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V. G. Turaev

Quantum Invariants of Knots and 3-Manifolds

With 206 illustrations



Walter de Gruyter
Berlin · New York 1994

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1991 Mathematics Subject Classification: 57-02, 18-02; 17B37, 81Txx, 82B23

Key words: Topological field theory, knots, 3-manifold invariants,
state sums, monoidal categories

⊗ Printed on acid-free paper which falls within the guidelines of the ANSI to ensure permanence and durability.

Library of Congress Cataloging-in-Publication Data

Turaev, V. G. (Vladimir G.), 1954–

Quantum invariants of knots and 3-manifolds / V. G. Turaev.

p. cm. – (De Gruyter studies in mathematics : 18)

Includes bibliographical references and index.

ISBN 3-11-013704-6 (acid-free paper)

1. Quantum field theory. 2. Knot theory. 3. Three-manifolds (Topology) 4. Invariants. 5. Mathematical physics.

I. Title. II. Series.

QC174.52.C66T87 1994

512'.55–dc20

94-21249

Die Deutsche Bibliothek – Cataloging-in-Publication Data

Turaev, Vladimir G.:

Quantum invariants of knots and 3-manifolds / V. G. Turaev. –

Berlin ; New York : de Gruyter, 1994

(De Gruyter studies in mathematics ; 18)

ISBN 3-11-013704-6

NE: GT

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Disk conversion: Lewis & Leins, Berlin. Printing: Arthur Collignon GmbH, Berlin. Binding: Dieter Mikolai, Berlin. Cover design: Rudolf Hübler, Berlin.

Illustrations: DTP L. C. & R. Hartmann, Haierweg 47, D-79114 Freiburg

Dedicated to my parents

