) values, as before.

The critical behaviour of the thermal expansion  $\alpha_p$  which we predicted in this study using the Raman frequencies of the modes considered, can be examined by the measurements of the  $\alpha_p$  at various temperatures ( $P=0$ ) close to the I-II phase transition in s-triazine. From the thermodynamics measurements, the change in the thermal expansion at  $T_c$ ,  $\Delta\alpha_p$ , can also be determined and it can then be compared with our calculated values given in Table 3.

#### 4. CONCLUSIONS

The spectroscopic modification of the Pippard relation was constructed by a linear variation of the specific heat  $C/R$  with the frequency shifts  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  close to the I-II phase transition in s-triazine. The observed specific heat and the observed frequencies of the Raman modes I, II, III, IV and V were used for this linear variation of  $C/R$  with the  $\frac{1}{\omega} \left( \frac{\partial \omega}{\partial T} \right)_p$  in phases I and II of s-triazine. From linear plots, the values of the isobaric mode Grüneisen parameter  $\gamma_p$  were extracted for the Raman modes studied here. By means of the  $\gamma_p$  values, the thermal expansion  $\alpha_p$  was calculated as a function of temperature at zero pressure close to the I-II phase transition in s-triazine.

Measurements of the length-change or the lattice parameter which can be conducted at various temperatures ( $P=0$ ), can be compared with our predictions of the thermal expansion  $\alpha_p$  near the I-II phase transition in s-triazine.

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